

# Mathematica 11.3 Integration Test Results

Test results for the 358 problems in "4.1.3.1 (a+b sin)^m (c+d sin)^n (A+B sin).m"

Problem 1: Unable to integrate problem.

$$\int (d \sin[e + f x])^n (a + a \sin[e + f x])^3 (A + B \sin[e + f x]) dx$$

Optimal (type 5, 373 leaves, 7 steps):

$$\begin{aligned} & - \frac{a^3 (B (27 + 14 n + 2 n^2) + A (28 + 15 n + 2 n^2)) \cos[e + f x] (d \sin[e + f x])^{1+n}}{d f (2 + n) (3 + n) (4 + n)} + \\ & \left( a^3 (B (15 + 19 n + 4 n^2) + A (20 + 21 n + 4 n^2)) \cos[e + f x] \right. \\ & \quad \left. \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+n}{2}, \frac{3+n}{2}, \sin[e + f x]^2\right] (d \sin[e + f x])^{1+n}\right) / \\ & \left( d f (1 + n) (2 + n) (4 + n) \sqrt{\cos[e + f x]^2} \right) + \left( a^3 (B (9 + 4 n) + A (11 + 4 n)) \cos[e + f x] \right. \\ & \quad \left. \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2+n}{2}, \frac{4+n}{2}, \sin[e + f x]^2\right] (d \sin[e + f x])^{2+n}\right) / \\ & \left( d^2 f (2 + n) (3 + n) \sqrt{\cos[e + f x]^2} \right) - \frac{a B \cos[e + f x] (d \sin[e + f x])^{1+n} (a + a \sin[e + f x])^2}{d f (4 + n)} - \\ & \frac{(A (4 + n) + B (6 + n)) \cos[e + f x] (d \sin[e + f x])^{1+n} (a^3 + a^3 \sin[e + f x])}{d f (3 + n) (4 + n)} \end{aligned}$$

Result (type 9, 68520 leaves): Display of huge result suppressed!

Problem 2: Unable to integrate problem.

$$\int (d \sin[e + f x])^n (a + a \sin[e + f x])^2 (A + B \sin[e + f x]) dx$$

Optimal (type 5, 277 leaves, 6 steps):

$$\begin{aligned}
 & - \frac{a^2 (A (3+n) + B (4+n)) \cos[e+fx] (d \sin[e+fx])^{1+n}}{df (2+n) (3+n)} + \\
 & \left( a^2 (2B (1+n) + A (3+2n)) \cos[e+fx] \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1+n}{2}, \frac{3+n}{2}, \sin[e+fx]^2 \right] \right. \\
 & \quad \left. (d \sin[e+fx])^{1+n} \right) / \left( df (1+n) (2+n) \sqrt{\cos[e+fx]^2} \right) + \\
 & \left( a^2 (2A (3+n) + B (5+2n)) \cos[e+fx] \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{2+n}{2}, \frac{4+n}{2}, \sin[e+fx]^2 \right] \right. \\
 & \quad \left. (d \sin[e+fx])^{2+n} \right) / \left( d^2 f (2+n) (3+n) \sqrt{\cos[e+fx]^2} \right) - \\
 & \frac{B \cos[e+fx] (d \sin[e+fx])^{1+n} (a^2 + a^2 \sin[e+fx])}{df (3+n)}
 \end{aligned}$$

Result (type 9, 25571 leaves): Display of huge result suppressed!

**Problem 3: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (d \sin[e+fx])^n (a + a \sin[e+fx]) (A + B \sin[e+fx]) dx$$

Optimal (type 5, 191 leaves, 5 steps):

$$\begin{aligned}
 & - \frac{a B \cos[e+fx] (d \sin[e+fx])^{1+n}}{df (2+n)} + \\
 & \left( a (B (1+n) + A (2+n)) \cos[e+fx] \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1+n}{2}, \frac{3+n}{2}, \sin[e+fx]^2 \right] \right. \\
 & \quad \left. (d \sin[e+fx])^{1+n} \right) / \left( df (1+n) (2+n) \sqrt{\cos[e+fx]^2} \right) + \\
 & \frac{a (A+B) \cos[e+fx] \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{2+n}{2}, \frac{4+n}{2}, \sin[e+fx]^2 \right] (d \sin[e+fx])^{2+n}}{d^2 f (2+n) \sqrt{\cos[e+fx]^2}}
 \end{aligned}$$

Result (type 5, 392 leaves):

$$\begin{aligned}
 & \frac{1}{f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2} \\
 & 2^{-2-n} a e^{i f n x} \left( 1 - e^{2 i (e+f x)} \right)^{-n} \left( -i e^{-i (e+f x)} \left( -1 + e^{2 i (e+f x)} \right) \right)^n \\
 & \left( \frac{2 (A+B) e^{-i (e+f (1+n) x)} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2} (-1-n), -n, \frac{1-n}{2}, e^{2 i (e+f x)} \right]}{1+n} - \right. \\
 & \left. \frac{2 (A+B) e^{i (e-f (-1+n) x)} \operatorname{Hypergeometric2F1} \left[ \frac{1-n}{2}, -n, \frac{3-n}{2}, e^{2 i (e+f x)} \right]}{-1+n} + \right. \\
 & \left. i \left( \frac{B e^{-i (2e+f (2+n) x)} \operatorname{Hypergeometric2F1} \left[ -1 - \frac{n}{2}, -n, -\frac{n}{2}, e^{2 i (e+f x)} \right]}{2+n} + \frac{1}{(-2+n) n} \right. \right. \\
 & \left. \left. e^{-i f n x} \left( B e^{2 i (e+f x)} n \operatorname{Hypergeometric2F1} \left[ 1 - \frac{n}{2}, -n, 2 - \frac{n}{2}, e^{2 i (e+f x)} \right] - \right. \right. \right. \\
 & \left. \left. \left. 2 (2A+B) (-2+n) \operatorname{Hypergeometric2F1} \left[ -n, -\frac{n}{2}, 1 - \frac{n}{2}, e^{2 i (e+f x)} \right] \right) \right) \right) \\
 & \sin [e + f x]^{-n} (d \sin [e + f x])^n (1 + \sin [e + f x])
 \end{aligned}$$

#### Problem 4: Unable to integrate problem.

$$\int \frac{(d \sin [e + f x])^n (A + B \sin [e + f x])}{a + a \sin [e + f x]} dx$$

Optimal (type 5, 202 leaves, 4 steps):

$$\begin{aligned}
 & \left( (B - A n + B n) \cos [e + f x] \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1+n}{2}, \frac{3+n}{2}, \sin [e + f x]^2 \right] (d \sin [e + f x])^{1+n} \right) / \\
 & \left( a d f (1+n) \sqrt{\cos [e + f x]^2} \right) + \\
 & \left( (A - B) (1+n) \cos [e + f x] \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{2+n}{2}, \frac{4+n}{2}, \sin [e + f x]^2 \right] \right. \\
 & \left. (d \sin [e + f x])^{2+n} \right) / \left( a d^2 f (2+n) \sqrt{\cos [e + f x]^2} \right) + \frac{(A - B) \cos [e + f x] (d \sin [e + f x])^{1+n}}{d f (a + a \sin [e + f x])}
 \end{aligned}$$

Result (type 8, 35 leaves):

$$\int \frac{(d \sin [e + f x])^n (A + B \sin [e + f x])}{a + a \sin [e + f x]} dx$$

#### Problem 5: Unable to integrate problem.

$$\int \frac{(d \sin [e + f x])^n (A + B \sin [e + f x])}{(a + a \sin [e + f x])^2} dx$$

Optimal (type 5, 279 leaves, 5 steps):

$$\begin{aligned}
 & - \left( \left( n (A - 2 A n + 2 B (1 + n)) \cos [e + f x] \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1+n}{2}, \frac{3+n}{2}, \sin [e + f x]^2 \right] \right. \right. \\
 & \quad \left. \left. (d \sin [e + f x])^{1+n} \right) / \left( 3 a^2 d f (1+n) \sqrt{\cos [e + f x]^2} \right) \right) + \\
 & \left( (1+n) (B + 2 A (1-n) + 2 B n) \cos [e + f x] \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{2+n}{2}, \frac{4+n}{2}, \sin [e + f x]^2 \right] \right. \\
 & \quad \left. (d \sin [e + f x])^{2+n} \right) / \left( 3 a^2 d^2 f (2+n) \sqrt{\cos [e + f x]^2} \right) + \\
 & \frac{(B + 2 A (1-n) + 2 B n) \cos [e + f x] (d \sin [e + f x])^{1+n}}{3 a^2 d f (1 + \sin [e + f x])} + \\
 & \frac{(A - B) \cos [e + f x] (d \sin [e + f x])^{1+n}}{3 d f (a + a \sin [e + f x])^2}
 \end{aligned}$$

Result (type 8, 35 leaves):

$$\int \frac{(d \sin [e + f x])^n (A + B \sin [e + f x])}{(a + a \sin [e + f x])^2} dx$$

**Problem 6: Unable to integrate problem.**

$$\int \frac{(d \sin [e + f x])^n (A + B \sin [e + f x])}{(a + a \sin [e + f x])^3} dx$$

Optimal (type 5, 362 leaves, 6 steps):

$$\begin{aligned}
 & - \left( \left( n (B (3 - n - 4 n^2) + A (2 - 9 n + 4 n^2)) \cos [e + f x] \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1+n}{2}, \right. \right. \right. \\
 & \quad \left. \left. \frac{3+n}{2}, \sin [e + f x]^2 \right] (d \sin [e + f x])^{1+n} \right) / \left( 15 a^3 d f (1+n) \sqrt{\cos [e + f x]^2} \right) \right) + \\
 & \left( (1-n) (1+n) (7 A + 3 B - 4 A n + 4 B n) \cos [e + f x] \operatorname{Hypergeometric2F1} \left[ \right. \right. \\
 & \quad \left. \left. \frac{1}{2}, \frac{2+n}{2}, \frac{4+n}{2}, \sin [e + f x]^2 \right] (d \sin [e + f x])^{2+n} \right) / \\
 & \left( 15 a^3 d^2 f (2+n) \sqrt{\cos [e + f x]^2} \right) + \frac{(A - B) \cos [e + f x] (d \sin [e + f x])^{1+n}}{5 d f (a + a \sin [e + f x])^3} + \\
 & \frac{(A (5 - 2 n) + 2 B n) \cos [e + f x] (d \sin [e + f x])^{1+n}}{15 a d f (a + a \sin [e + f x])^2} + \\
 & \frac{(1-n) (7 A + 3 B - 4 A n + 4 B n) \cos [e + f x] (d \sin [e + f x])^{1+n}}{15 d f (a^3 + a^3 \sin [e + f x])}
 \end{aligned}$$

Result (type 8, 35 leaves):

$$\int \frac{(d \sin [e + f x])^n (A + B \sin [e + f x])}{(a + a \sin [e + f x])^3} dx$$

### Problem 7: Result more than twice size of optimal antiderivative.

$$\int (d \sin[e + f x])^n (a + a \sin[e + f x])^{5/2} (A + B \sin[e + f x]) dx$$

Optimal (type 5, 336 leaves, 6 steps):

$$\begin{aligned}
 & - \left( \left( 2 a^3 (2 B (115 + 203 n + 104 n^2 + 16 n^3) + A (301 + 478 n + 224 n^2 + 32 n^3)) \cos[e + f x] \right. \right. \\
 & \quad \left. \left. \text{Hypergeometric2F1}\left[\frac{1}{2}, -n, \frac{3}{2}, 1 - \sin[e + f x]\right] \sin[e + f x]^{-n} (d \sin[e + f x])^n \right) / \right. \\
 & \quad \left. (f (3 + 2 n) (5 + 2 n) (7 + 2 n) \sqrt{a + a \sin[e + f x]}) \right) - \\
 & \left( 2 a^3 (2 B (35 + 23 n + 4 n^2) + A (77 + 50 n + 8 n^2)) \cos[e + f x] (d \sin[e + f x])^{1+n} / \right. \\
 & \quad \left. (d f (3 + 2 n) (5 + 2 n) (7 + 2 n) \sqrt{a + a \sin[e + f x]}) - \right. \\
 & \left( 2 a^2 (2 B (5 + n) + A (7 + 2 n)) \cos[e + f x] (d \sin[e + f x])^{1+n} \sqrt{a + a \sin[e + f x]} / \right. \\
 & \quad \left. (d f (5 + 2 n) (7 + 2 n)) - \right. \\
 & \quad \left. \frac{2 a B \cos[e + f x] (d \sin[e + f x])^{1+n} (a + a \sin[e + f x])^{3/2}}{d f (7 + 2 n)} \right)
 \end{aligned}$$

Result (type 5, 791 leaves):

$$\begin{aligned}
 & \frac{1}{f \sqrt{\sec\left[\frac{1}{2}(e+fx)\right]^2 \left(\cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right]\right)^5}} \\
 & 2^{1+n} \sec\left[\frac{1}{2}(e+fx)\right] \sin[e+fx]^{-n} (d \sin[e+fx])^n (a(1+\sin[e+fx]))^{5/2} \\
 & \tan\left[\frac{1}{2}(e+fx)\right] \left(\frac{\tan\left[\frac{1}{2}(e+fx)\right]}{1+\tan\left[\frac{1}{2}(e+fx)\right]^2}\right)^n \left(1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^n \\
 & \left(\frac{\text{A Hypergeometric2F1}\left[\frac{1+n}{2}, \frac{9}{2}+n, \frac{3+n}{2}, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]}{1+n} + \frac{1}{2+n}\right) \\
 & (5A+2B) \text{Hypergeometric2F1}\left[1+\frac{n}{2}, \frac{9}{2}+n, 2+\frac{n}{2}, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right] + \\
 & \frac{1}{3+n} 11A \text{Hypergeometric2F1}\left[\frac{3+n}{2}, \frac{9}{2}+n, \frac{5+n}{2}, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 + \\
 & \frac{1}{3+n} 10B \text{Hypergeometric2F1}\left[\frac{3+n}{2}, \frac{9}{2}+n, \frac{5+n}{2}, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 + \frac{1}{4+n} \\
 & 5(3A+4B) \text{Hypergeometric2F1}\left[2+\frac{n}{2}, \frac{9}{2}+n, 3+\frac{n}{2}, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^3 + \\
 & \frac{1}{5+n} 15A \text{Hypergeometric2F1}\left[\frac{9}{2}+n, \frac{5+n}{2}, \frac{7+n}{2}, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^4 + \\
 & \frac{1}{5+n} 20B \text{Hypergeometric2F1}\left[\frac{9}{2}+n, \frac{5+n}{2}, \frac{7+n}{2}, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^4 + \\
 & \frac{1}{6+n} 11A \text{Hypergeometric2F1}\left[3+\frac{n}{2}, \frac{9}{2}+n, 4+\frac{n}{2}, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^5 + \\
 & \frac{1}{6+n} 10B \text{Hypergeometric2F1}\left[3+\frac{n}{2}, \frac{9}{2}+n, 4+\frac{n}{2}, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^5 + \\
 & \frac{1}{7+n} 5A \text{Hypergeometric2F1}\left[\frac{9}{2}+n, \frac{7+n}{2}, \frac{9+n}{2}, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^6 + \\
 & \frac{1}{7+n} 2B \text{Hypergeometric2F1}\left[\frac{9}{2}+n, \frac{7+n}{2}, \frac{9+n}{2}, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^6 + \\
 & \left.\frac{1}{8+n} A \text{Hypergeometric2F1}\left[4+\frac{n}{2}, \frac{9}{2}+n, 5+\frac{n}{2}, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^7\right)
 \end{aligned}$$

**Problem 8: Result more than twice size of optimal antiderivative.**

$$\int (d \sin[e+fx])^n (a+a \sin[e+fx])^{3/2} (A+B \sin[e+fx]) dx$$

Optimal (type 5, 229 leaves, 5 steps):

$$\begin{aligned}
 & - \left( \left( 2 a^2 (2 B (9 + 13 n + 4 n^2) + A (25 + 30 n + 8 n^2)) \cos [e + f x] \right. \right. \\
 & \quad \left. \left. \text{Hypergeometric2F1} \left[ \frac{1}{2}, -n, \frac{3}{2}, 1 - \sin [e + f x] \right] \sin [e + f x]^{-n} (d \sin [e + f x])^n \right) / \right. \\
 & \quad \left. \left( f (3 + 2 n) (5 + 2 n) \sqrt{a + a \sin [e + f x]} \right) \right) - \\
 & \frac{2 a^2 (2 B (3 + n) + A (5 + 2 n)) \cos [e + f x] (d \sin [e + f x])^{1+n}}{d f (3 + 2 n) (5 + 2 n) \sqrt{a + a \sin [e + f x]}} - \\
 & \frac{2 a B \cos [e + f x] (d \sin [e + f x])^{1+n} \sqrt{a + a \sin [e + f x]}}{d f (5 + 2 n)}
 \end{aligned}$$

Result (type 5, 575 leaves):

$$\begin{aligned}
 & \frac{1}{f \sqrt{\sec \left[ \frac{1}{2} (e + f x) \right]^2 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^3}} \\
 & 2^{1+n} \sec \left[ \frac{1}{2} (e + f x) \right] \sin [e + f x]^{-n} (d \sin [e + f x])^n (a (1 + \sin [e + f x]))^{3/2} \\
 & \tan \left[ \frac{1}{2} (e + f x) \right] \left( \frac{\tan \left[ \frac{1}{2} (e + f x) \right]}{1 + \tan \left[ \frac{1}{2} (e + f x) \right]^2} \right)^n \left( 1 + \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right)^n \\
 & \left( \frac{A \text{Hypergeometric2F1} \left[ \frac{1+n}{2}, \frac{7}{2} + n, \frac{3+n}{2}, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right]}{1+n} + \frac{1}{2+n} \right. \\
 & \quad (3 A + 2 B) \text{Hypergeometric2F1} \left[ 1 + \frac{n}{2}, \frac{7}{2} + n, 2 + \frac{n}{2}, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \tan \left[ \frac{1}{2} (e + f x) \right] + \\
 & \quad \frac{1}{3+n} 4 A \text{Hypergeometric2F1} \left[ \frac{3+n}{2}, \frac{7}{2} + n, \frac{5+n}{2}, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \tan \left[ \frac{1}{2} (e + f x) \right]^2 + \\
 & \quad \frac{1}{3+n} 6 B \text{Hypergeometric2F1} \left[ \frac{3+n}{2}, \frac{7}{2} + n, \frac{5+n}{2}, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \tan \left[ \frac{1}{2} (e + f x) \right]^2 + \frac{1}{4+n} \\
 & \quad 2 (2 A + 3 B) \text{Hypergeometric2F1} \left[ 2 + \frac{n}{2}, \frac{7}{2} + n, 3 + \frac{n}{2}, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \tan \left[ \frac{1}{2} (e + f x) \right]^3 + \\
 & \quad \frac{1}{5+n} 3 A \text{Hypergeometric2F1} \left[ \frac{7}{2} + n, \frac{5+n}{2}, \frac{7+n}{2}, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \tan \left[ \frac{1}{2} (e + f x) \right]^4 + \\
 & \quad \frac{1}{5+n} 2 B \text{Hypergeometric2F1} \left[ \frac{7}{2} + n, \frac{5+n}{2}, \frac{7+n}{2}, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \tan \left[ \frac{1}{2} (e + f x) \right]^4 + \\
 & \quad \left. \frac{1}{6+n} A \text{Hypergeometric2F1} \left[ 3 + \frac{n}{2}, \frac{7}{2} + n, 4 + \frac{n}{2}, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \tan \left[ \frac{1}{2} (e + f x) \right]^5 \right)
 \end{aligned}$$

**Problem 9: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (d \sin [e + f x])^n \sqrt{a + a \sin [e + f x]} (A + B \sin [e + f x]) dx$$

Optimal (type 5, 137 leaves, 4 steps):

$$- \left( \left( 2 a (2 B (1+n) + A (3+2 n)) \operatorname{Cos}[e+f x] \right. \right. \\ \left. \left. \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, -n, \frac{3}{2}, 1-\operatorname{Sin}[e+f x]\right] \operatorname{Sin}[e+f x]^{-n} (d \operatorname{Sin}[e+f x])^n \right) / \right. \\ \left. \left. (f (3+2 n) \sqrt{a+a \operatorname{Sin}[e+f x]}) \right) - \frac{2 a B \operatorname{Cos}[e+f x] (d \operatorname{Sin}[e+f x])^{1+n}}{d f (3+2 n) \sqrt{a+a \operatorname{Sin}[e+f x]}} \right)$$

Result (type 5, 409 leaves):

$$- \frac{1}{\operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] + \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right]} \\ (1+i) 2^{-2-n} e^{-\frac{3 i e}{2}+i f n x} (1-e^{2 i(e+f x)})^{-n} (-i e^{-i(e+f x)} (-1+e^{2 i(e+f x)}))^n \\ \left( \frac{1}{f(3+2 n)} 2 B e^{-\frac{1}{2} i f(3+2 n) x} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}(-3-2 n), -n, \frac{1}{4}(1-2 n), e^{2 i(e+f x)}\right] + \right. \\ \left. 2 e^i e^{-\frac{1}{f+2 f n} i(2 A+B)} e^{-\frac{1}{2} i f(1+2 n) x} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}(-1-2 n), -n, \frac{1}{4}(3-2 n), e^{2 i(e+f x)}\right] + \left( e^{\frac{1}{2} i(2 e+f(1-2 n) x)} \right. \right. \\ \left. \left. (- (2 A+B) (-3+2 n) \operatorname{Hypergeometric2F1}\left[\frac{1}{4}(1-2 n), -n, \frac{1}{4}(5-2 n), e^{2 i(e+f x)}\right] + i B e^{i(e+f x)} (-1+2 n) \operatorname{Hypergeometric2F1}\left[\frac{1}{4}(3-2 n), -n, \frac{1}{4}(7-2 n), e^{2 i(e+f x)}\right]) \right) \right) / \\ \left. (f(-3+2 n)(-1+2 n)) \right) \operatorname{Sin}[e+f x]^{-n} (d \operatorname{Sin}[e+f x])^n \sqrt{a(1+\operatorname{Sin}[e+f x])}$$

### Problem 10: Result more than twice size of optimal antiderivative.

$$\int \frac{(d \operatorname{Sin}[e+f x])^n (A+B \operatorname{Sin}[e+f x])}{\sqrt{a+a \operatorname{Sin}[e+f x]}} dx$$

Optimal (type 6, 152 leaves, 9 steps):

$$- \left( \left( (A-B) \operatorname{AppellF1}\left[\frac{1}{2}, -n, 1, \frac{3}{2}, 1-\operatorname{Sin}[e+f x], \frac{1}{2}(1-\operatorname{Sin}[e+f x])\right] \right. \right. \\ \left. \left. \operatorname{Cos}[e+f x] \operatorname{Sin}[e+f x]^{-n} (d \operatorname{Sin}[e+f x])^n \right) / (f \sqrt{a+a \operatorname{Sin}[e+f x]}) \right) - \\ \left( \frac{2 B \operatorname{Cos}[e+f x] \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, -n, \frac{3}{2}, 1-\operatorname{Sin}[e+f x]\right] \operatorname{Sin}[e+f x]^{-n} (d \operatorname{Sin}[e+f x])^n}{f \sqrt{a+a \operatorname{Sin}[e+f x]}} \right)$$

Result (type 6, 818 leaves):



$$\begin{aligned}
 & \frac{1}{f \sqrt{a (1 + \sin[e + f x])}} \operatorname{Sec}[e + f x] \sin[e + f x]^{-n} (d \sin[e + f x])^n (1 + \sin[e + f x])^2 \\
 & \left( B \sin[e + f x]^n \left( \left( 4 a \operatorname{AppellF1}\left[1, \frac{1}{2}, -n, 2, \frac{1}{2} (1 + \sin[e + f x]), 1 + \sin[e + f x]\right] \right) \right) / \right. \\
 & \quad \left( 8 a \operatorname{AppellF1}\left[1, \frac{1}{2}, -n, 2, \frac{1}{2} (1 + \sin[e + f x]), 1 + \sin[e + f x]\right] + \right. \\
 & \quad \quad a \left( -4 n \operatorname{AppellF1}\left[2, \frac{1}{2}, 1 - n, 3, \frac{1}{2} (1 + \sin[e + f x]), 1 + \sin[e + f x]\right] + \right. \\
 & \quad \quad \quad \left. \operatorname{AppellF1}\left[2, \frac{3}{2}, -n, 3, \frac{1}{2} (1 + \sin[e + f x]), 1 + \sin[e + f x]\right] \right) (1 + \sin[e + f x]) \left. \right) + \\
 & \quad \left( (-1 + 2 n) \operatorname{AppellF1}\left[-\frac{1}{2} - n, -\frac{1}{2}, -n, \frac{1}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{1}{1 + \sin[e + f x]} \right] \right. \\
 & \quad \left. (-1 + \sin[e + f x]) \right) / \left( (1 + 2 n) \right. \\
 & \quad \left( 2 \left( n \operatorname{AppellF1}\left[\frac{1}{2} - n, -\frac{1}{2}, 1 - n, \frac{3}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{1}{1 + \sin[e + f x]} \right] + \operatorname{AppellF1}\left[ \right. \right. \\
 & \quad \quad \left. \frac{1}{2} - n, \frac{1}{2}, -n, \frac{3}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{1}{1 + \sin[e + f x]} \right] \right) + (-1 + 2 n) \operatorname{AppellF1}\left[ \right. \\
 & \quad \quad \left. -\frac{1}{2} - n, -\frac{1}{2}, -n, \frac{1}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{1}{1 + \sin[e + f x]} \right] (1 + \sin[e + f x]) \left. \right) \left. \right) \left. \right) + \\
 & A \left( \left( 4 \operatorname{AppellF1}\left[1, \frac{1}{2}, -n, 2, \frac{1}{2} (1 + \sin[e + f x]), 1 + \sin[e + f x]\right] (-\sin[e + f x])^{-n} \right. \right. \\
 & \quad \left. \left. (-\sin[e + f x]^2)^n \right) / \left( 8 \operatorname{AppellF1}\left[1, \frac{1}{2}, -n, 2, \frac{1}{2} (1 + \sin[e + f x]), 1 + \sin[e + f x]\right] - \right. \right. \\
 & \quad \left( 4 n \operatorname{AppellF1}\left[2, \frac{1}{2}, 1 - n, 3, \frac{1}{2} (1 + \sin[e + f x]), 1 + \sin[e + f x]\right] - \right. \\
 & \quad \quad \left. \left. \operatorname{AppellF1}\left[2, \frac{3}{2}, -n, 3, \frac{1}{2} (1 + \sin[e + f x]), 1 + \sin[e + f x]\right] \right) (1 + \sin[e + f x]) \right) - \\
 & \quad \left( (-1 + 2 n) \operatorname{AppellF1}\left[-\frac{1}{2} - n, -\frac{1}{2}, -n, \frac{1}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{1}{1 + \sin[e + f x]} \right] \right. \\
 & \quad \left. (-1 + \sin[e + f x]) \sin[e + f x]^n \right) / \left( (1 + 2 n) \right. \\
 & \quad \left( 2 \left( n \operatorname{AppellF1}\left[\frac{1}{2} - n, -\frac{1}{2}, 1 - n, \frac{3}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{1}{1 + \sin[e + f x]} \right] + \operatorname{AppellF1}\left[ \right. \right. \\
 & \quad \quad \left. \frac{1}{2} - n, \frac{1}{2}, -n, \frac{3}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{1}{1 + \sin[e + f x]} \right] \right) + (-1 + 2 n) \operatorname{AppellF1}\left[ \right. \\
 & \quad \quad \left. -\frac{1}{2} - n, -\frac{1}{2}, -n, \frac{1}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{1}{1 + \sin[e + f x]} \right] (1 + \sin[e + f x]) \left. \right) \left. \right) \left. \right) \left. \right)
 \end{aligned}$$

**Problem 11: Result more than twice size of optimal antiderivative.**

$$\int \frac{(d \sin[e + f x])^n (A + B \sin[e + f x])}{(a + a \sin[e + f x])^{3/2}} dx$$

Optimal (type 6, 226 leaves, 10 steps):

$$\frac{(A - B) \cos[e + f x] (d \sin[e + f x])^{1+n}}{2 d f (a + a \sin[e + f x])^{3/2}} -$$

$$\left( (A - 4 A n + B (3 + 4 n)) \operatorname{AppellF1}\left[\frac{1}{2}, -n, 1, \frac{3}{2}, 1 - \sin[e + f x], \frac{1}{2} (1 - \sin[e + f x])\right] \right.$$

$$\left. \cos[e + f x] \sin[e + f x]^{-n} (d \sin[e + f x])^n \right) / \left( 4 a f \sqrt{a + a \sin[e + f x]} \right) -$$

$$\left( (A - B) (1 + 2 n) \cos[e + f x] \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, -n, \frac{3}{2}, 1 - \sin[e + f x]\right] \right.$$

$$\left. \sin[e + f x]^{-n} (d \sin[e + f x])^n \right) / \left( 2 a f \sqrt{a + a \sin[e + f x]} \right)$$

Result(type 6, 1568 leaves):

$$\left( B \cos[e + f x] \sin[e + f x]^{1+n} (d \sin[e + f x])^n (1 + \sin[e + f x]) \left( \frac{-a + a (1 + \sin[e + f x])}{a} \right)^{-n} \right.$$

$$\left( \left( 4 a \operatorname{AppellF1}\left[1, \frac{1}{2}, -n, 2, \frac{1}{2} (1 + \sin[e + f x]), 1 + \sin[e + f x]\right] (1 + \sin[e + f x]) \right) / \right.$$

$$\left( 8 a \operatorname{AppellF1}\left[1, \frac{1}{2}, -n, 2, \frac{1}{2} (1 + \sin[e + f x]), 1 + \sin[e + f x]\right] + \right.$$

$$a \left( -4 n \operatorname{AppellF1}\left[2, \frac{1}{2}, 1 - n, 3, \frac{1}{2} (1 + \sin[e + f x]), 1 + \sin[e + f x]\right] + \right.$$

$$\left. \operatorname{AppellF1}\left[2, \frac{3}{2}, -n, 3, \frac{1}{2} (1 + \sin[e + f x]), 1 + \sin[e + f x]\right] \right) (1 + \sin[e + f x]) \right) -$$

$$\left( (-1 + 2 n) \operatorname{AppellF1}\left[-\frac{1}{2} - n, -\frac{1}{2}, -n, \frac{1}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{1}{1 + \sin[e + f x]} \right] \right.$$

$$\left. (1 + \sin[e + f x]) (-2 a + a (1 + \sin[e + f x])) \right) / \left( (1 + 2 n) \right.$$

$$\left( 2 a \left( n \operatorname{AppellF1}\left[\frac{1}{2} - n, -\frac{1}{2}, 1 - n, \frac{3}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{1}{1 + \sin[e + f x]} \right] + \operatorname{AppellF1}\left[\frac{1}{2} - n, \frac{1}{2}, -n, \frac{3}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{1}{1 + \sin[e + f x]} \right] \right) + a (-1 + 2 n) \operatorname{AppellF1}\left[-\frac{1}{2} - n, -\frac{1}{2}, -n, \frac{1}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{1}{1 + \sin[e + f x]} \right] (1 + \sin[e + f x]) \right) \right) +$$

$$\left( 2 (-3 + 2 n) \operatorname{AppellF1}\left[\frac{1}{2} - n, -\frac{1}{2}, -n, \frac{3}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{1}{1 + \sin[e + f x]} \right] \right.$$

$$\left. (-2 a + a (1 + \sin[e + f x])) \right) / \left( (-1 + 2 n) \right.$$

$$\left( 2 a \left( n \operatorname{AppellF1}\left[\frac{3}{2} - n, -\frac{1}{2}, 1 - n, \frac{5}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{1}{1 + \sin[e + f x]} \right] + \operatorname{AppellF1}\left[\frac{3}{2} - n, \frac{1}{2}, -n, \frac{5}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{1}{1 + \sin[e + f x]} \right] \right) + a (-3 + 2 n) \operatorname{AppellF1}\left[\frac{1}{2} - n, -\frac{1}{2}, -n, \frac{3}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{1}{1 + \sin[e + f x]} \right] (1 + \sin[e + f x]) \right) \right) \right) /$$

$$\left( 2 f \sqrt{a (1 + \sin[e + f x])} (-a + a (1 + \sin[e + f x])) \right)$$

$$\begin{aligned}
 & \sqrt{\frac{2 a^2 (1 + \sin[e + f x]) - a^2 (1 + \sin[e + f x])^2}{a^2}} \\
 & \sqrt{1 - \frac{(-a + a (1 + \sin[e + f x]))^2}{a^2}} + \\
 & \left( A \cos[e + f x] (d \sin[e + f x])^n \right. \\
 & \quad (1 + \sin[e + f x]) \\
 & \quad \left. \left( \frac{-a + a (1 + \sin[e + f x])}{a} \right)^{-n} \right. \\
 & \quad \left( \left( 4 a^2 \operatorname{AppellF1}\left[1, \frac{1}{2}, -n, 2, \frac{1}{2} (1 + \sin[e + f x])\right], 1 + \sin[e + f x]\right] \right. \\
 & \quad \quad \left. (-\sin[e + f x])^{-n} (1 + \sin[e + f x]) \left( -\frac{(a - a (1 + \sin[e + f x]))^2}{a^2} \right)^n \right) / \\
 & \quad \left( 8 a \operatorname{AppellF1}\left[1, \frac{1}{2}, -n, 2, \frac{1}{2} (1 + \sin[e + f x])\right], 1 + \sin[e + f x]\right) + \\
 & \quad a \left( -4 n \operatorname{AppellF1}\left[2, \frac{1}{2}, 1 - n, 3, \frac{1}{2} (1 + \sin[e + f x])\right], 1 + \sin[e + f x]\right) + \\
 & \quad \quad \operatorname{AppellF1}\left[2, \frac{3}{2}, -n, 3, \frac{1}{2} (1 + \sin[e + f x])\right], 1 + \sin[e + f x]\right) (1 + \sin[e + f x]) - \\
 & \quad \left( a (-1 + 2 n) \operatorname{AppellF1}\left[-\frac{1}{2} - n, -\frac{1}{2}, -n, \frac{1}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{1}{1 + \sin[e + f x]}\right] \right. \\
 & \quad \left. \sin[e + f x]^n (1 + \sin[e + f x]) (-2 a + a (1 + \sin[e + f x])) \right) / \left( (1 + 2 n) \right. \\
 & \quad \left( 2 a \left( n \operatorname{AppellF1}\left[\frac{1}{2} - n, -\frac{1}{2}, 1 - n, \frac{3}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{1}{1 + \sin[e + f x]}\right] + \operatorname{AppellF1}\left[ \right. \right. \\
 & \quad \quad \left. \frac{1}{2} - n, \frac{1}{2}, -n, \frac{3}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{1}{1 + \sin[e + f x]}\right] \right) + a (-1 + 2 n) \operatorname{AppellF1}\left[ \right. \\
 & \quad \quad \left. -\frac{1}{2} - n, -\frac{1}{2}, -n, \frac{1}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{1}{1 + \sin[e + f x]}\right] (1 + \sin[e + f x]) \left. \right) - \\
 & \quad \left( 2 a (-3 + 2 n) \operatorname{AppellF1}\left[\frac{1}{2} - n, -\frac{1}{2}, -n, \frac{3}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{1}{1 + \sin[e + f x]}\right] \right. \\
 & \quad \left. \sin[e + f x]^n (-2 a + a (1 + \sin[e + f x])) \right) / \left( (-1 + 2 n) \right. \\
 & \quad \left( 2 a \left( n \operatorname{AppellF1}\left[\frac{3}{2} - n, -\frac{1}{2}, 1 - n, \frac{5}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{1}{1 + \sin[e + f x]}\right] + \operatorname{AppellF1}\left[ \right. \right. \\
 & \quad \quad \left. \frac{3}{2} - n, \frac{1}{2}, -n, \frac{5}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{1}{1 + \sin[e + f x]}\right] \right) + a (-3 + 2 n) \operatorname{AppellF1}\left[ \right. \\
 & \quad \quad \left. \frac{1}{2} - n, -\frac{1}{2}, -n, \frac{3}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{1}{1 + \sin[e + f x]}\right] (1 + \sin[e + f x]) \left. \right) \left. \right) /
 \end{aligned}$$

$$\left( 2 a^2 f \sqrt{a (1 + \sin[e + f x])} \sqrt{\frac{2 a^2 (1 + \sin[e + f x]) - a^2 (1 + \sin[e + f x])^2}{a^2}} \right) \sqrt{1 - \frac{(-a + a (1 + \sin[e + f x]))^2}{a^2}}$$

**Problem 12: Result more than twice size of optimal antiderivative.**

$$\int (d \sin[e + f x])^n (a + a \sin[e + f x])^m (A + B \sin[e + f x]) dx$$

Optimal (type 6, 221 leaves, 9 steps):

$$\begin{aligned} & -\frac{1}{f} 2^{\frac{3}{2}+m} B \operatorname{AppellF1}\left[\frac{1}{2}, -n, -\frac{1}{2}-m, \frac{3}{2}, 1-\sin[e+f x], \frac{1}{2}(1-\sin[e+f x])\right] \\ & \cos[e+f x] \sin[e+f x]^{-n} (d \sin[e+f x])^n (1+\sin[e+f x])^{-\frac{1}{2}-m} (a+a \sin[e+f x])^m - \\ & \frac{1}{f} 2^{\frac{1}{2}+m} (A-B) \operatorname{AppellF1}\left[\frac{1}{2}, -n, \frac{1}{2}-m, \frac{3}{2}, 1-\sin[e+f x], \frac{1}{2}(1-\sin[e+f x])\right] \\ & \cos[e+f x] \sin[e+f x]^{-n} (d \sin[e+f x])^n (1+\sin[e+f x])^{-\frac{1}{2}-m} (a+a \sin[e+f x])^m \end{aligned}$$

Result (type 6, 5918 leaves):

$$\begin{aligned} & -\left( \left( 6 \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^{-1-2m} \left( \sec\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \right)^{-2-m} \right. \right. \\ & \quad \left. \sin\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right] (d \sin[e+f x])^n (a+a \sin[e+f x])^m \right. \\ & \quad \left. \left( A \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^{2m} \sin[e+f x]^n + B \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^{2m} \sin[e+f x]^{1+n} \right) \right. \\ & \quad \left. \left( \left( (A-B) \operatorname{AppellF1}\left[\frac{1}{2}, -n, 1+m+n, \frac{3}{2}, \tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \right. \right. \\ & \quad \quad \left. \left. \left. -\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \right] \sec\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \right) / \right. \right. \\ & \quad \left. \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -n, 1+m+n, \frac{3}{2}, \tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \right] - \right. \right. \\ & \quad \quad \left. \left. 2 \left( n \operatorname{AppellF1}\left[\frac{3}{2}, 1-n, 1+m+n, \frac{5}{2}, \tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \right. \right. \right. \\ & \quad \quad \quad \left. \left. \left. -\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \right) + (1+m+n) \operatorname{AppellF1}\left[\frac{3}{2}, -n, 2+m+n, \frac{5}{2}, \right. \right. \right. \right. \\ & \quad \quad \quad \left. \left. \left. \tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \right] \right) \tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \right) + \right. \\ & \quad \left. \left. \left( 2 B \operatorname{AppellF1}\left[\frac{1}{2}, -n, 2+m+n, \frac{3}{2}, \tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \right] \right) / \right. \right. \\ & \quad \left. \left. \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -n, 2+m+n, \frac{3}{2}, \tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \right] - \right. \right. \\ & \quad \quad \left. \left. 2 \left( n \operatorname{AppellF1}\left[\frac{3}{2}, 1-n, 2+m+n, \frac{5}{2}, \tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \right. \right. \right. \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + (2+m+n) \operatorname{AppellF1}\left[\frac{3}{2}, -n, 3+m+n, \frac{5}{2}, \right. \\
 & \left. \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \Big/ \\
 & \left(f \left(3 \left(\sec\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{-1-m} \sin[efx]^n \left(\left((A-B) \operatorname{AppellF1}\left[\frac{1}{2}, -n, 1+m+n, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{3}{2}, \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \Big/ \right. \right. \\
 & \left. \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -n, 1+m+n, \frac{3}{2}, \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \right. \right. \\
 & \left. \left. 2 \left(n \operatorname{AppellF1}\left[\frac{3}{2}, 1-n, 1+m+n, \frac{5}{2}, \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (1+m+n) \operatorname{AppellF1}\left[\frac{3}{2}, -n, 2+m+n, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \right. \\
 & \left. \left(2 B \operatorname{AppellF1}\left[\frac{1}{2}, -n, 2+m+n, \frac{3}{2}, \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \Big/ \right. \\
 & \left. \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -n, 2+m+n, \frac{3}{2}, \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \right. \right. \\
 & \left. \left. 2 \left(n \operatorname{AppellF1}\left[\frac{3}{2}, 1-n, 2+m+n, \frac{5}{2}, \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (2+m+n) \operatorname{AppellF1}\left[\frac{3}{2}, -n, 3+m+n, \frac{5}{2}, \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) - \right. \\
 & \left. 6 n \cos[efx] \left(\sec\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{-2-m} \sin[efx]^{-1+n} \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \right. \\
 & \left. \left(\left((A-B) \operatorname{AppellF1}\left[\frac{1}{2}, -n, 1+m+n, \frac{3}{2}, \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \Big/ \right. \\
 & \left. \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -n, 1+m+n, \frac{3}{2}, \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \right. \right. \\
 & \left. \left. 2 \left(n \operatorname{AppellF1}\left[\frac{3}{2}, 1-n, 1+m+n, \frac{5}{2}, \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (1+m+n) \operatorname{AppellF1}\left[\frac{3}{2}, -n, 2+m+n, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \right. \\
 & \left. \left(2 B \operatorname{AppellF1}\left[\frac{1}{2}, -n, 2+m+n, \frac{3}{2}, \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \Big/ \right. \\
 & \left. -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \Big/
 \end{aligned}$$





$$\begin{aligned}
& \text{Sec}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right] + 3\left(-\frac{1}{3} n \text{AppellF1}\left[\frac{3}{2},\right.\right. \\
& \quad \left.1 - n, 1 + m + n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \\
& \text{Sec}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{1}{3}(1 + m + n) \text{AppellF1}\left[\right. \\
& \quad \left.\frac{3}{2}, -n, 2 + m + n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \\
& \text{Sec}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right] - 2 \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \\
& \left(n\left(-\frac{3}{5}(1 + m + n) \text{AppellF1}\left[\frac{5}{2}, 1 - n, 2 + m + n, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2,\right.\right.\right. \\
& \quad \left.-\text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \text{Sec}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\right. \\
& \quad \left.\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right] + \frac{3}{5}(1 - n) \text{AppellF1}\left[\frac{5}{2}, 2 - n, 1 + m + n, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}\right.\right. \\
& \quad \left.\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \text{Sec}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \\
& \left.\text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]\right) + (1 + m + n)\left(-\frac{3}{5} n \text{AppellF1}\left[\frac{5}{2}, 1 - n,\right.\right. \\
& \quad \left.2 + m + n, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \\
& \text{Sec}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{3}{5}(2 + m + n) \text{AppellF1}\left[\right. \\
& \quad \left.\frac{5}{2}, -n, 3 + m + n, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \\
& \left.\left.\text{Sec}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)\right)\right)\right)\Bigg/ \\
& \left(3 \text{AppellF1}\left[\frac{1}{2}, -n, 1 + m + n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2,\right.\right. \\
& \quad \left.-\text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] - 2\left(n \text{AppellF1}\left[\frac{3}{2}, 1 - n, 1 + m + n,\right.\right. \\
& \quad \left.\left.\frac{5}{2}, \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] +\right. \\
& \quad \left.(1 + m + n) \text{AppellF1}\left[\frac{3}{2}, -n, 2 + m + n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2,\right.\right. \\
& \quad \left.\left.-\text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^2 - \\
& \left(2 \text{B AppellF1}\left[\frac{1}{2}, -n, 2 + m + n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right. \\
& \quad \left.- 2\left(n \text{AppellF1}\left[\frac{3}{2}, 1 - n, 2 + m + n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2,\right.\right.\right. \\
& \quad \left.-\text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (2 + m + n) \text{AppellF1}\left[\frac{3}{2}, -n,\right. \\
& \quad \left.3 + m + n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right]\right)
\end{aligned}$$



$$\begin{aligned}
 & \text{Sec}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right] + 3\left(-\frac{1}{3} n \text{AppellF1}\left[\frac{3}{2},\right.\right. \\
 & \quad \left.1 - n, 2 + m + n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \\
 & \text{Sec}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{1}{3}(2 + m + n) \text{AppellF1}\left[\right. \\
 & \quad \left.\frac{3}{2}, -n, 3 + m + n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \\
 & \text{Sec}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right] - 2 \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \\
 & \left(n\left(-\frac{3}{5}(2 + m + n) \text{AppellF1}\left[\frac{5}{2}, 1 - n, 3 + m + n, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2,\right.\right.\right. \\
 & \quad \left.-\text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \text{Sec}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\right. \\
 & \quad \left.\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right] + \frac{3}{5}(1 - n) \text{AppellF1}\left[\frac{5}{2}, 2 - n, 2 + m + n, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}\right. \right. \\
 & \quad \left.\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \text{Sec}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \\
 & \left.\text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]\right) + (2 + m + n)\left(-\frac{3}{5} n \text{AppellF1}\left[\frac{5}{2}, 1 - n,\right.\right. \\
 & \quad \left.3 + m + n, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \\
 & \text{Sec}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{3}{5}(3 + m + n) \text{AppellF1}\left[\right. \\
 & \quad \left.\frac{5}{2}, -n, 4 + m + n, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \\
 & \left.\left.\text{Sec}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)\right)\right)\right) / \\
 & \left(3 \text{AppellF1}\left[\frac{1}{2}, -n, 2 + m + n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2,\right.\right. \\
 & \quad \left.-\text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] - 2\left(n \text{AppellF1}\left[\frac{3}{2}, 1 - n, 2 + m + n,\right.\right. \\
 & \quad \left.\frac{5}{2}, \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \right. \\
 & \quad \left.(2 + m + n) \text{AppellF1}\left[\frac{3}{2}, -n, 3 + m + n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2,\right.\right. \\
 & \quad \left.\left.-\text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right]\right) \text{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)\right)\right)\right)
 \end{aligned}$$

Problem 13: Unable to integrate problem.

$$\int (d \sin[e + f x])^n (a - a \sin[e + f x]) (a + a \sin[e + f x])^m dx$$

Optimal (type 6, 114 leaves, 4 steps):

$$\left( \text{AppellF1}\left[1+n, -\frac{1}{2}, \frac{1}{2}-m, 2+n, \text{Sin}[e+fx], -\text{Sin}[e+fx]\right] \text{Sec}[e+fx] (d \text{Sin}[e+fx])^{1+n} \right. \\ \left. (1+\text{Sin}[e+fx])^{\frac{1}{2}-m} (a-a \text{Sin}[e+fx]) (a+a \text{Sin}[e+fx])^m \right] / \left( df(1+n) \sqrt{1-\text{Sin}[e+fx]} \right)$$

Result (type 8, 36 leaves):

$$\int (d \text{Sin}[e+fx])^n (a-a \text{Sin}[e+fx]) (a+a \text{Sin}[e+fx])^m dx$$

**Problem 14: Result more than twice size of optimal antiderivative.**

$$\int \text{Sin}[c+dx]^n (a+a \text{Sin}[c+dx])^{-2-n} (-1-n - (-2-n) \text{Sin}[c+dx]) dx$$

Optimal (type 3, 37 leaves, 1 step):

$$\frac{\text{Cos}[c+dx] \text{Sin}[c+dx]^{1+n} (a+a \text{Sin}[c+dx])^{-2-n}}{d}$$

Result (type 3, 107 leaves):

$$-\frac{1}{d} 2^n \text{Sin}\left[\frac{1}{2}(c+dx)\right] \left( \text{Cos}\left[\frac{1}{2}(c+dx)\right] + \text{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \\ \left( \text{Cos}\left[\frac{1}{4}(c+dx)\right] \left( -\text{Sin}\left[\frac{1}{4}(c+dx)\right] + \text{Sin}\left[\frac{3}{4}(c+dx)\right] \right) \right)^n \\ (1+\text{Cos}[c+dx] - \text{Sin}[c+dx]) (a(1+\text{Sin}[c+dx]))^{-2-n}$$

**Problem 21: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a+a \text{Sin}[e+fx]) (A+B \text{Sin}[e+fx])}{c-c \text{Sin}[e+fx]} dx$$

Optimal (type 3, 56 leaves, 4 steps):

$$-\frac{a(A+2B)x}{c} + \frac{aB \text{Cos}[e+fx]}{cf} + \frac{2a(A+B) \text{Cos}[e+fx]}{f(c-c \text{Sin}[e+fx])}$$

Result (type 3, 125 leaves):

$$\left( a \left( - (A+2B)x + \frac{B \text{Cos}[e] \text{Cos}[fx]}{f} - \frac{B \text{Sin}[e] \text{Sin}[fx]}{f} + \right. \right. \\ \left. \left. \frac{4(A+B) \text{Sin}\left[\frac{fx}{2}\right]}{f \left( \text{Cos}\left[\frac{e}{2}\right] - \text{Sin}\left[\frac{e}{2}\right] \right) \left( \text{Cos}\left[\frac{1}{2}(e+fx)\right] - \text{Sin}\left[\frac{1}{2}(e+fx)\right] \right)} \right) \right) \\ \left. (1+\text{Sin}[e+fx]) \right) / \left( c \left( \text{Cos}\left[\frac{1}{2}(e+fx)\right] + \text{Sin}\left[\frac{1}{2}(e+fx)\right] \right)^2 \right)$$

**Problem 22: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sin[e + f x]) (A + B \sin[e + f x])}{(c - c \sin[e + f x])^2} dx$$

Optimal (type 3, 72 leaves, 4 steps):

$$\frac{a B x}{c^2} - \frac{a (A + 7 B) \cos[e + f x]}{3 c^2 f (1 - \sin[e + f x])} + \frac{2 a (A + B) \cos[e + f x]}{3 f (c - c \sin[e + f x])^2}$$

Result (type 3, 160 leaves):

$$- \left( \left( a \left( -9 B f x \cos\left[\frac{f x}{2}\right] - 6 (A + 3 B) \cos\left[e + \frac{f x}{2}\right] + 2 A \cos\left[e + \frac{3 f x}{2}\right] + 14 B \cos\left[e + \frac{3 f x}{2}\right] + 3 B f x \cos\left[2 e + \frac{3 f x}{2}\right] + 24 B \sin\left[\frac{f x}{2}\right] + 9 B f x \sin\left[e + \frac{f x}{2}\right] + 3 B f x \sin\left[e + \frac{3 f x}{2}\right] \right) \right) / \left( 6 c^2 f \left( \cos\left[\frac{e}{2}\right] - \sin\left[\frac{e}{2}\right] \right) \left( \cos\left[\frac{1}{2} (e + f x)\right] - \sin\left[\frac{1}{2} (e + f x)\right] \right)^3 \right)$$

**Problem 32: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sin[e + f x])^2 (A + B \sin[e + f x])}{(c - c \sin[e + f x])^2} dx$$

Optimal (type 3, 109 leaves, 5 steps):

$$\frac{a^2 (A + 4 B) x}{c^2} - \frac{a^2 (A + 4 B) \cos[e + f x]}{c^2 f} + \frac{a^2 (A + B) c^2 \cos[e + f x]^5}{3 f (c - c \sin[e + f x])^4} - \frac{2 a^2 (A + 4 B) \cos[e + f x]^3}{3 f (c - c \sin[e + f x])^2}$$

Result (type 3, 238 leaves):

$$\frac{1}{3 f \left( \cos\left[\frac{1}{2} (e + f x)\right] + \sin\left[\frac{1}{2} (e + f x)\right] \right)^4 (c - c \sin[e + f x])^2} + a^2 \left( \cos\left[\frac{1}{2} (e + f x)\right] - \sin\left[\frac{1}{2} (e + f x)\right] \right) \left( 4 (A + B) \left( \cos\left[\frac{1}{2} (e + f x)\right] - \sin\left[\frac{1}{2} (e + f x)\right] \right) + 3 (A + 4 B) (e + f x) \left( \cos\left[\frac{1}{2} (e + f x)\right] - \sin\left[\frac{1}{2} (e + f x)\right] \right)^3 - 3 B \cos[e + f x] \left( \cos\left[\frac{1}{2} (e + f x)\right] - \sin\left[\frac{1}{2} (e + f x)\right] \right)^3 + 8 (A + B) \sin\left[\frac{1}{2} (e + f x)\right] - 8 (2 A + 5 B) \left( \cos\left[\frac{1}{2} (e + f x)\right] - \sin\left[\frac{1}{2} (e + f x)\right] \right)^2 \sin\left[\frac{1}{2} (e + f x)\right] \right) (1 + \sin[e + f x])^2$$

**Problem 33: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sin[e + f x])^2 (A + B \sin[e + f x])}{(c - c \sin[e + f x])^3} dx$$

Optimal (type 3, 112 leaves, 5 steps):

$$-\frac{a^2 B x}{c^3} + \frac{a^2 (A+B) c^2 \cos [e+f x]^5}{5 f (c-c \sin [e+f x])^5} - \frac{2 a^2 B \cos [e+f x]^3}{3 f (c-c \sin [e+f x])^3} + \frac{2 a^2 B \cos [e+f x]}{f (c^3-c^3 \sin [e+f x])}$$

Result (type 3, 278 leaves):

$$\frac{1}{15 f \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right)^4 (c-c \sin [e+f x])^3} a^2 \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right) \left( 12 (A+B) \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right) - 4 (3 A+8 B) \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right)^3 - 15 B (e+f x) \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right)^5 + 24 (A+B) \sin \left[ \frac{1}{2} (e+f x) \right] - 8 (3 A+8 B) \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right)^2 \sin \left[ \frac{1}{2} (e+f x) \right] + 2 (3 A+43 B) \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right)^4 \sin \left[ \frac{1}{2} (e+f x) \right] \right) (1+\sin [e+f x])^2$$

**Problem 34: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a+a \sin [e+f x])^2 (A+B \sin [e+f x])}{(c-c \sin [e+f x])^4} dx$$

Optimal (type 3, 75 leaves, 3 steps):

$$\frac{a^2 (A+B) c^2 \cos [e+f x]^5}{7 f (c-c \sin [e+f x])^6} + \frac{a^2 (A-6 B) c \cos [e+f x]^5}{35 f (c-c \sin [e+f x])^5}$$

Result (type 3, 191 leaves):

$$-\left( \left( a^2 \left( -35 (A+4 B) \cos \left[ \frac{1}{2} (e+f x) \right] + 7 (2 A+13 B) \cos \left[ \frac{3}{2} (e+f x) \right] + 35 B \cos \left[ \frac{5}{2} (e+f x) \right] + A \cos \left[ \frac{7}{2} (e+f x) \right] - 6 B \cos \left[ \frac{7}{2} (e+f x) \right] - 70 A \sin \left[ \frac{1}{2} (e+f x) \right] + 70 B \sin \left[ \frac{1}{2} (e+f x) \right] - 35 A \sin \left[ \frac{3}{2} (e+f x) \right] + 35 B \sin \left[ \frac{3}{2} (e+f x) \right] + 7 A \sin \left[ \frac{5}{2} (e+f x) \right] - 7 B \sin \left[ \frac{5}{2} (e+f x) \right] \right) \right) / \left( 140 c^4 f \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right)^7 \right)$$

**Problem 35: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a+a \sin [e+f x])^2 (A+B \sin [e+f x])}{(c-c \sin [e+f x])^5} dx$$

Optimal (type 3, 115 leaves, 4 steps):

$$\frac{a^2 (A+B) c^2 \cos [e+f x]^5}{9 f (c-c \sin [e+f x])^7} + \frac{a^2 (2 A-7 B) c \cos [e+f x]^5}{63 f (c-c \sin [e+f x])^6} + \frac{a^2 (2 A-7 B) \cos [e+f x]^5}{315 f (c-c \sin [e+f x])^5}$$

Result (type 3, 261 leaves):

$$\frac{1}{2520 c^5 f \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right)^4 (-1 + \sin [e+f x])^5 + a^2 \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right) (1 + \sin [e+f x])^2 \left( 315 (2 A+3 B) \cos \left[ \frac{1}{2} (e+f x) \right] - 63 (4 A+11 B) \cos \left[ \frac{3}{2} (e+f x) \right] - 315 B \cos \left[ \frac{5}{2} (e+f x) \right] - 18 A \cos \left[ \frac{7}{2} (e+f x) \right] + 63 B \cos \left[ \frac{7}{2} (e+f x) \right] + 882 A \sin \left[ \frac{1}{2} (e+f x) \right] + 63 B \sin \left[ \frac{1}{2} (e+f x) \right] + 420 A \sin \left[ \frac{3}{2} (e+f x) \right] + 105 B \sin \left[ \frac{3}{2} (e+f x) \right] - 72 A \sin \left[ \frac{5}{2} (e+f x) \right] - 63 B \sin \left[ \frac{5}{2} (e+f x) \right] + 2 A \sin \left[ \frac{9}{2} (e+f x) \right] - 7 B \sin \left[ \frac{9}{2} (e+f x) \right] \right)}$$

**Problem 38: Result more than twice size of optimal antiderivative.**

$$\int (a + a \sin [e+f x])^3 (A+B \sin [e+f x]) (c-c \sin [e+f x])^6 dx$$

Optimal (type 3, 265 leaves, 9 steps):

$$\frac{11}{256} a^3 (10 A-3 B) c^6 x + \frac{11 a^3 (10 A-3 B) c^6 \cos [e+f x]^7}{560 f} + \frac{11 a^3 (10 A-3 B) c^6 \cos [e+f x] \sin [e+f x]}{256 f} + \frac{11 a^3 (10 A-3 B) c^6 \cos [e+f x]^3 \sin [e+f x]}{384 f} + \frac{11 a^3 (10 A-3 B) c^6 \cos [e+f x]^5 \sin [e+f x]}{480 f} - \frac{a^3 B \cos [e+f x]^7 (c^2 - c^2 \sin [e+f x])^3}{10 f} + \frac{a^3 (10 A-3 B) \cos [e+f x]^7 (c^3 - c^3 \sin [e+f x])^2}{90 f} + \frac{11 a^3 (10 A-3 B) \cos [e+f x]^7 (c^6 - c^6 \sin [e+f x])}{720 f}$$

Result (type 3, 1033 leaves):

$$\begin{aligned}
& \left( 11 (10A - 3B) (e + fx) (a + a \sin[e + fx])^3 (c - c \sin[e + fx])^6 \right) / \\
& \left( 256 f \left( \cos\left[\frac{1}{2}(e + fx)\right] - \sin\left[\frac{1}{2}(e + fx)\right] \right)^{12} \left( \cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right] \right)^6 \right) + \\
& \left( (33A - 19B) \cos[e + fx] (a + a \sin[e + fx])^3 (c - c \sin[e + fx])^6 \right) / \\
& \left( 128 f \left( \cos\left[\frac{1}{2}(e + fx)\right] - \sin\left[\frac{1}{2}(e + fx)\right] \right)^{12} \left( \cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right] \right)^6 \right) + \\
& \left( (29A - 15B) \cos[3(e + fx)] (a + a \sin[e + fx])^3 (c - c \sin[e + fx])^6 \right) / \\
& \left( 192 f \left( \cos\left[\frac{1}{2}(e + fx)\right] - \sin\left[\frac{1}{2}(e + fx)\right] \right)^{12} \left( \cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right] \right)^6 \right) + \\
& \left( (3A - B) \cos[5(e + fx)] (a + a \sin[e + fx])^3 (c - c \sin[e + fx])^6 \right) / \\
& \left( 64 f \left( \cos\left[\frac{1}{2}(e + fx)\right] - \sin\left[\frac{1}{2}(e + fx)\right] \right)^{12} \left( \cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right] \right)^6 \right) + \\
& \left( (9A + 5B) \cos[7(e + fx)] (a + a \sin[e + fx])^3 (c - c \sin[e + fx])^6 \right) / \\
& \left( 1792 f \left( \cos\left[\frac{1}{2}(e + fx)\right] - \sin\left[\frac{1}{2}(e + fx)\right] \right)^{12} \left( \cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right] \right)^6 \right) - \\
& \left( (A - 3B) \cos[9(e + fx)] (a + a \sin[e + fx])^3 (c - c \sin[e + fx])^6 \right) / \\
& \left( 2304 f \left( \cos\left[\frac{1}{2}(e + fx)\right] - \sin\left[\frac{1}{2}(e + fx)\right] \right)^{12} \left( \cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right] \right)^6 \right) + \\
& \left( (144A - 25B) (a + a \sin[e + fx])^3 (c - c \sin[e + fx])^6 \sin[2(e + fx)] \right) / \\
& \left( 512 f \left( \cos\left[\frac{1}{2}(e + fx)\right] - \sin\left[\frac{1}{2}(e + fx)\right] \right)^{12} \left( \cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right] \right)^6 \right) + \\
& \left( (6A + 7B) (a + a \sin[e + fx])^3 (c - c \sin[e + fx])^6 \sin[4(e + fx)] \right) / \\
& \left( 256 f \left( \cos\left[\frac{1}{2}(e + fx)\right] - \sin\left[\frac{1}{2}(e + fx)\right] \right)^{12} \left( \cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right] \right)^6 \right) - \\
& \left( (32A - 51B) (a + a \sin[e + fx])^3 (c - c \sin[e + fx])^6 \sin[6(e + fx)] \right) / \\
& \left( 3072 f \left( \cos\left[\frac{1}{2}(e + fx)\right] - \sin\left[\frac{1}{2}(e + fx)\right] \right)^{12} \left( \cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right] \right)^6 \right) - \\
& \left( (6A - 5B) (a + a \sin[e + fx])^3 (c - c \sin[e + fx])^6 \sin[8(e + fx)] \right) / \\
& \left( 2048 f \left( \cos\left[\frac{1}{2}(e + fx)\right] - \sin\left[\frac{1}{2}(e + fx)\right] \right)^{12} \left( \cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right] \right)^6 \right) - \\
& \left( B (a + a \sin[e + fx])^3 (c - c \sin[e + fx])^6 \sin[10(e + fx)] \right) / \\
& \left( 5120 f \left( \cos\left[\frac{1}{2}(e + fx)\right] - \sin\left[\frac{1}{2}(e + fx)\right] \right)^{12} \left( \cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right] \right)^6 \right)
\end{aligned}$$

**Problem 46: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sin[e + f x])^3 (A + B \sin[e + f x])}{(c - c \sin[e + f x])^3} dx$$

Optimal (type 3, 153 leaves, 6 steps):

$$-\frac{a^3 (A + 6 B) x}{c^3} + \frac{a^3 (A + 6 B) \cos[e + f x]}{c^3 f} + \frac{a^3 (A + B) c^3 \cos[e + f x]^7}{5 f (c - c \sin[e + f x])^6} -$$

$$\frac{2 a^3 (A + 6 B) c \cos[e + f x]^5}{15 f (c - c \sin[e + f x])^4} + \frac{2 a^3 (A + 6 B) c^3 \cos[e + f x]^3}{3 f (c^3 - c^3 \sin[e + f x])^2}$$

Result (type 3, 316 leaves):

$$\frac{1}{15 f \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right)^6 (c - c \sin[e + f x])^3}$$

$$a^3 \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right) \left( 24 (A + B) \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right) \right) -$$

$$4 (11 A + 21 B) \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right)^3 -$$

$$15 (A + 6 B) (e + f x) \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right)^5 +$$

$$15 B \cos[e + f x] \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right)^5 + 48 (A + B) \sin\left[\frac{1}{2}(e + f x)\right] -$$

$$8 (11 A + 21 B) \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right)^2 \sin\left[\frac{1}{2}(e + f x)\right] +$$

$$4 (23 A + 93 B) \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right)^4 \sin\left[\frac{1}{2}(e + f x)\right] \left( 1 + \sin[e + f x] \right)^3$$

**Problem 47: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sin[e + f x])^3 (A + B \sin[e + f x])}{(c - c \sin[e + f x])^4} dx$$

Optimal (type 3, 151 leaves, 6 steps):

$$\frac{a^3 B x}{c^4} + \frac{a^3 (A + B) c^3 \cos[e + f x]^7}{7 f (c - c \sin[e + f x])^7} - \frac{2 a^3 B c \cos[e + f x]^5}{5 f (c - c \sin[e + f x])^5} +$$

$$\frac{2 a^3 B c^2 \cos[e + f x]^3}{3 f (c^2 - c^2 \sin[e + f x])^3} - \frac{2 a^3 B \cos[e + f x]}{f (c^4 - c^4 \sin[e + f x])}$$

Result (type 3, 356 leaves):

$$\frac{1}{105 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 (c - c \sin[e + f x])^4}$$

$$a^3 \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \left( 120 (A + B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) - \right.$$

$$12 (15 A + 29 B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^3 +$$

$$2 (45 A + 199 B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^5 +$$

$$105 B (e + f x) \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^7 + 240 (A + B) \sin \left[ \frac{1}{2} (e + f x) \right] -$$

$$24 (15 A + 29 B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 \sin \left[ \frac{1}{2} (e + f x) \right] +$$

$$4 (45 A + 199 B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^4 \sin \left[ \frac{1}{2} (e + f x) \right] -$$

$$\left. 2 (15 A + 337 B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 \sin \left[ \frac{1}{2} (e + f x) \right] \right) (1 + \sin[e + f x])^3$$

**Problem 48: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sin[e + f x])^3 (A + B \sin[e + f x])}{(c - c \sin[e + f x])^5} dx$$

Optimal (type 3, 77 leaves, 3 steps):

$$\frac{a^3 (A + B) c^3 \cos[e + f x]^7}{9 f (c - c \sin[e + f x])^8} + \frac{a^3 (A - 8 B) c^2 \cos[e + f x]^7}{63 f (c - c \sin[e + f x])^7}$$

Result (type 3, 283 leaves):

$$\frac{1}{504 c^5 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 (-1 + \sin[e + f x])^5}$$

$$a^3 \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) (1 + \sin[e + f x])^3$$

$$\left( 315 (A - B) \cos \left[ \frac{1}{2} (e + f x) \right] - 189 (A - B) \cos \left[ \frac{3}{2} (e + f x) \right] - 63 A \cos \left[ \frac{5}{2} (e + f x) \right] + \right.$$

$$63 B \cos \left[ \frac{5}{2} (e + f x) \right] + 9 A \cos \left[ \frac{7}{2} (e + f x) \right] - 9 B \cos \left[ \frac{7}{2} (e + f x) \right] + 189 A \sin \left[ \frac{1}{2} (e + f x) \right] + 693$$

$$B \sin \left[ \frac{1}{2} (e + f x) \right] + 105 A \sin \left[ \frac{3}{2} (e + f x) \right] + 483 B \sin \left[ \frac{3}{2} (e + f x) \right] - 27 A \sin \left[ \frac{5}{2} (e + f x) \right] -$$

$$\left. 225 B \sin \left[ \frac{5}{2} (e + f x) \right] - 63 B \sin \left[ \frac{7}{2} (e + f x) \right] - A \sin \left[ \frac{9}{2} (e + f x) \right] + 8 B \sin \left[ \frac{9}{2} (e + f x) \right] \right)$$



### Problem 49: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sin[e + f x])^3 (A + B \sin[e + f x])}{(c - c \sin[e + f x])^6} dx$$

Optimal (type 3, 118 leaves, 4 steps):

$$\frac{a^3 (A + B) c^3 \cos[e + f x]^7}{11 f (c - c \sin[e + f x])^9} + \frac{a^3 (2A - 9B) c^2 \cos[e + f x]^7}{99 f (c - c \sin[e + f x])^8} + \frac{a^3 (2A - 9B) c \cos[e + f x]^7}{693 f (c - c \sin[e + f x])^7}$$

Result (type 3, 313 leaves):

$$\frac{1}{11088 c^6 f \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right)^6 (-1 + \sin[e + f x])^6}$$

$$a^3 \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right) (1 + \sin[e + f x])^3$$

$$\left( 462 (11A + 3B) \cos\left[\frac{1}{2}(e + f x)\right] - 594 (5A + 2B) \cos\left[\frac{3}{2}(e + f x)\right] - 924 A \cos\left[\frac{5}{2}(e + f x)\right] - \right.$$

$$693 B \cos\left[\frac{5}{2}(e + f x)\right] + 110 A \cos\left[\frac{7}{2}(e + f x)\right] + 198 B \cos\left[\frac{7}{2}(e + f x)\right] - 2 A \cos\left[\frac{11}{2}(e + f x)\right] +$$

$$9 B \cos\left[\frac{11}{2}(e + f x)\right] + 4158 A \sin\left[\frac{1}{2}(e + f x)\right] + 5544 B \sin\left[\frac{1}{2}(e + f x)\right] +$$

$$2310 A \sin\left[\frac{3}{2}(e + f x)\right] + 4158 B \sin\left[\frac{3}{2}(e + f x)\right] - 594 A \sin\left[\frac{5}{2}(e + f x)\right] -$$

$$\left. 2178 B \sin\left[\frac{5}{2}(e + f x)\right] - 693 B \sin\left[\frac{7}{2}(e + f x)\right] - 22 A \sin\left[\frac{9}{2}(e + f x)\right] + 99 B \sin\left[\frac{9}{2}(e + f x)\right] \right)$$

### Problem 50: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sin[e + f x])^3 (A + B \sin[e + f x])}{(c - c \sin[e + f x])^7} dx$$

Optimal (type 3, 156 leaves, 5 steps):

$$\frac{a^3 (A + B) c^3 \cos[e + f x]^7}{13 f (c - c \sin[e + f x])^{10}} + \frac{a^3 (3A - 10B) c^2 \cos[e + f x]^7}{143 f (c - c \sin[e + f x])^9} +$$

$$\frac{2 a^3 (3A - 10B) c \cos[e + f x]^7}{1287 f (c - c \sin[e + f x])^8} + \frac{2 a^3 (3A - 10B) \cos[e + f x]^7}{9009 f (c - c \sin[e + f x])^7}$$

Result (type 3, 352 leaves):

$$\frac{1}{144144 f \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^6 (c - c \sin[e+fx])^7 \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right) (a + a \sin[e+fx])^3 \left( 54054 A \cos\left[\frac{1}{2}(e+fx)\right] + 30030 B \cos\left[\frac{1}{2}(e+fx)\right] - 30888 A \cos\left[\frac{3}{2}(e+fx)\right] - 23166 B \cos\left[\frac{3}{2}(e+fx)\right] - 9009 A \cos\left[\frac{5}{2}(e+fx)\right] - 12012 B \cos\left[\frac{5}{2}(e+fx)\right] + 858 A \cos\left[\frac{7}{2}(e+fx)\right] + 3146 B \cos\left[\frac{7}{2}(e+fx)\right] - 39 A \cos\left[\frac{11}{2}(e+fx)\right] + 130 B \cos\left[\frac{11}{2}(e+fx)\right] + 48906 A \sin\left[\frac{1}{2}(e+fx)\right] + 47190 B \sin\left[\frac{1}{2}(e+fx)\right] + 27027 A \sin\left[\frac{3}{2}(e+fx)\right] + 36036 B \sin\left[\frac{3}{2}(e+fx)\right] - 6864 A \sin\left[\frac{5}{2}(e+fx)\right] - 19162 B \sin\left[\frac{5}{2}(e+fx)\right] - 6006 B \sin\left[\frac{7}{2}(e+fx)\right] - 234 A \sin\left[\frac{9}{2}(e+fx)\right] + 780 B \sin\left[\frac{9}{2}(e+fx)\right] + 3 A \sin\left[\frac{13}{2}(e+fx)\right] - 10 B \sin\left[\frac{13}{2}(e+fx)\right] \right)}$$

**Problem 55: Result more than twice size of optimal antiderivative.**

$$\int \frac{(A + B \sin[e + fx]) (c - c \sin[e + fx])}{a + a \sin[e + fx]} dx$$

Optimal (type 3, 57 leaves, 4 steps):

$$-\frac{(A - 2B) cx}{a} + \frac{B c \cos[e + fx]}{af} - \frac{2(A - B) c \cos[e + fx]}{f(a + a \sin[e + fx])}$$

Result (type 3, 127 leaves):

$$\left( \left( - (A - 2B) x + \frac{B \cos[e] \cos[fx]}{f} - \frac{B \sin[e] \sin[fx]}{f} + \frac{4(A - B) \sin\left[\frac{fx}{2}\right]}{f \left( \cos\left[\frac{e}{2}\right] + \sin\left[\frac{e}{2}\right] \right) \left( \cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right] \right)} \right) (c - c \sin[e + fx]) \right) / \left( a \left( \cos\left[\frac{1}{2}(e + fx)\right] - \sin\left[\frac{1}{2}(e + fx)\right] \right) \right)^2$$

**Problem 63: Result more than twice size of optimal antiderivative.**

$$\int \frac{(A + B \sin[e + fx]) (c - c \sin[e + fx])^2}{(a + a \sin[e + fx])^2} dx$$

Optimal (type 3, 108 leaves, 5 steps):

$$\frac{(A-4B)c^2x}{a^2} + \frac{(A-4B)c^2 \cos[e+fx]}{a^2 f} - \frac{a^2(A-B)c^2 \cos[e+fx]^5}{3f(a+a \sin[e+fx])^4} + \frac{2(A-4B)c^2 \cos[e+fx]^3}{3f(a+a \sin[e+fx])^2}$$

Result (type 3, 234 leaves):

$$\frac{1}{3a^2 f \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^4 (1 + \sin[e+fx])^2 \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right) \left( 8(A-B) \sin\left[\frac{1}{2}(e+fx)\right] - 4(A-B) \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right) - 8(2A-5B) \sin\left[\frac{1}{2}(e+fx)\right] \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^2 + 3(A-4B)(e+fx) \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^3 - 3B \cos[e+fx] \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^3 (c - c \sin[e+fx])^2}$$

**Problem 64: Result more than twice size of optimal antiderivative.**

$$\int \frac{(A+B \sin[e+fx])(c-c \sin[e+fx])}{(a+a \sin[e+fx])^2} dx$$

Optimal (type 3, 72 leaves, 4 steps):

$$-\frac{Bcx}{a^2} + \frac{(A-7B)c \cos[e+fx]}{3a^2 f (1 + \sin[e+fx])} - \frac{2(A-B)c \cos[e+fx]}{3f(a+a \sin[e+fx])^2}$$

Result (type 3, 156 leaves):

$$\left( c \left( -9Bfx \cos\left[\frac{fx}{2}\right] - 6(A-3B) \cos\left[e + \frac{fx}{2}\right] + 2A \cos\left[e + \frac{3fx}{2}\right] - 14B \cos\left[e + \frac{3fx}{2}\right] + 3Bfx \cos\left[2e + \frac{3fx}{2}\right] + 24B \sin\left[\frac{fx}{2}\right] - 9Bfx \sin\left[e + \frac{fx}{2}\right] - 3Bfx \sin\left[e + \frac{3fx}{2}\right] \right) \right) / \left( 6a^2 f \left( \cos\left[\frac{e}{2}\right] + \sin\left[\frac{e}{2}\right] \right) \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^3 \right)$$

**Problem 67: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+B \sin[e+fx]}{(a+a \sin[e+fx])^2 (c-c \sin[e+fx])^3} dx$$

Optimal (type 3, 93 leaves, 4 steps):

$$\frac{(A+B) \sec[e+fx]^3}{5a^2 f (c^3 - c^3 \sin[e+fx])} + \frac{(4A-B) \tan[e+fx]}{5a^2 c^3 f} + \frac{(4A-B) \tan[e+fx]^3}{15a^2 c^3 f}$$

Result (type 3, 237 leaves):

$$\frac{1}{960 a^2 c^3 f (-1 + \sin[e + f x])^3 (1 + \sin[e + f x])^2} \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right) \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right) \left( -240 B + 54 (A + B) \cos[e + f x] - 32 (4 A - B) \cos[2(e + f x)] + 18 A \cos[3(e + f x)] + 18 B \cos[3(e + f x)] - 64 A \cos[4(e + f x)] + 16 B \cos[4(e + f x)] - 384 A \sin[e + f x] + 96 B \sin[e + f x] - 18 A \sin[2(e + f x)] - 18 B \sin[2(e + f x)] - 128 A \sin[3(e + f x)] + 32 B \sin[3(e + f x)] - 9 A \sin[4(e + f x)] - 9 B \sin[4(e + f x)] \right)$$

**Problem 68: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sin[e + f x]}{(a + a \sin[e + f x])^2 (c - c \sin[e + f x])^4} dx$$

Optimal (type 3, 135 leaves, 5 steps):

$$\frac{(A + B) \operatorname{Sec}[e + f x]^3}{7 a^2 f (c^2 - c^2 \sin[e + f x])^2} + \frac{(5 A - 2 B) \operatorname{Sec}[e + f x]^3}{35 a^2 f (c^4 - c^4 \sin[e + f x])} + \frac{4 (5 A - 2 B) \operatorname{Tan}[e + f x]}{35 a^2 c^4 f} + \frac{4 (5 A - 2 B) \operatorname{Tan}[e + f x]^3}{105 a^2 c^4 f}$$

Result (type 3, 285 leaves):

$$\frac{1}{13440 a^2 c^4 f (-1 + \sin[e + f x])^4 (1 + \sin[e + f x])^2} \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right) \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right) \left( -2688 B + 42 (25 A + 4 B) \cos[e + f x] - 512 (5 A - 2 B) \cos[2(e + f x)] + 225 A \cos[3(e + f x)] + 36 B \cos[3(e + f x)] - 1280 A \cos[4(e + f x)] + 512 B \cos[4(e + f x)] - 75 A \cos[5(e + f x)] - 12 B \cos[5(e + f x)] - 4480 A \sin[e + f x] + 1792 B \sin[e + f x] - 600 A \sin[2(e + f x)] - 96 B \sin[2(e + f x)] - 960 A \sin[3(e + f x)] + 384 B \sin[3(e + f x)] - 300 A \sin[4(e + f x)] - 48 B \sin[4(e + f x)] + 320 A \sin[5(e + f x)] - 128 B \sin[5(e + f x)] \right)$$

**Problem 72: Result more than twice size of optimal antiderivative.**

$$\int \frac{(A + B \sin[e + f x]) (c - c \sin[e + f x])^3}{(a + a \sin[e + f x])^3} dx$$

Optimal (type 3, 153 leaves, 6 steps):

$$-\frac{(A - 6 B) c^3 x}{a^3} - \frac{(A - 6 B) c^3 \cos[e + f x]}{a^3 f} - \frac{a^3 (A - B) c^3 \cos[e + f x]^7}{5 f (a + a \sin[e + f x])^6} + \frac{2 a (A - 6 B) c^3 \cos[e + f x]^5}{15 f (a + a \sin[e + f x])^4} - \frac{2 a^3 (A - 6 B) c^3 \cos[e + f x]^3}{3 f (a^3 + a^3 \sin[e + f x])^2}$$

Result (type 3, 308 leaves):

$$\begin{aligned}
 & \frac{1}{15 a^3 f \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right)^6 \left( 1 + \sin [e+f x] \right)^3} \\
 & \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right) \\
 & \left( 48 (A-B) \sin \left[ \frac{1}{2} (e+f x) \right] - 24 (A-B) \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right) \right) - \\
 & 8 (11 A - 21 B) \sin \left[ \frac{1}{2} (e+f x) \right] \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right)^2 + \\
 & 4 (11 A - 21 B) \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right)^3 + \\
 & 4 (23 A - 93 B) \sin \left[ \frac{1}{2} (e+f x) \right] \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right)^4 - \\
 & 15 (A - 6 B) (e+f x) \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right)^5 + \\
 & 15 B \cos [e+f x] \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right)^5 \left( c - c \sin [e+f x] \right)^3
 \end{aligned}$$

**Problem 73: Result more than twice size of optimal antiderivative.**

$$\int \frac{(A+B \sin [e+f x]) (c-c \sin [e+f x])^2}{(a+a \sin [e+f x])^3} dx$$

Optimal (type 3, 110 leaves, 5 steps):

$$\frac{B c^2 x}{a^3} - \frac{a^2 (A-B) c^2 \cos [e+f x]^5}{5 f (a+a \sin [e+f x])^5} - \frac{2 B c^2 \cos [e+f x]^3}{3 f (a+a \sin [e+f x])^3} + \frac{2 B c^2 \cos [e+f x]}{f (a^3+a^3 \sin [e+f x])}$$

Result (type 3, 272 leaves):

$$\begin{aligned}
 & \frac{1}{15 a^3 f \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right)^4 \left( 1 + \sin [e+f x] \right)^3} \\
 & \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right) \\
 & \left( 24 (A-B) \sin \left[ \frac{1}{2} (e+f x) \right] - 12 (A-B) \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right) \right) - \\
 & 8 (3 A - 8 B) \sin \left[ \frac{1}{2} (e+f x) \right] \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right)^2 + \\
 & 4 (3 A - 8 B) \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right)^3 + \\
 & 2 (3 A - 43 B) \sin \left[ \frac{1}{2} (e+f x) \right] \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right)^4 + \\
 & 15 B (e+f x) \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right)^5 \left( c - c \sin [e+f x] \right)^2
 \end{aligned}$$

### Problem 76: Result more than twice size of optimal antiderivative.

$$\int \frac{A + B \sin[e + f x]}{(a + a \sin[e + f x])^3 (c - c \sin[e + f x])^2} dx$$

Optimal (type 3, 90 leaves, 4 steps):

$$-\frac{(A - B) \operatorname{Sec}[e + f x]^3}{5 c^2 f (a^3 + a^3 \sin[e + f x])} + \frac{(4 A + B) \operatorname{Tan}[e + f x]}{5 a^3 c^2 f} + \frac{(4 A + B) \operatorname{Tan}[e + f x]^3}{15 a^3 c^2 f}$$

Result (type 3, 237 leaves):

$$\frac{1}{960 a^3 c^2 f (-1 + \sin[e + f x])^2 (1 + \sin[e + f x])^3} \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right) \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right) \\ (240 B + 54 (A - B) \cos[e + f x] - 32 (4 A + B) \cos[2(e + f x)] + 18 A \cos[3(e + f x)] - 18 B \cos[3(e + f x)] - 64 A \cos[4(e + f x)] - 16 B \cos[4(e + f x)] + 384 A \sin[e + f x] + 96 B \sin[e + f x] + 18 A \sin[2(e + f x)] - 18 B \sin[2(e + f x)] + 128 A \sin[3(e + f x)] + 32 B \sin[3(e + f x)] + 9 A \sin[4(e + f x)] - 9 B \sin[4(e + f x)])$$

### Problem 78: Result more than twice size of optimal antiderivative.

$$\int \frac{A + B \sin[e + f x]}{(a + a \sin[e + f x])^3 (c - c \sin[e + f x])^4} dx$$

Optimal (type 3, 121 leaves, 4 steps):

$$\frac{(A + B) \operatorname{Sec}[e + f x]^5}{7 a^3 f (c^4 - c^4 \sin[e + f x])} + \frac{(6 A - B) \operatorname{Tan}[e + f x]}{7 a^3 c^4 f} + \frac{2 (6 A - B) \operatorname{Tan}[e + f x]^3}{21 a^3 c^4 f} + \frac{(6 A - B) \operatorname{Tan}[e + f x]^5}{35 a^3 c^4 f}$$

Result (type 3, 325 leaves):

$$\frac{1}{53760 a^3 c^4 f (-1 + \sin[e + f x])^4 (1 + \sin[e + f x])^3} \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right) \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right) \\ (-8960 B + 1500 (A + B) \cos[e + f x] - 640 (6 A - B) \cos[2(e + f x)] + 750 A \cos[3(e + f x)] + 750 B \cos[3(e + f x)] - 3072 A \cos[4(e + f x)] + 512 B \cos[4(e + f x)] + 150 A \cos[5(e + f x)] + 150 B \cos[5(e + f x)] - 768 A \cos[6(e + f x)] + 128 B \cos[6(e + f x)] - 15360 A \sin[e + f x] + 2560 B \sin[e + f x] - 375 A \sin[2(e + f x)] - 375 B \sin[2(e + f x)] - 7680 A \sin[3(e + f x)] + 1280 B \sin[3(e + f x)] - 300 A \sin[4(e + f x)] - 300 B \sin[4(e + f x)] - 1536 A \sin[5(e + f x)] + 256 B \sin[5(e + f x)] - 75 A \sin[6(e + f x)] - 75 B \sin[6(e + f x)])$$

### Problem 79: Result more than twice size of optimal antiderivative.

$$\int \frac{A + B \sin[e + f x]}{(a + a \sin[e + f x])^3 (c - c \sin[e + f x])^5} dx$$

Optimal (type 3, 162 leaves, 5 steps):

$$\frac{(A + B) \operatorname{Sec}[e + f x]^5}{9 a^3 c^3 f (c - c \sin[e + f x])^2} + \frac{(7 A - 2 B) \operatorname{Sec}[e + f x]^5}{63 a^3 f (c^5 - c^5 \sin[e + f x])} +$$

$$\frac{2 (7 A - 2 B) \operatorname{Tan}[e + f x]}{21 a^3 c^5 f} + \frac{4 (7 A - 2 B) \operatorname{Tan}[e + f x]^3}{63 a^3 c^5 f} + \frac{2 (7 A - 2 B) \operatorname{Tan}[e + f x]^5}{105 a^3 c^5 f}$$

Result (type 3, 373 leaves):

$$\frac{1}{1290240 a^3 c^5 f (-1 + \sin[e + f x])^5 (1 + \sin[e + f x])^3}$$

$$\left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right) \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right)$$

$$(-184320 B + 1125 (49 A + 13 B) \cos[e + f x] - 20480 (7 A - 2 B) \cos[2(e + f x)] +$$

$$23275 A \cos[3(e + f x)] + 6175 B \cos[3(e + f x)] - 114688 A \cos[4(e + f x)] +$$

$$32768 B \cos[4(e + f x)] + 1225 A \cos[5(e + f x)] + 325 B \cos[5(e + f x)] -$$

$$28672 A \cos[6(e + f x)] + 8192 B \cos[6(e + f x)] - 1225 A \cos[7(e + f x)] -$$

$$325 B \cos[7(e + f x)] - 322560 A \sin[e + f x] + 92160 B \sin[e + f x] -$$

$$24500 A \sin[2(e + f x)] - 6500 B \sin[2(e + f x)] - 136192 A \sin[3(e + f x)] +$$

$$38912 B \sin[3(e + f x)] - 19600 A \sin[4(e + f x)] - 5200 B \sin[4(e + f x)] -$$

$$7168 A \sin[5(e + f x)] + 2048 B \sin[5(e + f x)] - 4900 A \sin[6(e + f x)] -$$

$$1300 B \sin[6(e + f x)] + 7168 A \sin[7(e + f x)] - 2048 B \sin[7(e + f x)])$$

### Problem 85: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{(a + a \sin[e + f x]) (A + B \sin[e + f x])}{\sqrt{c - c \sin[e + f x]}} dx$$

Optimal (type 3, 122 leaves, 5 steps):

$$\frac{2 \sqrt{2} a (A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{c} \cos[e + f x]}{\sqrt{2} \sqrt{c - c \sin[e + f x]}}\right]}{\sqrt{c} f} -$$

$$\frac{2 a (3 A + 5 B) \cos[e + f x]}{3 f \sqrt{c - c \sin[e + f x]}} + \frac{2 a B \cos[e + f x] \sqrt{c - c \sin[e + f x]}}{3 c f}$$

Result (type 3, 200 leaves):

$$\begin{aligned}
 & - \left( \left( a \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right. \right. \\
 & \quad \left( 3 (2 A + 3 B) \sqrt{c} - B \sqrt{c} \cos [2 (e + f x)] + 2 (3 A + 5 B) \sqrt{c} \sin [e + f x] - \right. \\
 & \quad \left. \left. 6 i \sqrt{2} (A + B) \operatorname{Log} \left[ \frac{2 \left( -i \sqrt{2} \sqrt{c} + \sqrt{-c (1 + \sin [e + f x])} \right)}{\sqrt{c - c \sin [e + f x]}} \right] \sqrt{-c (1 + \sin [e + f x])} \right) \right) / \\
 & \quad \left( 3 \sqrt{c} f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) \sqrt{c - c \sin [e + f x]} \right) \Bigg)
 \end{aligned}$$

**Problem 86: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(a + a \sin [e + f x]) (A + B \sin [e + f x])}{(c - c \sin [e + f x])^{3/2}} dx$$

Optimal (type 3, 115 leaves, 5 steps):

$$- \frac{a (A + 5 B) \operatorname{ArcTanh} \left[ \frac{\sqrt{c} \cos [e + f x]}{\sqrt{2} \sqrt{c - c \sin [e + f x]}} \right]}{\sqrt{2} c^{3/2} f} + \frac{a (A + B) \cos [e + f x]}{f (c - c \sin [e + f x])^{3/2}} + \frac{2 a B \cos [e + f x]}{c f \sqrt{c - c \sin [e + f x]}}$$

Result (type 3, 218 leaves):

$$\begin{aligned}
 & \left( a (-1 + \sin [e + f x]) (1 + \sin [e + f x]) \right. \\
 & \quad \left( i \sqrt{2} (A + 5 B) \operatorname{Log} \left[ \frac{2 \left( -i \sqrt{2} \sqrt{c} + \sqrt{-c (1 + \sin [e + f x])} \right)}{\sqrt{c - c \sin [e + f x]}} \right] \operatorname{Sec} [e + f x] \right. \\
 & \quad \left. \sqrt{-c (1 + \sin [e + f x])} - \left( 2 \sqrt{c} \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right) \right. \\
 & \quad \left. \left. (A + 3 B - 2 B \sin [e + f x]) \right) \right) / \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^3 \Bigg) / \\
 & \quad \left( 2 c^{3/2} f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 \sqrt{c - c \sin [e + f x]} \right)
 \end{aligned}$$



**Problem 87: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(a + a \sin[e + f x]) (A + B \sin[e + f x])}{(c - c \sin[e + f x])^{5/2}} dx$$

Optimal (type 3, 126 leaves, 5 steps):

$$-\frac{a (A - 7 B) \operatorname{ArcTanh}\left[\frac{\sqrt{c} \cos[e + f x]}{\sqrt{2} \sqrt{c - c \sin[e + f x]}}\right]}{8 \sqrt{2} c^{5/2} f} + \frac{a (A + B) \cos[e + f x]}{2 f (c - c \sin[e + f x])^{5/2}} - \frac{a (A + 9 B) \cos[e + f x]}{8 c f (c - c \sin[e + f x])^{3/2}}$$

Result (type 3, 223 leaves):

$$\left( a (-1 + \sin[e + f x]) (1 + \sin[e + f x]) \right. \\ \left. \left( i \sqrt{2} (A - 7 B) \operatorname{Log}\left[\frac{2 \left(-i \sqrt{2} \sqrt{c} + \sqrt{-c (1 + \sin[e + f x])}\right)}{\sqrt{c - c \sin[e + f x]}}\right] \operatorname{Sec}[e + f x] \right. \right. \\ \left. \left. \sqrt{-c (1 + \sin[e + f x])} - \left(2 \sqrt{c} \left(\cos\left[\frac{1}{2} (e + f x)\right] + \sin\left[\frac{1}{2} (e + f x)\right]\right)\right) \right. \right. \\ \left. \left. (3 A - 5 B + (A + 9 B) \sin[e + f x]) \right) \right) / \left( \cos\left[\frac{1}{2} (e + f x)\right] - \sin\left[\frac{1}{2} (e + f x)\right] \right)^5 \Bigg) / \\ \left( 16 c^{5/2} f \left(\cos\left[\frac{1}{2} (e + f x)\right] + \sin\left[\frac{1}{2} (e + f x)\right]\right)^2 \sqrt{c - c \sin[e + f x]} \right)$$

**Problem 88: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sin[e + f x]) (A + B \sin[e + f x])}{(c - c \sin[e + f x])^{7/2}} dx$$

Optimal (type 3, 163 leaves, 6 steps):

$$-\frac{a (A - 3 B) \operatorname{ArcTanh}\left[\frac{\sqrt{c} \cos[e + f x]}{\sqrt{2} \sqrt{c - c \sin[e + f x]}}\right]}{32 \sqrt{2} c^{7/2} f} + \frac{a (A + B) \cos[e + f x]}{3 f (c - c \sin[e + f x])^{7/2}} - \\ \frac{a (A + 13 B) \cos[e + f x]}{24 c f (c - c \sin[e + f x])^{5/2}} - \frac{a (A - 3 B) \cos[e + f x]}{32 c^2 f (c - c \sin[e + f x])^{3/2}}$$

Result (type 3, 796 leaves):

$$\begin{aligned}
 & a \left( \left( i (A - 3B) \cos[e + fx] \operatorname{Log} \left[ \frac{2 \left( -i \sqrt{2} \sqrt{c} + \sqrt{-2c - c(-1 + \sin[e + fx])} \right)}{\sqrt{-c(-1 + \sin[e + fx])}} \right] \right) \right. \\
 & \quad \left. \sqrt{-2c - c(-1 + \sin[e + fx])} (-1 + \sin[e + fx]) (1 + \sin[e + fx]) \right) / \\
 & \left( 32 \sqrt{2} c^{7/2} f \left( \cos \left[ \frac{e}{2} + \frac{fx}{2} \right] + \sin \left[ \frac{e}{2} + \frac{fx}{2} \right] \right)^2 \sqrt{1 - \frac{(c + c(-1 + \sin[e + fx]))^2}{c^2}} \right. \\
 & \quad \left. \sqrt{\frac{-2c^2(-1 + \sin[e + fx]) - c^2(-1 + \sin[e + fx])^2}{c^2}} \sqrt{-c(-1 + \sin[e + fx])} \right) + \\
 & \frac{1}{\left( \cos \left[ \frac{e}{2} + \frac{fx}{2} \right] + \sin \left[ \frac{e}{2} + \frac{fx}{2} \right] \right)^2} \left( \frac{2 \left( A \sin \left[ \frac{fx}{2} \right] + B \sin \left[ \frac{fx}{2} \right] \right)}{3 c^4 f \left( \cos \left[ \frac{e}{2} \right] - \sin \left[ \frac{e}{2} \right] \right) \left( \cos \left[ \frac{e}{2} + \frac{fx}{2} \right] - \sin \left[ \frac{e}{2} + \frac{fx}{2} \right] \right)^7} + \right. \\
 & \quad \frac{A \cos \left[ \frac{e}{2} \right] + B \cos \left[ \frac{e}{2} \right] + A \sin \left[ \frac{e}{2} \right] + B \sin \left[ \frac{e}{2} \right]}{3 c^4 f \left( \cos \left[ \frac{e}{2} \right] - \sin \left[ \frac{e}{2} \right] \right) \left( \cos \left[ \frac{e}{2} + \frac{fx}{2} \right] - \sin \left[ \frac{e}{2} + \frac{fx}{2} \right] \right)^6} + \\
 & \quad \frac{-A \sin \left[ \frac{fx}{2} \right] - 13 B \sin \left[ \frac{fx}{2} \right]}{12 c^4 f \left( \cos \left[ \frac{e}{2} \right] - \sin \left[ \frac{e}{2} \right] \right) \left( \cos \left[ \frac{e}{2} + \frac{fx}{2} \right] - \sin \left[ \frac{e}{2} + \frac{fx}{2} \right] \right)^5} + \\
 & \quad \frac{-A \cos \left[ \frac{e}{2} \right] - 13 B \cos \left[ \frac{e}{2} \right] - A \sin \left[ \frac{e}{2} \right] - 13 B \sin \left[ \frac{e}{2} \right]}{24 c^4 f \left( \cos \left[ \frac{e}{2} \right] - \sin \left[ \frac{e}{2} \right] \right) \left( \cos \left[ \frac{e}{2} + \frac{fx}{2} \right] - \sin \left[ \frac{e}{2} + \frac{fx}{2} \right] \right)^4} + \\
 & \quad \frac{-A \sin \left[ \frac{fx}{2} \right] + 3 B \sin \left[ \frac{fx}{2} \right]}{16 c^4 f \left( \cos \left[ \frac{e}{2} \right] - \sin \left[ \frac{e}{2} \right] \right) \left( \cos \left[ \frac{e}{2} + \frac{fx}{2} \right] - \sin \left[ \frac{e}{2} + \frac{fx}{2} \right] \right)^3} + \\
 & \quad \left. \frac{-A \cos \left[ \frac{e}{2} \right] + 3 B \cos \left[ \frac{e}{2} \right] - A \sin \left[ \frac{e}{2} \right] + 3 B \sin \left[ \frac{e}{2} \right]}{32 c^4 f \left( \cos \left[ \frac{e}{2} \right] - \sin \left[ \frac{e}{2} \right] \right) \left( \cos \left[ \frac{e}{2} + \frac{fx}{2} \right] - \sin \left[ \frac{e}{2} + \frac{fx}{2} \right] \right)^2} \right) \\
 & \left. (1 + \sin[e + fx]) \sqrt{c - c \sin[e + fx]} \right)
 \end{aligned}$$

**Problem 89: Result more than twice size of optimal antiderivative.**

$$\int (a + a \sin[e + fx])^2 (A + B \sin[e + fx]) (c - c \sin[e + fx])^{7/2} dx$$

Optimal (type 3, 210 leaves, 6 steps):

$$\frac{256 a^2 (13 A - 3 B) c^6 \operatorname{Cos}[e + f x]^5}{15015 f (c - c \operatorname{Sin}[e + f x])^{5/2}} + \frac{64 a^2 (13 A - 3 B) c^5 \operatorname{Cos}[e + f x]^5}{3003 f (c - c \operatorname{Sin}[e + f x])^{3/2}} +$$

$$\frac{8 a^2 (13 A - 3 B) c^4 \operatorname{Cos}[e + f x]^5}{429 f \sqrt{c - c \operatorname{Sin}[e + f x]}} + \frac{2 a^2 (13 A - 3 B) c^3 \operatorname{Cos}[e + f x]^5 \sqrt{c - c \operatorname{Sin}[e + f x]}}{143 f} -$$

$$\frac{2 a^2 B c^2 \operatorname{Cos}[e + f x]^5 (c - c \operatorname{Sin}[e + f x])^{3/2}}{13 f}$$

Result (type 3, 1355 leaves):

$$\left( (7 A - 2 B) \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] (a + a \operatorname{Sin}[e + f x])^2 (c - c \operatorname{Sin}[e + f x])^{7/2} \right) /$$

$$\left( 8 f \left( \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] - \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] \right)^7 \left( \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] + \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] \right)^4 \right) -$$

$$\left( (4 A + B) \operatorname{Cos}\left[\frac{3}{2}(e + f x)\right] (a + a \operatorname{Sin}[e + f x])^2 (c - c \operatorname{Sin}[e + f x])^{7/2} \right) /$$

$$\left( 32 f \left( \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] - \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] \right)^7 \left( \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] + \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] \right)^4 \right) +$$

$$\left( (22 A - 7 B) \operatorname{Cos}\left[\frac{5}{2}(e + f x)\right] (a + a \operatorname{Sin}[e + f x])^2 (c - c \operatorname{Sin}[e + f x])^{7/2} \right) /$$

$$\left( 160 f \left( \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] - \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] \right)^7 \left( \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] + \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] \right)^4 \right) +$$

$$\left( (A - 4 B) \operatorname{Cos}\left[\frac{7}{2}(e + f x)\right] (a + a \operatorname{Sin}[e + f x])^2 (c - c \operatorname{Sin}[e + f x])^{7/2} \right) /$$

$$\left( 112 f \left( \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] - \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] \right)^7 \left( \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] + \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] \right)^4 \right) +$$

$$\left( A \operatorname{Cos}\left[\frac{9}{2}(e + f x)\right] (a + a \operatorname{Sin}[e + f x])^2 (c - c \operatorname{Sin}[e + f x])^{7/2} \right) /$$

$$\left( 48 f \left( \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] - \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] \right)^7 \left( \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] + \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] \right)^4 \right) +$$

$$\left( (2 A - 3 B) \operatorname{Cos}\left[\frac{11}{2}(e + f x)\right] (a + a \operatorname{Sin}[e + f x])^2 (c - c \operatorname{Sin}[e + f x])^{7/2} \right) /$$

$$\left( 352 f \left( \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] - \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] \right)^7 \left( \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] + \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] \right)^4 \right) +$$

$$\left( B \operatorname{Cos}\left[\frac{13}{2}(e + f x)\right] (a + a \operatorname{Sin}[e + f x])^2 (c - c \operatorname{Sin}[e + f x])^{7/2} \right) /$$

$$\left( 416 f \left( \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] - \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] \right)^7 \left( \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] + \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] \right)^4 \right) +$$

$$\left( (7 A - 2 B) \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] (a + a \operatorname{Sin}[e + f x])^2 (c - c \operatorname{Sin}[e + f x])^{7/2} \right) /$$

$$\left( 8 f \left( \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] - \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] \right)^7 \left( \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] + \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] \right)^4 \right) +$$

$$\left( (4 A + B) (a + a \operatorname{Sin}[e + f x])^2 (c - c \operatorname{Sin}[e + f x])^{7/2} \operatorname{Sin}\left[\frac{3}{2}(e + f x)\right] \right) /$$

$$\left( 32 f \left( \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] - \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] \right)^7 \left( \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] + \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] \right)^4 \right) +$$

$$\begin{aligned}
& \left( (22A - 7B) (a + a \sin[e + fx])^2 (c - c \sin[e + fx])^{7/2} \sin\left[\frac{5}{2}(e + fx)\right] \right) / \\
& \left( 160f \left( \cos\left[\frac{1}{2}(e + fx)\right] - \sin\left[\frac{1}{2}(e + fx)\right] \right)^7 \left( \cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right] \right)^4 \right) - \\
& \left( (A - 4B) (a + a \sin[e + fx])^2 (c - c \sin[e + fx])^{7/2} \sin\left[\frac{7}{2}(e + fx)\right] \right) / \\
& \left( 112f \left( \cos\left[\frac{1}{2}(e + fx)\right] - \sin\left[\frac{1}{2}(e + fx)\right] \right)^7 \left( \cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right] \right)^4 \right) + \\
& \left( A (a + a \sin[e + fx])^2 (c - c \sin[e + fx])^{7/2} \sin\left[\frac{9}{2}(e + fx)\right] \right) / \\
& \left( 48f \left( \cos\left[\frac{1}{2}(e + fx)\right] - \sin\left[\frac{1}{2}(e + fx)\right] \right)^7 \left( \cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right] \right)^4 \right) - \\
& \left( (2A - 3B) (a + a \sin[e + fx])^2 (c - c \sin[e + fx])^{7/2} \sin\left[\frac{11}{2}(e + fx)\right] \right) / \\
& \left( 352f \left( \cos\left[\frac{1}{2}(e + fx)\right] - \sin\left[\frac{1}{2}(e + fx)\right] \right)^7 \left( \cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right] \right)^4 \right) + \\
& \left( B (a + a \sin[e + fx])^2 (c - c \sin[e + fx])^{7/2} \sin\left[\frac{13}{2}(e + fx)\right] \right) / \\
& \left( 416f \left( \cos\left[\frac{1}{2}(e + fx)\right] - \sin\left[\frac{1}{2}(e + fx)\right] \right)^7 \left( \cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right] \right)^4 \right)
\end{aligned}$$

### Problem 90: Result more than twice size of optimal antiderivative.

$$\int (a + a \sin[e + fx])^2 (A + B \sin[e + fx]) (c - c \sin[e + fx])^{5/2} dx$$

Optimal (type 3, 167 leaves, 5 steps):

$$\begin{aligned}
& \frac{64 a^2 (11 A - B) c^5 \cos[e + fx]^5}{3465 f (c - c \sin[e + fx])^{5/2}} + \frac{16 a^2 (11 A - B) c^4 \cos[e + fx]^5}{693 f (c - c \sin[e + fx])^{3/2}} + \\
& \frac{2 a^2 (11 A - B) c^3 \cos[e + fx]^5}{99 f \sqrt{c - c \sin[e + fx]}} - \frac{2 a^2 B c^2 \cos[e + fx]^5 \sqrt{c - c \sin[e + fx]}}{11 f}
\end{aligned}$$

Result (type 3, 1173 leaves):

$$\begin{aligned}
& \left( (6A - B) \cos\left[\frac{1}{2}(e + fx)\right] (a + a \sin[e + fx])^2 (c - c \sin[e + fx])^{5/2} \right) / \\
& \left( 8f \left( \cos\left[\frac{1}{2}(e + fx)\right] - \sin\left[\frac{1}{2}(e + fx)\right] \right)^5 \left( \cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right] \right)^4 \right) - \\
& \left( (4A + B) \cos\left[\frac{3}{2}(e + fx)\right] (a + a \sin[e + fx])^2 (c - c \sin[e + fx])^{5/2} \right) / \\
& \left( 24f \left( \cos\left[\frac{1}{2}(e + fx)\right] - \sin\left[\frac{1}{2}(e + fx)\right] \right)^5 \left( \cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right] \right)^4 \right) + \\
& \left( (8A - 3B) \cos\left[\frac{5}{2}(e + fx)\right] (a + a \sin[e + fx])^2 (c - c \sin[e + fx])^{5/2} \right) / \\
& \left( 80f \left( \cos\left[\frac{1}{2}(e + fx)\right] - \sin\left[\frac{1}{2}(e + fx)\right] \right)^5 \left( \cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right] \right)^4 \right) -
\end{aligned}$$

$$\begin{aligned}
 & \left( (2A+3B) \cos\left[\frac{7}{2}(e+fx)\right] (a+a\sin[e+fx])^2 (c-c\sin[e+fx])^{5/2} \right) / \\
 & \left( 112f \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^4 \right) + \\
 & \left( (2A-B) \cos\left[\frac{9}{2}(e+fx)\right] (a+a\sin[e+fx])^2 (c-c\sin[e+fx])^{5/2} \right) / \\
 & \left( 144f \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^4 \right) - \\
 & \left( B \cos\left[\frac{11}{2}(e+fx)\right] (a+a\sin[e+fx])^2 (c-c\sin[e+fx])^{5/2} \right) / \\
 & \left( 176f \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^4 \right) + \\
 & \left( (6A-B) \sin\left[\frac{1}{2}(e+fx)\right] (a+a\sin[e+fx])^2 (c-c\sin[e+fx])^{5/2} \right) / \\
 & \left( 8f \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^4 \right) + \\
 & \left( (4A+B) (a+a\sin[e+fx])^2 (c-c\sin[e+fx])^{5/2} \sin\left[\frac{3}{2}(e+fx)\right] \right) / \\
 & \left( 24f \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^4 \right) + \\
 & \left( (8A-3B) (a+a\sin[e+fx])^2 (c-c\sin[e+fx])^{5/2} \sin\left[\frac{5}{2}(e+fx)\right] \right) / \\
 & \left( 80f \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^4 \right) + \\
 & \left( (2A+3B) (a+a\sin[e+fx])^2 (c-c\sin[e+fx])^{5/2} \sin\left[\frac{7}{2}(e+fx)\right] \right) / \\
 & \left( 112f \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^4 \right) + \\
 & \left( (2A-B) (a+a\sin[e+fx])^2 (c-c\sin[e+fx])^{5/2} \sin\left[\frac{9}{2}(e+fx)\right] \right) / \\
 & \left( 144f \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^4 \right) + \\
 & \left( B (a+a\sin[e+fx])^2 (c-c\sin[e+fx])^{5/2} \sin\left[\frac{11}{2}(e+fx)\right] \right) / \\
 & \left( 176f \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^4 \right)
 \end{aligned}$$

**Problem 91: Result more than twice size of optimal antiderivative.**

$$\int (a+a\sin[e+fx])^2 (A+B\sin[e+fx]) (c-c\sin[e+fx])^{3/2} dx$$

Optimal (type 3, 120 leaves, 4 steps):

$$\frac{8a^2(9A+B)c^4\cos[e+fx]^5}{315f(c-c\sin[e+fx])^{5/2}} + \frac{2a^2(9A+B)c^3\cos[e+fx]^5}{63f(c-c\sin[e+fx])^{3/2}} - \frac{2a^2Bc^2\cos[e+fx]^5}{9f\sqrt{c-c\sin[e+fx]}}$$



**Problem 93: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(a + a \sin[e + f x])^2 (A + B \sin[e + f x])}{\sqrt{c - c \sin[e + f x]}} dx$$

Optimal (type 3, 161 leaves, 6 steps):

$$\frac{4 \sqrt{2} a^2 (A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{c} \cos[e + f x]}{\sqrt{2} \sqrt{c - c \sin[e + f x]}}\right]}{\sqrt{c} f} - \frac{2 a^2 B c^2 \cos[e + f x]^5}{5 f (c - c \sin[e + f x])^{5/2}} - \frac{2 a^2 (A + B) c \cos[e + f x]^3}{3 f (c - c \sin[e + f x])^{3/2}} - \frac{4 a^2 (A + B) \cos[e + f x]}{f \sqrt{c - c \sin[e + f x]}}$$

Result (type 3, 175 leaves):

$$-\left(\left(a^2 \left(\cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right]\right) (1 + \sin[e + f x])^2 \left((120 + 120 i) (-1)^{1/4} (A + B) \operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{1/4} \left(1 + \tan\left[\frac{1}{4}(e + f x)\right]\right)\right] + \left(\cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right]\right) (70 A + 79 B - 3 B \cos[2(e + f x)] + 2(5 A + 11 B) \sin[e + f x])\right)\right) / \left(15 f \left(\cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right]\right)^4 \sqrt{c - c \sin[e + f x]}\right)\right)$$

**Problem 94: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sin[e + f x])^2 (A + B \sin[e + f x])}{(c - c \sin[e + f x])^{3/2}} dx$$

Optimal (type 3, 176 leaves, 6 steps):

$$-\frac{\sqrt{2} a^2 (3 A + 7 B) \operatorname{ArcTanh}\left[\frac{\sqrt{c} \cos[e + f x]}{\sqrt{2} \sqrt{c - c \sin[e + f x]}}\right]}{c^{3/2} f} + \frac{a^2 (A + B) c^2 \cos[e + f x]^5}{2 f (c - c \sin[e + f x])^{7/2}} + \frac{a^2 (3 A + 7 B) \cos[e + f x]^3}{6 f (c - c \sin[e + f x])^{3/2}} + \frac{a^2 (3 A + 7 B) \cos[e + f x]}{c f \sqrt{c - c \sin[e + f x]}}$$

Result (type 3, 355 leaves):

$$\frac{1}{3 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^4 (c - c \sin [e + f x])^{3/2} + a^2 \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) (1 + \sin [e + f x])^2 + \left( 6 (A + B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) + (6 + 6 i) (-1)^{1/4} (3 A + 7 B) \operatorname{ArcTan} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{1/4} \left( 1 + \tan \left[ \frac{1}{4} (e + f x) \right] \right) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 + 3 (2 A + 7 B) \cos \left[ \frac{1}{2} (e + f x) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 - B \cos \left[ \frac{3}{2} (e + f x) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 + 12 (A + B) \sin \left[ \frac{1}{2} (e + f x) \right] + 3 (2 A + 7 B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 \sin \left[ \frac{1}{2} (e + f x) \right] + B \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 \sin \left[ \frac{3}{2} (e + f x) \right]}$$

**Problem 95: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(a + a \sin [e + f x])^2 (A + B \sin [e + f x])}{(c - c \sin [e + f x])^{5/2}} dx$$

Optimal (type 3, 175 leaves, 6 steps):

$$\frac{3 a^2 (A + 9 B) \operatorname{ArcTanh} \left[ \frac{\sqrt{c} \cos [e + f x]}{\sqrt{2} \sqrt{c - c \sin [e + f x]}} \right]}{4 \sqrt{2} c^{5/2} f} + \frac{a^2 (A + B) c^2 \cos [e + f x]^5}{4 f (c - c \sin [e + f x])^{9/2}} - \frac{a^2 (A + 9 B) \cos [e + f x]^3}{8 f (c - c \sin [e + f x])^{5/2}} - \frac{3 a^2 (A + 9 B) \cos [e + f x]}{8 c^2 f \sqrt{c - c \sin [e + f x]}}$$

Result (type 3, 344 leaves):



$$\begin{aligned}
 & \frac{1}{4 f \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right)^4 (c-c \sin [e+f x])^{5/2}} \\
 & a^2 \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right) \left( 4 (A+B) \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right) - \right. \\
 & \quad (5 A+13 B) \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right)^3 - (3+3 i) (-1)^{1/4} (A+9 B) \\
 & \quad \left. \operatorname{ArcTan} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{1/4} \left( 1 + \operatorname{Tan} \left[ \frac{1}{4} (e+f x) \right] \right) \right] \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right)^4 - \right. \\
 & \quad 8 B \cos \left[ \frac{1}{2} (e+f x) \right] \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right)^4 + 8 (A+B) \sin \left[ \frac{1}{2} (e+f x) \right] - \\
 & \quad 2 (5 A+13 B) \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right)^2 \sin \left[ \frac{1}{2} (e+f x) \right] - \\
 & \quad \left. 8 B \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right)^4 \sin \left[ \frac{1}{2} (e+f x) \right] \right) (1+\sin [e+f x])^2
 \end{aligned}$$

**Problem 96: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(a+a \sin [e+f x])^2 (A+B \sin [e+f x])}{(c-c \sin [e+f x])^{7/2}} dx$$

Optimal (type 3, 175 leaves, 6 steps):

$$\begin{aligned}
 & \frac{a^2 (A-11 B) \operatorname{ArcTanh} \left[ \frac{\sqrt{c} \cos [e+f x]}{\sqrt{2} \sqrt{c-c \sin [e+f x]}} \right]}{16 \sqrt{2} c^{7/2} f} + \frac{a^2 (A+B) c^2 \cos [e+f x]^5}{6 f (c-c \sin [e+f x])^{11/2}} + \\
 & \frac{a^2 (A-11 B) \cos [e+f x]^3}{24 f (c-c \sin [e+f x])^{7/2}} - \frac{a^2 (A-11 B) \cos [e+f x]}{16 c^2 f (c-c \sin [e+f x])^{3/2}}
 \end{aligned}$$

Result (type 3, 342 leaves):

$$\begin{aligned}
 & \frac{1}{48 f \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^4 (c - c \sin[e+fx])^{7/2}} \\
 & a^2 \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right) \\
 & \left( 32 (A+B) \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right) - 4 (7A+19B) \right. \\
 & \quad \left. \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^3 + 3 (A+21B) \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 - \right. \\
 & \quad \left. (3+3i) (-1)^{1/4} (A-11B) \operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{1/4} \left(1 + \tan\left[\frac{1}{4}(e+fx)\right]\right)\right] \right) \\
 & \quad \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^6 + 64 (A+B) \sin\left[\frac{1}{2}(e+fx)\right] - \\
 & 8 (7A+19B) \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^2 \sin\left[\frac{1}{2}(e+fx)\right] + \\
 & 6 (A+21B) \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^4 \sin\left[\frac{1}{2}(e+fx)\right] \left(1 + \sin[e+fx]\right)^2
 \end{aligned}$$

**Problem 97: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(a + a \sin[e+fx])^2 (A + B \sin[e+fx])}{(c - c \sin[e+fx])^{9/2}} dx$$

Optimal (type 3, 222 leaves, 7 steps):

$$\begin{aligned}
 & \frac{a^2 (3A - 13B) \operatorname{ArcTanh}\left[\frac{\sqrt{c} \cos[e+fx]}{\sqrt{2} \sqrt{c-c \sin[e+fx]}}\right]}{256 \sqrt{2} c^{9/2} f} + \frac{a^2 (A+B) c^2 \cos[e+fx]^5}{8 f (c - c \sin[e+fx])^{13/2}} + \\
 & \frac{a^2 (3A - 13B) \cos[e+fx]^3}{48 f (c - c \sin[e+fx])^{9/2}} - \frac{a^2 (3A - 13B) \cos[e+fx]}{64 c^2 f (c - c \sin[e+fx])^{5/2}} + \frac{a^2 (3A - 13B) \cos[e+fx]}{256 c^3 f (c - c \sin[e+fx])^{3/2}}
 \end{aligned}$$

Result (type 3, 357 leaves):

1

$$\begin{aligned}
 & 6144 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^4 (c - c \sin[e + f x])^{9/2} \\
 & a^2 \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) (1 + \sin[e + f x])^2 \\
 & \left( 2013 A \cos \left[ \frac{1}{2} (e + f x) \right] + 1517 B \cos \left[ \frac{1}{2} (e + f x) \right] - 999 A \cos \left[ \frac{3}{2} (e + f x) \right] - \right. \\
 & \quad 791 B \cos \left[ \frac{3}{2} (e + f x) \right] - 69 A \cos \left[ \frac{5}{2} (e + f x) \right] - 725 B \cos \left[ \frac{5}{2} (e + f x) \right] - \\
 & \quad 9 A \cos \left[ \frac{7}{2} (e + f x) \right] + 39 B \cos \left[ \frac{7}{2} (e + f x) \right] - (24 + 24 i) (-1)^{1/4} (3 A - 13 B) \\
 & \quad \left. \text{ArcTan} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{1/4} \left( 1 + \tan \left[ \frac{1}{4} (e + f x) \right] \right) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^8 + \\
 & 2013 A \sin \left[ \frac{1}{2} (e + f x) \right] + 1517 B \sin \left[ \frac{1}{2} (e + f x) \right] + 999 A \sin \left[ \frac{3}{2} (e + f x) \right] + \\
 & 791 B \sin \left[ \frac{3}{2} (e + f x) \right] - 69 A \sin \left[ \frac{5}{2} (e + f x) \right] - \\
 & 725 B \sin \left[ \frac{5}{2} (e + f x) \right] + 9 A \sin \left[ \frac{7}{2} (e + f x) \right] - 39 B \sin \left[ \frac{7}{2} (e + f x) \right] \Big)
 \end{aligned}$$

**Problem 98: Result more than twice size of optimal antiderivative.**

$$\int (a + a \sin[e + f x])^3 (A + B \sin[e + f x]) (c - c \sin[e + f x])^{7/2} dx$$

Optimal (type 3, 210 leaves, 6 steps):

$$\begin{aligned}
 & \frac{256 a^3 (15 A - B) c^7 \cos[e + f x]^7}{45045 f (c - c \sin[e + f x])^{7/2}} + \frac{64 a^3 (15 A - B) c^6 \cos[e + f x]^7}{6435 f (c - c \sin[e + f x])^{5/2}} + \frac{8 a^3 (15 A - B) c^5 \cos[e + f x]^7}{715 f (c - c \sin[e + f x])^{3/2}} + \\
 & \frac{2 a^3 (15 A - B) c^4 \cos[e + f x]^7}{195 f \sqrt{c - c \sin[e + f x]}} - \frac{2 a^3 B c^3 \cos[e + f x]^7 \sqrt{c - c \sin[e + f x]}}{15 f}
 \end{aligned}$$

Result (type 3, 1569 leaves):

$$\begin{aligned}
 & \left( 5 (8 A - B) \cos \left[ \frac{1}{2} (e + f x) \right] (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{7/2} \right) / \\
 & \left( 64 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^7 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 - \\
 & \left( 5 (6 A + B) \cos \left[ \frac{3}{2} (e + f x) \right] (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{7/2} \right) / \\
 & \left( 192 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^7 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 + \\
 & \left( 3 (10 A - 3 B) \cos \left[ \frac{5}{2} (e + f x) \right] (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{7/2} \right) / \\
 & \left( 320 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^7 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 - \\
 & \left( 3 (4 A + 3 B) \cos \left[ \frac{7}{2} (e + f x) \right] (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{7/2} \right) /
 \end{aligned}$$

$$\begin{aligned}
& \left( 448 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^7 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 + \\
& \left( (12 A - 5 B) \cos \left[ \frac{9}{2} (e + f x) \right] (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{7/2} \right) / \\
& \left( 576 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^7 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 - \\
& \left( (2 A + 5 B) \cos \left[ \frac{11}{2} (e + f x) \right] (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{7/2} \right) / \\
& \left( 704 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^7 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 + \\
& \left( (2 A - B) \cos \left[ \frac{13}{2} (e + f x) \right] (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{7/2} \right) / \\
& \left( 832 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^7 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 - \\
& \left( B \cos \left[ \frac{15}{2} (e + f x) \right] (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{7/2} \right) / \\
& \left( 960 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^7 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 + \\
& \left( 5 (8 A - B) \sin \left[ \frac{1}{2} (e + f x) \right] (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{7/2} \right) / \\
& \left( 64 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^7 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 + \\
& \left( 5 (6 A + B) (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{7/2} \sin \left[ \frac{3}{2} (e + f x) \right] \right) / \\
& \left( 192 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^7 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 + \\
& \left( 3 (10 A - 3 B) (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{7/2} \sin \left[ \frac{5}{2} (e + f x) \right] \right) / \\
& \left( 320 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^7 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 + \\
& \left( 3 (4 A + 3 B) (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{7/2} \sin \left[ \frac{7}{2} (e + f x) \right] \right) / \\
& \left( 448 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^7 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 + \\
& \left( (12 A - 5 B) (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{7/2} \sin \left[ \frac{9}{2} (e + f x) \right] \right) / \\
& \left( 576 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^7 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 + \\
& \left( (2 A + 5 B) (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{7/2} \sin \left[ \frac{11}{2} (e + f x) \right] \right) / \\
& \left( 704 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^7 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 + \\
& \left( (2 A - B) (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{7/2} \sin \left[ \frac{13}{2} (e + f x) \right] \right) /
\end{aligned}$$

$$\begin{aligned} & \left( 832 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^7 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 + \\ & \left( B (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{7/2} \sin \left[ \frac{15}{2} (e + f x) \right] \right) / \\ & \left( 960 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^7 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 \end{aligned}$$

### Problem 99: Result more than twice size of optimal antiderivative.

$$\int (a + a \sin[e + f x])^3 (A + B \sin[e + f x]) (c - c \sin[e + f x])^{5/2} dx$$

Optimal (type 3, 161 leaves, 5 steps):

$$\begin{aligned} & \frac{64 a^3 (13 A + B) c^6 \cos[e + f x]^7}{9009 f (c - c \sin[e + f x])^{7/2}} + \frac{16 a^3 (13 A + B) c^5 \cos[e + f x]^7}{1287 f (c - c \sin[e + f x])^{5/2}} + \\ & \frac{2 a^3 (13 A + B) c^4 \cos[e + f x]^7}{143 f (c - c \sin[e + f x])^{3/2}} - \frac{2 a^3 B c^3 \cos[e + f x]^7}{13 f \sqrt{c - c \sin[e + f x]}} \end{aligned}$$

Result (type 3, 1351 leaves):

$$\begin{aligned} & \left( 5 A \cos \left[ \frac{1}{2} (e + f x) \right] (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{5/2} \right) / \\ & \left( 8 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^5 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 - \\ & \left( 5 (4 A + B) \cos \left[ \frac{3}{2} (e + f x) \right] (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{5/2} \right) / \\ & \left( 96 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^5 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 + \\ & \left( (2 A - B) \cos \left[ \frac{5}{2} (e + f x) \right] (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{5/2} \right) / \\ & \left( 32 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^5 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 - \\ & \left( (5 A + 2 B) \cos \left[ \frac{7}{2} (e + f x) \right] (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{5/2} \right) / \\ & \left( 112 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^5 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 + \\ & \left( (A - 2 B) \cos \left[ \frac{9}{2} (e + f x) \right] (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{5/2} \right) / \\ & \left( 144 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^5 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 - \\ & \left( (2 A + B) \cos \left[ \frac{11}{2} (e + f x) \right] (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{5/2} \right) / \\ & \left( 352 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^5 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 - \\ & \left( B \cos \left[ \frac{13}{2} (e + f x) \right] (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{5/2} \right) / \end{aligned}$$

$$\begin{aligned}
& \left( 416 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^5 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 + \\
& \left( 5 A \sin \left[ \frac{1}{2} (e + f x) \right] (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{5/2} \right) / \\
& \left( 8 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^5 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 + \\
& \left( 5 (4 A + B) (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{5/2} \sin \left[ \frac{3}{2} (e + f x) \right] \right) / \\
& \left( 96 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^5 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 + \\
& \left( 2 A - B (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{5/2} \sin \left[ \frac{5}{2} (e + f x) \right] \right) / \\
& \left( 32 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^5 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 + \\
& \left( 5 A + 2 B (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{5/2} \sin \left[ \frac{7}{2} (e + f x) \right] \right) / \\
& \left( 112 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^5 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 + \\
& \left( A - 2 B (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{5/2} \sin \left[ \frac{9}{2} (e + f x) \right] \right) / \\
& \left( 144 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^5 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 + \\
& \left( 2 A + B (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{5/2} \sin \left[ \frac{11}{2} (e + f x) \right] \right) / \\
& \left( 352 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^5 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 - \\
& \left( B (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{5/2} \sin \left[ \frac{13}{2} (e + f x) \right] \right) / \\
& \left( 416 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^5 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6
\end{aligned}$$

### Problem 100: Result more than twice size of optimal antiderivative.

$$\int (a + a \sin[e + f x])^3 (A + B \sin[e + f x]) (c - c \sin[e + f x])^{3/2} dx$$

Optimal (type 3, 124 leaves, 4 steps):

$$\frac{8 a^3 (11 A + 3 B) c^5 \cos[e + f x]^7}{693 f (c - c \sin[e + f x])^{7/2}} + \frac{2 a^3 (11 A + 3 B) c^4 \cos[e + f x]^7}{99 f (c - c \sin[e + f x])^{5/2}} - \frac{2 a^3 B c^3 \cos[e + f x]^7}{11 f (c - c \sin[e + f x])^{3/2}}$$

Result (type 3, 1157 leaves):

$$\begin{aligned}
& \left( (6 A + B) \cos \left[ \frac{1}{2} (e + f x) \right] (a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{3/2} \right) / \\
& \left( 8 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^3 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 -
\end{aligned}$$

$$\begin{aligned}
 & \left( (8A+3B) \cos\left[\frac{3}{2}(e+fx)\right] (a+a \sin[e+fx])^3 (c-c \sin[e+fx])^{3/2} \right) / \\
 & \left( 24f \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^3 \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^6 \right) - \\
 & \left( B \cos\left[\frac{5}{2}(e+fx)\right] (a+a \sin[e+fx])^3 (c-c \sin[e+fx])^{3/2} \right) / \\
 & \left( 16f \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^3 \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^6 \right) - \\
 & \left( (6A+B) \cos\left[\frac{7}{2}(e+fx)\right] (a+a \sin[e+fx])^3 (c-c \sin[e+fx])^{3/2} \right) / \\
 & \left( 112f \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^3 \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^6 \right) - \\
 & \left( (2A+3B) \cos\left[\frac{9}{2}(e+fx)\right] (a+a \sin[e+fx])^3 (c-c \sin[e+fx])^{3/2} \right) / \\
 & \left( 144f \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^3 \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^6 \right) + \\
 & \left( B \cos\left[\frac{11}{2}(e+fx)\right] (a+a \sin[e+fx])^3 (c-c \sin[e+fx])^{3/2} \right) / \\
 & \left( 176f \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^3 \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^6 \right) + \\
 & \left( (6A+B) \sin\left[\frac{1}{2}(e+fx)\right] (a+a \sin[e+fx])^3 (c-c \sin[e+fx])^{3/2} \right) / \\
 & \left( 8f \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^3 \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^6 \right) + \\
 & \left( (8A+3B) (a+a \sin[e+fx])^3 (c-c \sin[e+fx])^{3/2} \sin\left[\frac{3}{2}(e+fx)\right] \right) / \\
 & \left( 24f \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^3 \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^6 \right) - \\
 & \left( B (a+a \sin[e+fx])^3 (c-c \sin[e+fx])^{3/2} \sin\left[\frac{5}{2}(e+fx)\right] \right) / \\
 & \left( 16f \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^3 \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^6 \right) + \\
 & \left( (6A+B) (a+a \sin[e+fx])^3 (c-c \sin[e+fx])^{3/2} \sin\left[\frac{7}{2}(e+fx)\right] \right) / \\
 & \left( 112f \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^3 \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^6 \right) - \\
 & \left( (2A+3B) (a+a \sin[e+fx])^3 (c-c \sin[e+fx])^{3/2} \sin\left[\frac{9}{2}(e+fx)\right] \right) / \\
 & \left( 144f \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^3 \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^6 \right) - \\
 & \left( B (a+a \sin[e+fx])^3 (c-c \sin[e+fx])^{3/2} \sin\left[\frac{11}{2}(e+fx)\right] \right) / \\
 & \left( 176f \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^3 \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^6 \right)
 \end{aligned}$$

**Problem 102: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(a + a \sin[e + f x])^3 (A + B \sin[e + f x])}{\sqrt{c - c \sin[e + f x]}} dx$$

Optimal (type 3, 200 leaves, 7 steps):

$$\frac{8 \sqrt{2} a^3 (A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{c} \cos[e + f x]}{\sqrt{2} \sqrt{c - c \sin[e + f x]}}\right]}{\sqrt{c} f} - \frac{2 a^3 B c^3 \cos[e + f x]^7}{7 f (c - c \sin[e + f x])^{7/2}} - \frac{2 a^3 (A + B) c^2 \cos[e + f x]^5}{5 f (c - c \sin[e + f x])^{5/2}} - \frac{4 a^3 (A + B) c \cos[e + f x]^3}{3 f (c - c \sin[e + f x])^{3/2}} - \frac{8 a^3 (A + B) \cos[e + f x]}{f \sqrt{c - c \sin[e + f x]}}$$

Result (type 3, 193 leaves):

$$-\frac{1}{420 f \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right)^6 \sqrt{c - c \sin[e + f x]}} a^3 \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right) (1 + \sin[e + f x])^3 \left( (6720 + 6720 i) (-1)^{1/4} (A + B) \operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{1/4} \left(1 + \tan\left[\frac{1}{4}(e + f x)\right]\right)\right] - 2 \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right) (-2086 A - 2236 B + 6 (7 A + 22 B) \cos[2(e + f x)] - (448 A + 673 B) \sin[e + f x] + 15 B \sin[3(e + f x)]) \right)$$

**Problem 103: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sin[e + f x])^3 (A + B \sin[e + f x])}{(c - c \sin[e + f x])^{3/2}} dx$$

Optimal (type 3, 218 leaves, 7 steps):

$$-\frac{2 \sqrt{2} a^3 (5 A + 9 B) \operatorname{ArcTanh}\left[\frac{\sqrt{c} \cos[e + f x]}{\sqrt{2} \sqrt{c - c \sin[e + f x]}}\right]}{c^{3/2} f} + \frac{a^3 (A + B) c^3 \cos[e + f x]^7}{2 f (c - c \sin[e + f x])^{9/2}} + \frac{a^3 (5 A + 9 B) c \cos[e + f x]^5}{10 f (c - c \sin[e + f x])^{5/2}} + \frac{a^3 (5 A + 9 B) \cos[e + f x]^3}{3 f (c - c \sin[e + f x])^{3/2}} + \frac{2 a^3 (5 A + 9 B) \cos[e + f x]}{c f \sqrt{c - c \sin[e + f x]}}$$

Result (type 3, 444 leaves):



1

$$\begin{aligned}
 & 30 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 (c - c \sin[e + f x])^{3/2} \\
 & a^3 \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) (1 + \sin[e + f x])^3 \\
 & \left( 120 (A + B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) + (120 + 120 i) (-1)^{1/4} (5 A + 9 B) \right. \\
 & \quad \left. \operatorname{ArcTan} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{1/4} \left( 1 + \tan \left[ \frac{1}{4} (e + f x) \right] \right) \right] \right) \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 + \\
 & 30 (9 A + 20 B) \cos \left[ \frac{1}{2} (e + f x) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 - \\
 & 5 (2 A + 9 B) \cos \left[ \frac{3}{2} (e + f x) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 - \\
 & 3 B \cos \left[ \frac{5}{2} (e + f x) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 + 240 (A + B) \sin \left[ \frac{1}{2} (e + f x) \right] + \\
 & 30 (9 A + 20 B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 \sin \left[ \frac{1}{2} (e + f x) \right] + \\
 & 5 (2 A + 9 B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 \sin \left[ \frac{3}{2} (e + f x) \right] - \\
 & 3 B \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 \sin \left[ \frac{5}{2} (e + f x) \right]
 \end{aligned}$$

**Problem 104: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(a + a \sin[e + f x])^3 (A + B \sin[e + f x])}{(c - c \sin[e + f x])^{5/2}} dx$$

Optimal (type 3, 225 leaves, 7 steps):

$$\begin{aligned}
 & \frac{5 a^3 (3 A + 11 B) \operatorname{ArcTanh} \left[ \frac{\sqrt{c} \cos[e + f x]}{\sqrt{2} \sqrt{c - c \sin[e + f x]}} \right]}{2 \sqrt{2} c^{5/2} f} + \frac{a^3 (A + B) c^3 \cos[e + f x]^7}{4 f (c - c \sin[e + f x])^{11/2}} - \\
 & \frac{a^3 (3 A + 11 B) c \cos[e + f x]^5}{8 f (c - c \sin[e + f x])^{7/2}} - \frac{5 a^3 (3 A + 11 B) \cos[e + f x]^3}{24 c f (c - c \sin[e + f x])^{3/2}} - \frac{5 a^3 (3 A + 11 B) \cos[e + f x]}{4 c^2 f \sqrt{c - c \sin[e + f x]}}
 \end{aligned}$$

Result (type 3, 434 leaves):

$$\begin{aligned}
& \frac{1}{6 f \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right)^6 (c-c \sin [e+f x])^{5/2}} \\
& a^3 \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right) (1+\sin [e+f x])^3 \\
& \left( 12 (A+B) \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right) - \right. \\
& \quad 3 (9 A+17 B) \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right)^3 - (15+15 i) (-1)^{1/4} (3 A+11 B) \\
& \quad \text{ArcTan} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{1/4} \left( 1 + \tan \left[ \frac{1}{4} (e+f x) \right] \right) \right] \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right)^4 - \\
& \quad 6 (2 A+11 B) \cos \left[ \frac{1}{2} (e+f x) \right] \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right)^4 + \\
& \quad 2 B \cos \left[ \frac{3}{2} (e+f x) \right] \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right)^4 + 24 (A+B) \sin \left[ \frac{1}{2} (e+f x) \right] - \\
& \quad 6 (9 A+17 B) \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right)^2 \sin \left[ \frac{1}{2} (e+f x) \right] - \\
& \quad 6 (2 A+11 B) \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right)^4 \sin \left[ \frac{1}{2} (e+f x) \right] - \\
& \quad \left. 2 B \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right)^4 \sin \left[ \frac{3}{2} (e+f x) \right] \right)
\end{aligned}$$

**Problem 105: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a+a \sin [e+f x])^3 (A+B \sin [e+f x])}{(c-c \sin [e+f x])^{7/2}} dx$$

Optimal (type 3, 217 leaves, 7 steps):

$$\begin{aligned}
& -\frac{5 a^3 (A+13 B) \text{ArcTanh} \left[ \frac{\sqrt{c} \cos [e+f x]}{\sqrt{2} \sqrt{c-c \sin [e+f x]}} \right]}{8 \sqrt{2} c^{7/2} f} + \frac{a^3 (A+B) c^3 \cos [e+f x]^7}{6 f (c-c \sin [e+f x])^{13/2}} - \\
& \frac{a^3 (A+13 B) c \cos [e+f x]^5}{24 f (c-c \sin [e+f x])^{9/2}} + \frac{5 a^3 (A+13 B) \cos [e+f x]^3}{48 c f (c-c \sin [e+f x])^{5/2}} + \frac{5 a^3 (A+13 B) \cos [e+f x]}{16 c^3 f \sqrt{c-c \sin [e+f x]}}
\end{aligned}$$

Result (type 3, 910 leaves):

$$\begin{aligned}
 & \frac{4 (A+B) \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^2 (a+a \sin[e+fx])^3}{3 f \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^6 (c-c \sin[e+fx])^{7/2}} + \\
 & \left( (-13A-25B) \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^4 (a+a \sin[e+fx])^3 \right) / \\
 & \left( 6 f \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^6 (c-c \sin[e+fx])^{7/2} \right) + \\
 & \left( (11A+47B) \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^6 (a+a \sin[e+fx])^3 \right) / \\
 & \left( 8 f \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^6 (c-c \sin[e+fx])^{7/2} \right) + \left( \left( \frac{5}{8} + \frac{5i}{8} \right) (-1)^{1/4} \right. \\
 & \quad \left. (A+13B) \operatorname{ArcTan}\left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{1/4} \operatorname{Sec}\left[\frac{1}{4}(e+fx)\right] \left( \cos\left[\frac{1}{4}(e+fx)\right] + \sin\left[\frac{1}{4}(e+fx)\right] \right) \right] \right) \\
 & \quad \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^7 (a+a \sin[e+fx])^3 \right) / \\
 & \left( f \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^6 (c-c \sin[e+fx])^{7/2} \right) + \\
 & \left( 2B \cos\left[\frac{1}{2}(e+fx)\right] \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^7 (a+a \sin[e+fx])^3 \right) / \\
 & \left( f \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^6 (c-c \sin[e+fx])^{7/2} \right) + \\
 & \left( 2B \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^7 \sin\left[\frac{1}{2}(e+fx)\right] (a+a \sin[e+fx])^3 \right) / \\
 & \left( f \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^6 (c-c \sin[e+fx])^{7/2} \right) + \\
 & \left( \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^3 \left( -13A \sin\left[\frac{1}{2}(e+fx)\right] - 25B \sin\left[\frac{1}{2}(e+fx)\right] \right) \right. \\
 & \quad \left. (a+a \sin[e+fx])^3 \right) / \left( 3 f \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^6 (c-c \sin[e+fx])^{7/2} \right) + \\
 & \left( 8 \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right) \left( A \sin\left[\frac{1}{2}(e+fx)\right] + B \sin\left[\frac{1}{2}(e+fx)\right] \right) \right. \\
 & \quad \left. (a+a \sin[e+fx])^3 \right) / \left( 3 f \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^6 (c-c \sin[e+fx])^{7/2} \right) + \\
 & \left( \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 \left( 11A \sin\left[\frac{1}{2}(e+fx)\right] + 47B \sin\left[\frac{1}{2}(e+fx)\right] \right) \right. \\
 & \quad \left. (a+a \sin[e+fx])^3 \right) / \left( 4 f \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^6 (c-c \sin[e+fx])^{7/2} \right)
 \end{aligned}$$

**Problem 106: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(a+a \sin[e+fx])^3 (A+B \sin[e+fx])}{(c-c \sin[e+fx])^{9/2}} dx$$

Optimal (type 3, 217 leaves, 7 steps):

$$\begin{aligned}
& - \frac{5 a^3 (A - 15 B) \operatorname{ArcTanh}\left[\frac{\sqrt{c} \cos[e+f x]}{\sqrt{2} \sqrt{c-c \sin[e+f x]}}\right]}{128 \sqrt{2} c^{9/2} f} + \frac{a^3 (A+B) c^3 \cos[e+f x]^7}{8 f (c-c \sin[e+f x])^{15/2}} + \\
& \frac{a^3 (A-15 B) c \cos[e+f x]^5}{48 f (c-c \sin[e+f x])^{11/2}} - \frac{5 a^3 (A-15 B) \cos[e+f x]^3}{192 c f (c-c \sin[e+f x])^{7/2}} + \frac{5 a^3 (A-15 B) \cos[e+f x]}{128 c^3 f (c-c \sin[e+f x])^{3/2}}
\end{aligned}$$

Result (type 3, 431 leaves):

$$\begin{aligned}
& \left( \left( \frac{5}{128} + \frac{5 i}{128} \right) (-1)^{1/4} (A-15 B) \right. \\
& \quad \left. \operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{1/4} \operatorname{Sec}\left[\frac{1}{4}(e+f x)\right] \left(\cos\left[\frac{1}{4}(e+f x)\right] + \sin\left[\frac{1}{4}(e+f x)\right]\right)\right] \right] \\
& \quad \left( \cos\left[\frac{1}{2}(e+f x)\right] - \sin\left[\frac{1}{2}(e+f x)\right] \right)^9 (a+a \sin[e+f x])^3 \Big/ \\
& \quad \left( f \left( \cos\left[\frac{1}{2}(e+f x)\right] + \sin\left[\frac{1}{2}(e+f x)\right] \right)^6 (c-c \sin[e+f x])^{9/2} \right) + \\
& \quad \frac{1}{3072 f \left( \cos\left[\frac{1}{2}(e+f x)\right] + \sin\left[\frac{1}{2}(e+f x)\right] \right)^6 (c-c \sin[e+f x])^{9/2}} \\
& \quad \left( \cos\left[\frac{1}{2}(e+f x)\right] - \sin\left[\frac{1}{2}(e+f x)\right] \right) (a+a \sin[e+f x])^3 \\
& \quad \left( 1765 A \cos\left[\frac{1}{2}(e+f x)\right] + 405 B \cos\left[\frac{1}{2}(e+f x)\right] - 895 A \cos\left[\frac{3}{2}(e+f x)\right] - \right. \\
& \quad \left. 2703 B \cos\left[\frac{3}{2}(e+f x)\right] - 397 A \cos\left[\frac{5}{2}(e+f x)\right] + 579 B \cos\left[\frac{5}{2}(e+f x)\right] + \right. \\
& \quad \left. 15 A \cos\left[\frac{7}{2}(e+f x)\right] + 543 B \cos\left[\frac{7}{2}(e+f x)\right] + 1765 A \sin\left[\frac{1}{2}(e+f x)\right] + \right. \\
& \quad \left. 405 B \sin\left[\frac{1}{2}(e+f x)\right] + 895 A \sin\left[\frac{3}{2}(e+f x)\right] + 2703 B \sin\left[\frac{3}{2}(e+f x)\right] - \right. \\
& \quad \left. 397 A \sin\left[\frac{5}{2}(e+f x)\right] + 579 B \sin\left[\frac{5}{2}(e+f x)\right] - 15 A \sin\left[\frac{7}{2}(e+f x)\right] - 543 B \sin\left[\frac{7}{2}(e+f x)\right] \right)
\end{aligned}$$

**Problem 107: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(a+a \sin[e+f x])^3 (A+B \sin[e+f x])}{(c-c \sin[e+f x])^{11/2}} dx$$

Optimal (type 3, 266 leaves, 8 steps):

$$\begin{aligned}
& - \frac{a^3 (3 A - 17 B) \operatorname{ArcTanh}\left[\frac{\sqrt{c} \cos[e+f x]}{\sqrt{2} \sqrt{c-c \sin[e+f x]}}\right]}{512 \sqrt{2} c^{11/2} f} + \frac{a^3 (A+B) c^3 \cos[e+f x]^7}{10 f (c-c \sin[e+f x])^{17/2}} + \\
& \frac{a^3 (3 A - 17 B) c \cos[e+f x]^5}{80 f (c-c \sin[e+f x])^{13/2}} - \frac{a^3 (3 A - 17 B) \cos[e+f x]^3}{96 c f (c-c \sin[e+f x])^{9/2}} + \\
& \frac{a^3 (3 A - 17 B) \cos[e+f x]}{128 c^3 f (c-c \sin[e+f x])^{5/2}} - \frac{a^3 (3 A - 17 B) \cos[e+f x]}{512 c^4 f (c-c \sin[e+f x])^{3/2}}
\end{aligned}$$

Result (type 3, 485 leaves):

$$\left( \left( \frac{1}{512} + \frac{i}{512} \right) (-1)^{1/4} (3A - 17B) \right. \\ \left. \text{ArcTan} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{1/4} \text{Sec} \left[ \frac{1}{4} (e + f x) \right] \left( \text{Cos} \left[ \frac{1}{4} (e + f x) \right] + \text{Sin} \left[ \frac{1}{4} (e + f x) \right] \right) \right] \right. \\ \left. \left( \text{Cos} \left[ \frac{1}{2} (e + f x) \right] - \text{Sin} \left[ \frac{1}{2} (e + f x) \right] \right)^{11} (a + a \text{Sin}[e + f x])^3 \right) / \\ \left( f \left( \text{Cos} \left[ \frac{1}{2} (e + f x) \right] + \text{Sin} \left[ \frac{1}{2} (e + f x) \right] \right)^6 (c - c \text{Sin}[e + f x])^{11/2} \right) + \\ \left( \left( \text{Cos} \left[ \frac{1}{2} (e + f x) \right] - \text{Sin} \left[ \frac{1}{2} (e + f x) \right] \right) (a + a \text{Sin}[e + f x])^3 \right. \\ \left. \left( 56370A \text{Cos} \left[ \frac{1}{2} (e + f x) \right] + 38970B \text{Cos} \left[ \frac{1}{2} (e + f x) \right] - \right. \right. \\ \left. \left. 31140A \text{Cos} \left[ \frac{3}{2} (e + f x) \right] - 38580B \text{Cos} \left[ \frac{3}{2} (e + f x) \right] - 10404A \text{Cos} \left[ \frac{5}{2} (e + f x) \right] - \right. \right. \\ \left. \left. 12724B \text{Cos} \left[ \frac{5}{2} (e + f x) \right] + 435A \text{Cos} \left[ \frac{7}{2} (e + f x) \right] + 7775B \text{Cos} \left[ \frac{7}{2} (e + f x) \right] - \right. \right. \\ \left. \left. 45A \text{Cos} \left[ \frac{9}{2} (e + f x) \right] + 255B \text{Cos} \left[ \frac{9}{2} (e + f x) \right] + 56370A \text{Sin} \left[ \frac{1}{2} (e + f x) \right] + \right. \right. \\ \left. \left. 38970B \text{Sin} \left[ \frac{1}{2} (e + f x) \right] + 31140A \text{Sin} \left[ \frac{3}{2} (e + f x) \right] + 38580B \text{Sin} \left[ \frac{3}{2} (e + f x) \right] - \right. \right. \\ \left. \left. 10404A \text{Sin} \left[ \frac{5}{2} (e + f x) \right] - 12724B \text{Sin} \left[ \frac{5}{2} (e + f x) \right] - 435A \text{Sin} \left[ \frac{7}{2} (e + f x) \right] - \right. \right. \\ \left. \left. 7775B \text{Sin} \left[ \frac{7}{2} (e + f x) \right] - 45A \text{Sin} \left[ \frac{9}{2} (e + f x) \right] + 255B \text{Sin} \left[ \frac{9}{2} (e + f x) \right] \right) \right) / \\ \left( 122880f \left( \text{Cos} \left[ \frac{1}{2} (e + f x) \right] + \text{Sin} \left[ \frac{1}{2} (e + f x) \right] \right)^6 (c - c \text{Sin}[e + f x])^{11/2} \right)$$

**Problem 108: Result more than twice size of optimal antiderivative.**

$$\int \frac{(A + B \text{Sin}[e + f x]) (c - c \text{Sin}[e + f x])^{7/2}}{a + a \text{Sin}[e + f x]} dx$$

Optimal (type 3, 200 leaves, 6 steps):

$$\frac{128 (7A - 9B) c^4 \text{Cos}[e + f x]}{35 a f \sqrt{c - c \text{Sin}[e + f x]}} - \frac{32 (7A - 9B) c^3 \text{Cos}[e + f x] \sqrt{c - c \text{Sin}[e + f x]}}{35 a f} - \\ \frac{12 (7A - 9B) c^2 \text{Cos}[e + f x] (c - c \text{Sin}[e + f x])^{3/2}}{35 a f} - \\ \frac{(7A - 9B) c \text{Cos}[e + f x] (c - c \text{Sin}[e + f x])^{5/2}}{7 a f} - \frac{(A - B) \text{Sec}[e + f x] (c - c \text{Sin}[e + f x])^{9/2}}{a c f}$$

Result (type 3, 864 leaves):

$$\begin{aligned}
& - \left( \left( 16 (A - B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) (c - c \sin[e + f x])^{7/2} \right) / \right. \\
& \quad \left. \left( f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^7 (a + a \sin[e + f x]) \right) \right) - \\
& \left( (76 A - 111 B) \cos \left[ \frac{1}{2} (e + f x) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 (c - c \sin[e + f x])^{7/2} \right) / \\
& \left( 4 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^7 (a + a \sin[e + f x]) \right) - \\
& \left( (6 A - 13 B) \cos \left[ \frac{3}{2} (e + f x) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 (c - c \sin[e + f x])^{7/2} \right) / \\
& \left( 4 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^7 (a + a \sin[e + f x]) \right) + \\
& \left( (2 A - 9 B) \cos \left[ \frac{5}{2} (e + f x) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 (c - c \sin[e + f x])^{7/2} \right) / \\
& \left( 20 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^7 (a + a \sin[e + f x]) \right) - \\
& \left( B \cos \left[ \frac{7}{2} (e + f x) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 (c - c \sin[e + f x])^{7/2} \right) / \\
& \left( 28 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^7 (a + a \sin[e + f x]) \right) - \\
& \left( (76 A - 111 B) \sin \left[ \frac{1}{2} (e + f x) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 (c - c \sin[e + f x])^{7/2} \right) / \\
& \left( 4 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^7 (a + a \sin[e + f x]) \right) + \\
& \left( (6 A - 13 B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 (c - c \sin[e + f x])^{7/2} \sin \left[ \frac{3}{2} (e + f x) \right] \right) / \\
& \left( 4 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^7 (a + a \sin[e + f x]) \right) + \\
& \left( (2 A - 9 B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 (c - c \sin[e + f x])^{7/2} \sin \left[ \frac{5}{2} (e + f x) \right] \right) / \\
& \left( 20 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^7 (a + a \sin[e + f x]) \right) + \\
& \left( B \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 (c - c \sin[e + f x])^{7/2} \sin \left[ \frac{7}{2} (e + f x) \right] \right) / \\
& \left( 28 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^7 (a + a \sin[e + f x]) \right)
\end{aligned}$$

**Problem 112: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A + B \sin[e + f x]}{(a + a \sin[e + f x]) \sqrt{c - c \sin[e + f x]}} dx$$

Optimal (type 3, 91 leaves, 4 steps):

$$\frac{(A+B) \operatorname{ArcTanh}\left[\frac{\sqrt{c} \cos[e+fx]}{\sqrt{2} \sqrt{c-c \sin[e+fx]}}\right]}{\sqrt{2} a \sqrt{c} f} - \frac{(A-B) \operatorname{Sec}[e+fx] \sqrt{c-c \sin[e+fx]}}{a c f}$$

Result (type 3, 140 leaves):

$$\left( \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right) \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right) \right. \\ \left. \left( -A+B - (1+i) (-1)^{1/4} (A+B) \operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{1/4} \left(1 + \tan\left[\frac{1}{4}(e+fx)\right]\right)\right] \right) \right. \\ \left. \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right) \right) / \left( a f (1 + \sin[e+fx]) \sqrt{c-c \sin[e+fx]} \right)$$

**Problem 113: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A+B \sin[e+fx]}{(a+a \sin[e+fx]) (c-c \sin[e+fx])^{3/2}} dx$$

Optimal (type 3, 136 leaves, 5 steps):

$$\frac{(3A-B) \operatorname{ArcTanh}\left[\frac{\sqrt{c} \cos[e+fx]}{\sqrt{2} \sqrt{c-c \sin[e+fx]}}\right]}{4 \sqrt{2} a c^{3/2} f} + \frac{(3A-B) \cos[e+fx]}{4 a f (c-c \sin[e+fx])^{3/2}} - \frac{(A-B) \operatorname{Sec}[e+fx]}{a c f \sqrt{c-c \sin[e+fx]}}$$

Result (type 3, 284 leaves):

$$\frac{1}{4 a f (1 + \sin[e+fx]) (c-c \sin[e+fx])^{3/2}} \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right) \\ \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right) \left( 2(-A+B) \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right) \right)^2 + \\ (A+B) \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right) \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right) - \\ (1+i) (-1)^{1/4} (3A-B) \operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{1/4} \left(1 + \tan\left[\frac{1}{4}(e+fx)\right]\right)\right] \\ \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^2 \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right) + \\ 2(A+B) \sin\left[\frac{1}{2}(e+fx)\right] \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)$$

**Problem 114: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A+B \sin[e+fx]}{(a+a \sin[e+fx]) (c-c \sin[e+fx])^{5/2}} dx$$

Optimal (type 3, 180 leaves, 6 steps):

$$\frac{3 (5 A - 3 B) \operatorname{ArcTanh}\left[\frac{\sqrt{c} \operatorname{Cos}[e+f x]}{\sqrt{2} \sqrt{c-c \operatorname{Sin}[e+f x]}}\right]}{32 \sqrt{2} a c^{5/2} f} + \frac{3 (5 A - 3 B) \operatorname{Cos}[e+f x]}{32 a c f (c-c \operatorname{Sin}[e+f x])^{3/2}} +$$

$$\frac{(A+B) \operatorname{Sec}[e+f x]}{4 a c f (c-c \operatorname{Sin}[e+f x])^{3/2}} - \frac{(5 A - 3 B) \operatorname{Sec}[e+f x]}{8 a c^2 f \sqrt{c-c \operatorname{Sin}[e+f x]}}$$

Result (type 3, 404 leaves):

$$\frac{1}{32 a f (1 + \operatorname{Sin}[e+f x]) (c-c \operatorname{Sin}[e+f x])^{5/2}} \left( \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] - \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] \right)$$

$$\left( \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] + \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] \right) \left( 8 (-A+B) \left( \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] - \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] \right) \right)^4 +$$

$$4 (A+B) \left( \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] - \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] \right) \left( \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] + \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] \right) +$$

$$(7 A - B) \left( \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] - \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] \right)^3 \left( \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] + \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] \right) -$$

$$(3 + 3 i) (-1)^{1/4} (5 A - 3 B) \operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{1/4} \left(1 + \operatorname{Tan}\left[\frac{1}{4}(e+f x)\right]\right)\right]$$

$$\left( \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] - \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] \right)^4 \left( \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] + \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] \right) +$$

$$8 (A+B) \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] \left( \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] + \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] \right) +$$

$$2 (7 A - B) \left( \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] - \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] \right)^2$$

$$\operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] \left( \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] + \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] \right)$$

### Problem 115: Result more than twice size of optimal antiderivative.

$$\int \frac{(A+B \operatorname{Sin}[e+f x]) (c-c \operatorname{Sin}[e+f x])^{9/2}}{(a+a \operatorname{Sin}[e+f x])^2} dx$$

Optimal (type 3, 242 leaves, 7 steps):

$$\frac{2048 (7 A - 13 B) c^4 \operatorname{Sec}[e+f x] \sqrt{c-c \operatorname{Sin}[e+f x]}}{105 a^2 f} -$$

$$\frac{512 (7 A - 13 B) c^3 \operatorname{Sec}[e+f x] (c-c \operatorname{Sin}[e+f x])^{3/2}}{105 a^2 f} -$$

$$\frac{64 (7 A - 13 B) c^2 \operatorname{Sec}[e+f x] (c-c \operatorname{Sin}[e+f x])^{5/2}}{105 a^2 f} -$$

$$\frac{16 (7 A - 13 B) c \operatorname{Sec}[e+f x] (c-c \operatorname{Sin}[e+f x])^{7/2}}{105 a^2 f} -$$

$$\frac{(7 A - 13 B) \operatorname{Sec}[e+f x] (c-c \operatorname{Sin}[e+f x])^{9/2}}{21 a^2 f} - \frac{(A-B) \operatorname{Sec}[e+f x]^3 (c-c \operatorname{Sin}[e+f x])^{13/2}}{3 a^2 c^2 f}$$



Result (type 3, 953 leaves):

$$\begin{aligned}
 & - \left( \left( 32 (A - B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) (c - c \sin[e + f x])^{9/2} \right) / \right. \\
 & \quad \left. \left( 3 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 (a + a \sin[e + f x])^2 \right) \right) + \\
 & \left( 32 (2A - 3B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^3 (c - c \sin[e + f x])^{9/2} \right) / \\
 & \quad \left( f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 (a + a \sin[e + f x])^2 \right) + \\
 & \left( (164A - 351B) \cos \left[ \frac{1}{2} (e + f x) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^4 (c - c \sin[e + f x])^{9/2} \right) / \\
 & \quad \left( 4 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 (a + a \sin[e + f x])^2 \right) + \\
 & \left( (26A - 83B) \cos \left[ \frac{3}{2} (e + f x) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^4 (c - c \sin[e + f x])^{9/2} \right) / \\
 & \quad \left( 12 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 (a + a \sin[e + f x])^2 \right) - \\
 & \left( (2A - 13B) \cos \left[ \frac{5}{2} (e + f x) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^4 (c - c \sin[e + f x])^{9/2} \right) / \\
 & \quad \left( 20 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 (a + a \sin[e + f x])^2 \right) + \\
 & \left( B \cos \left[ \frac{7}{2} (e + f x) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^4 (c - c \sin[e + f x])^{9/2} \right) / \\
 & \quad \left( 28 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 (a + a \sin[e + f x])^2 \right) + \\
 & \left( (164A - 351B) \sin \left[ \frac{1}{2} (e + f x) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^4 (c - c \sin[e + f x])^{9/2} \right) / \\
 & \quad \left( 4 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 (a + a \sin[e + f x])^2 \right) - \\
 & \left( (26A - 83B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^4 (c - c \sin[e + f x])^{9/2} \sin \left[ \frac{3}{2} (e + f x) \right] \right) / \\
 & \quad \left( 12 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 (a + a \sin[e + f x])^2 \right) - \\
 & \left( (2A - 13B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^4 (c - c \sin[e + f x])^{9/2} \sin \left[ \frac{5}{2} (e + f x) \right] \right) / \\
 & \quad \left( 20 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 (a + a \sin[e + f x])^2 \right) - \\
 & \left( B \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^4 (c - c \sin[e + f x])^{9/2} \sin \left[ \frac{7}{2} (e + f x) \right] \right) / \\
 & \quad \left( 28 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 (a + a \sin[e + f x])^2 \right)
 \end{aligned}$$

### Problem 120: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{A + B \sin[e + f x]}{(a + a \sin[e + f x])^2 \sqrt{c - c \sin[e + f x]}} dx$$

Optimal (type 3, 135 leaves, 5 steps):

$$\frac{(A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{c} \cos[e + f x]}{\sqrt{2} \sqrt{c - c \sin[e + f x]}}\right]}{2 \sqrt{2} a^2 \sqrt{c} f} - \frac{(A + B) \operatorname{Sec}[e + f x] \sqrt{c - c \sin[e + f x]}}{2 a^2 c f} - \frac{(A - B) \operatorname{Sec}[e + f x]^3 (c - c \sin[e + f x])^{3/2}}{3 a^2 c^2 f}$$

Result (type 3, 176 leaves):

$$\left( \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right) \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right) \right. \\ \left. \left( 2(-A + B) - 3(A + B) \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right)^2 - (3 + 3i)(-1)^{1/4}(A + B) \right. \right. \\ \left. \left. \operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right)(-1)^{1/4}\left(1 + \tan\left[\frac{1}{4}(e + f x)\right]\right)\right] \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right)^3 \right) \right) / \\ \left( 6 a^2 f (1 + \sin[e + f x])^2 \sqrt{c - c \sin[e + f x]} \right)$$

### Problem 121: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{A + B \sin[e + f x]}{(a + a \sin[e + f x])^2 (c - c \sin[e + f x])^{3/2}} dx$$

Optimal (type 3, 175 leaves, 6 steps):

$$\frac{(5A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{c} \cos[e + f x]}{\sqrt{2} \sqrt{c - c \sin[e + f x]}}\right]}{8 \sqrt{2} a^2 c^{3/2} f} + \frac{(5A + B) \cos[e + f x]}{8 a^2 f (c - c \sin[e + f x])^{3/2}} - \\ \frac{(5A + B) \operatorname{Sec}[e + f x]}{6 a^2 c f \sqrt{c - c \sin[e + f x]}} - \frac{(A - B) \operatorname{Sec}[e + f x]^3 \sqrt{c - c \sin[e + f x]}}{3 a^2 c^2 f}$$

Result (type 3, 300 leaves):

$$\begin{aligned}
 & \frac{1}{24 a^2 f (1 + \sin[e + f x])^2 (c - c \sin[e + f x])^{3/2}} \\
 & \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right) \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right) \\
 & \left( -12 A \cos[e + f x]^2 + 4 (-A + B) \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right)^2 + \right. \\
 & \quad \left. 3 (A + B) \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right) \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right) \right)^3 - \\
 & (3 + 3 i) (-1)^{1/4} (5 A + B) \operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{1/4} \left(1 + \tan\left[\frac{1}{4}(e + f x)\right]\right)\right] \\
 & \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right)^2 \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right)^3 + \\
 & 6 (A + B) \sin\left[\frac{1}{2}(e + f x)\right] \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right)^3
 \end{aligned}$$

**Problem 122: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A + B \sin[e + f x]}{(a + a \sin[e + f x])^2 (c - c \sin[e + f x])^{5/2}} dx$$

Optimal (type 3, 225 leaves, 7 steps):

$$\begin{aligned}
 & \frac{5 (7 A - B) \operatorname{ArcTanh}\left[\frac{\sqrt{c} \cos[e + f x]}{\sqrt{2} \sqrt{c - c \sin[e + f x]}}\right]}{64 \sqrt{2} a^2 c^{5/2} f} + \frac{5 (7 A - B) \cos[e + f x]}{64 a^2 c f (c - c \sin[e + f x])^{3/2}} + \\
 & \frac{(7 A - B) \operatorname{Sec}[e + f x]}{24 a^2 c f (c - c \sin[e + f x])^{3/2}} - \frac{5 (7 A - B) \operatorname{Sec}[e + f x]}{48 a^2 c^2 f \sqrt{c - c \sin[e + f x]}} - \frac{(A - B) \operatorname{Sec}[e + f x]^3}{3 a^2 c^2 f \sqrt{c - c \sin[e + f x]}}
 \end{aligned}$$

Result (type 3, 430 leaves):

$$\frac{1}{192 a^2 f (1 + \sin[e + f x])^2 (c - c \sin[e + f x])^{5/2}} \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right) \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right) \left( 3 (11 A + 3 B) \cos[e + f x]^3 + 16 (-A + B) \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right)^4 + 24 (-3 A + B) \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right)^4 \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right)^2 + 12 (A + B) \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right) \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right)^3 - (15 + 15 i) (-1)^{1/4} (7 A - B) \operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{1/4} \left(1 + \tan\left[\frac{1}{4}(e + f x)\right]\right)\right] \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right)^4 \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right)^3 + 24 (A + B) \sin\left[\frac{1}{2}(e + f x)\right] \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right)^3 + 6 (11 A + 3 B) \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right)^2 \sin\left[\frac{1}{2}(e + f x)\right] \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right)^3 \right)$$

**Problem 123: Result more than twice size of optimal antiderivative.**

$$\int \frac{(A + B \sin[e + f x]) (c - c \sin[e + f x])^{9/2}}{(a + a \sin[e + f x])^3} dx$$

Optimal (type 3, 242 leaves, 7 steps):

$$\begin{aligned} & - \frac{2048 (A - 3 B) c^3 \operatorname{Sec}[e + f x]^3 (c - c \sin[e + f x])^{3/2}}{15 a^3 f} + \\ & \frac{512 (A - 3 B) c^2 \operatorname{Sec}[e + f x]^3 (c - c \sin[e + f x])^{5/2}}{5 a^3 f} - \\ & \frac{64 (A - 3 B) c \operatorname{Sec}[e + f x]^3 (c - c \sin[e + f x])^{7/2}}{5 a^3 f} - \frac{16 (A - 3 B) \operatorname{Sec}[e + f x]^3 (c - c \sin[e + f x])^{9/2}}{15 a^3 f} - \\ & \frac{(A - 3 B) \operatorname{Sec}[e + f x]^3 (c - c \sin[e + f x])^{11/2}}{5 a^3 c f} - \frac{(A - B) \operatorname{Sec}[e + f x]^5 (c - c \sin[e + f x])^{15/2}}{5 a^3 c^3 f} \end{aligned}$$

Result (type 3, 840 leaves):

$$\begin{aligned}
 & - \left( \left( 32 (A - B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) (c - c \sin[e + f x])^{9/2} \right) / \right. \\
 & \quad \left. \left( 5 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 (a + a \sin[e + f x])^3 \right) + \right. \\
 & \quad \left( 32 (2A - 3B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^3 (c - c \sin[e + f x])^{9/2} \right) / \\
 & \quad \left( 3 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 (a + a \sin[e + f x])^3 \right) - \\
 & \quad \left( 16 (3A - 7B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^5 (c - c \sin[e + f x])^{9/2} \right) / \\
 & \quad \left( f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 (a + a \sin[e + f x])^3 \right) - \\
 & \quad \left( (15A - 56B) \cos \left[ \frac{1}{2} (e + f x) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 (c - c \sin[e + f x])^{9/2} \right) / \\
 & \quad \left( f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 (a + a \sin[e + f x])^3 \right) - \\
 & \quad \left( (2A - 15B) \cos \left[ \frac{3}{2} (e + f x) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 (c - c \sin[e + f x])^{9/2} \right) / \\
 & \quad \left( 6 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 (a + a \sin[e + f x])^3 \right) - \\
 & \quad \left( B \cos \left[ \frac{5}{2} (e + f x) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 (c - c \sin[e + f x])^{9/2} \right) / \\
 & \quad \left( 10 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 (a + a \sin[e + f x])^3 \right) - \\
 & \quad \left( (15A - 56B) \sin \left[ \frac{1}{2} (e + f x) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 (c - c \sin[e + f x])^{9/2} \right) / \\
 & \quad \left( f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 (a + a \sin[e + f x])^3 \right) + \\
 & \quad \left( (2A - 15B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 (c - c \sin[e + f x])^{9/2} \sin \left[ \frac{3}{2} (e + f x) \right] \right) / \\
 & \quad \left( 6 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 (a + a \sin[e + f x])^3 \right) - \\
 & \quad \left( B \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^6 (c - c \sin[e + f x])^{9/2} \sin \left[ \frac{5}{2} (e + f x) \right] \right) / \\
 & \quad \left( 10 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 (a + a \sin[e + f x])^3 \right)
 \end{aligned}$$

**Problem 128: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A + B \sin[e + f x]}{(a + a \sin[e + f x])^3 \sqrt{c - c \sin[e + f x]}} dx$$

Optimal (type 3, 174 leaves, 6 steps):

$$\frac{(A+B) \operatorname{ArcTanh}\left[\frac{\sqrt{c} \cos[e+fx]}{\sqrt{2} \sqrt{c-c \sin[e+fx]}}\right]}{4 \sqrt{2} a^3 \sqrt{c} f} - \frac{(A+B) \operatorname{Sec}[e+fx] \sqrt{c-c \sin[e+fx]}}{4 a^3 c f} - \frac{(A+B) \operatorname{Sec}[e+fx]^3 (c-c \sin[e+fx])^{3/2}}{6 a^3 c^2 f} - \frac{(A-B) \operatorname{Sec}[e+fx]^5 (c-c \sin[e+fx])^{5/2}}{5 a^3 c^3 f}$$

Result (type 3, 204 leaves):

$$\frac{1}{60 a^3 f (1 + \sin[e+fx])^3 \sqrt{c-c \sin[e+fx]}} \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right) \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right) \left( 12(-A+B) - 10(A+B) \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^2 - 15(A+B) \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^4 - (15+15i)(-1)^{1/4}(A+B) \operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right)(-1)^{1/4} \left(1 + \tan\left[\frac{1}{4}(e+fx)\right]\right)\right] \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 \right)$$

**Problem 129: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A+B \sin[e+fx]}{(a+a \sin[e+fx])^3 (c-c \sin[e+fx])^{3/2}} dx$$

Optimal (type 3, 224 leaves, 7 steps):

$$\frac{(7A+3B) \operatorname{ArcTanh}\left[\frac{\sqrt{c} \cos[e+fx]}{\sqrt{2} \sqrt{c-c \sin[e+fx]}}\right]}{16 \sqrt{2} a^3 c^{3/2} f} + \frac{(7A+3B) \cos[e+fx]}{16 a^3 f (c-c \sin[e+fx])^{3/2}} - \frac{(7A+3B) \operatorname{Sec}[e+fx]}{12 a^3 c f \sqrt{c-c \sin[e+fx]}} - \frac{(7A+3B) \operatorname{Sec}[e+fx]^3 \sqrt{c-c \sin[e+fx]}}{30 a^3 c^2 f} - \frac{(A-B) \operatorname{Sec}[e+fx]^5 (c-c \sin[e+fx])^{3/2}}{5 a^3 c^3 f}$$

Result (type 3, 357 leaves):

$$\begin{aligned}
 & \frac{1}{240 a^3 f (1 + \sin[e + f x])^3 (c - c \sin[e + f x])^{3/2}} \\
 & \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right) \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right) \\
 & \left( -40 A \cos[e + f x]^2 + 24 (-A + B) \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right)^2 - \right. \\
 & \quad \left. 30 (3 A + B) \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right)^2 \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right)^4 + \right. \\
 & \quad \left. 15 (A + B) \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right) \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right)^5 - \right. \\
 & \quad \left. (15 + 15 i) (-1)^{1/4} (7 A + 3 B) \operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{1/4} \left(1 + \tan\left[\frac{1}{4}(e + f x)\right]\right)\right] \right. \\
 & \quad \left. \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right)^2 \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right)^5 + \right. \\
 & \quad \left. 30 (A + B) \sin\left[\frac{1}{2}(e + f x)\right] \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right)^5 \right)
 \end{aligned}$$

**Problem 130: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A + B \sin[e + f x]}{(a + a \sin[e + f x])^3 (c - c \sin[e + f x])^{5/2}} dx$$

Optimal (type 3, 258 leaves, 8 steps):

$$\begin{aligned}
 & \frac{7 (9 A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{c} \cos[e + f x]}{\sqrt{2} \sqrt{c - c \sin[e + f x]}}\right]}{128 \sqrt{2} a^3 c^{5/2} f} + \frac{7 (9 A + B) \cos[e + f x]}{128 a^3 c f (c - c \sin[e + f x])^{3/2}} + \\
 & \frac{7 (9 A + B) \sec[e + f x]}{240 a^3 c f (c - c \sin[e + f x])^{3/2}} - \frac{7 (9 A + B) \sec[e + f x]}{96 a^3 c^2 f \sqrt{c - c \sin[e + f x]}} - \\
 & \frac{(9 A + B) \sec[e + f x]^3}{30 a^3 c^2 f \sqrt{c - c \sin[e + f x]}} - \frac{(A - B) \sec[e + f x]^5 \sqrt{c - c \sin[e + f x]}}{5 a^3 c^3 f}
 \end{aligned}$$

Result (type 3, 479 leaves):

$$\frac{1}{1920 a^3 f (1 + \sin [e + f x])^3 (c - c \sin [e + f x])^{5/2}} \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) \left( -720 A \cos [e + f x]^4 + 96 (-A + B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^4 + 80 (-3 A + B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^4 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 + 60 (A + B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^5 + 15 (15 A + 7 B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^3 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^5 - (105 + 105 i) (-1)^{1/4} (9 A + B) \operatorname{ArcTan} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{1/4} \left( 1 + \tan \left[ \frac{1}{4} (e + f x) \right] \right) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^4 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^5 + 120 (A + B) \sin \left[ \frac{1}{2} (e + f x) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^5 + 30 (15 A + 7 B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 \sin \left[ \frac{1}{2} (e + f x) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^5 \right)$$

**Problem 135: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\sqrt{a + a \sin [e + f x]} (A + B \sin [e + f x])}{\sqrt{c - c \sin [e + f x]}} dx$$

Optimal (type 3, 100 leaves, 5 steps):

$$-\frac{a (A + B) \cos [e + f x] \operatorname{Log} [1 - \sin [e + f x]]}{f \sqrt{a + a \sin [e + f x]} \sqrt{c - c \sin [e + f x]}} + \frac{a B \cos [e + f x] \sqrt{c - c \sin [e + f x]}}{c f \sqrt{a + a \sin [e + f x]}}$$

Result (type 3, 133 leaves):

$$-\left( \left( \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) \sqrt{a (1 + \sin [e + f x])} \right. \right. \\ \left. \left. (2 i (A + B) \operatorname{ArcTan} [e^{i (e + f x)}] + (A + B) (-i f x + \operatorname{Log} [1 + e^{2 i (e + f x)}]) + B \sin [e + f x]) \right) \right) / \\ \left( f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) \sqrt{c - c \sin [e + f x]} \right)$$

**Problem 136: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\sqrt{a + a \sin [e + f x]} (A + B \sin [e + f x])}{(c - c \sin [e + f x])^{3/2}} dx$$



Optimal (type 3, 99 leaves, 5 steps):

$$\frac{a (A+B) \cos [e+f x]}{f \sqrt{a+a \sin [e+f x]} (c-c \sin [e+f x])^{3/2}} + \frac{a B \cos [e+f x] \operatorname{Log}[1-\sin [e+f x]]}{c f \sqrt{a+a \sin [e+f x]} \sqrt{c-c \sin [e+f x]}}$$

Result (type 3, 177 leaves):

$$\left( \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right) \sqrt{a (1+\sin [e+f x])} (-A-B+i B f x - B \operatorname{Log}[1+e^{2 i (e+f x)}]) + \right. \\ \left. 2 i B \operatorname{ArcTan}\left[e^{i (e+f x)}\right] (-1+\sin [e+f x]) + B (-i f x + \operatorname{Log}[1+e^{2 i (e+f x)}]) \sin [e+f x] \right) / \\ \left( c f \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right) (-1+\sin [e+f x]) \sqrt{c-c \sin [e+f x]} \right)$$

**Problem 158: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a+a \sin [e+f x])^{5/2} (A+B \sin [e+f x])}{(c-c \sin [e+f x])^{11/2}} dx$$

Optimal (type 3, 146 leaves, 3 steps):

$$\frac{(A+B) \cos [e+f x] (a+a \sin [e+f x])^{5/2}}{10 f (c-c \sin [e+f x])^{11/2}} + \\ \frac{(A-4 B) \cos [e+f x] (a+a \sin [e+f x])^{5/2}}{40 c f (c-c \sin [e+f x])^{9/2}} + \frac{(A-4 B) \cos [e+f x] (a+a \sin [e+f x])^{5/2}}{240 c^2 f (c-c \sin [e+f x])^{7/2}}$$

Result (type 3, 348 leaves):

$$\left( 4 (A+B) \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right) (a (1+\sin [e+f x]))^{5/2} \right) / \\ \left( 5 f \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right)^5 (c-c \sin [e+f x])^{11/2} \right) + \\ \left( (-A-2 B) \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right)^3 (a (1+\sin [e+f x]))^{5/2} \right) / \\ \left( f \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right)^5 (c-c \sin [e+f x])^{11/2} \right) + \\ \left( (A+5 B) \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right)^5 (a (1+\sin [e+f x]))^{5/2} \right) / \\ \left( 3 f \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right)^5 (c-c \sin [e+f x])^{11/2} \right) - \\ \frac{B \left( \cos \left[ \frac{1}{2} (e+f x) \right] - \sin \left[ \frac{1}{2} (e+f x) \right] \right)^7 (a (1+\sin [e+f x]))^{5/2}}{2 f \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right)^5 (c-c \sin [e+f x])^{11/2}}$$

### Problem 160: Result more than twice size of optimal antiderivative.

$$\int (a + a \sin[e + f x])^{7/2} (A + B \sin[e + f x]) (c - c \sin[e + f x])^{9/2} dx$$

Optimal (type 3, 250 leaves, 5 steps):

$$\begin{aligned} & - \frac{a^4 (9A - B) \cos[e + f x] (c - c \sin[e + f x])^{9/2}}{315 f \sqrt{a + a \sin[e + f x]}} - \\ & \frac{a^3 (9A - B) \cos[e + f x] \sqrt{a + a \sin[e + f x]} (c - c \sin[e + f x])^{9/2}}{126 f} - \\ & \frac{a^2 (9A - B) \cos[e + f x] (a + a \sin[e + f x])^{3/2} (c - c \sin[e + f x])^{9/2}}{84 f} - \\ & \frac{a (9A - B) \cos[e + f x] (a + a \sin[e + f x])^{5/2} (c - c \sin[e + f x])^{9/2}}{72 f} - \\ & \frac{B \cos[e + f x] (a + a \sin[e + f x])^{7/2} (c - c \sin[e + f x])^{9/2}}{9 f} \end{aligned}$$

Result (type 3, 870 leaves):

$$\begin{aligned}
 & \left( 7 (A - B) \cos [2 (e + f x)] (a (1 + \sin [e + f x]))^{7/2} (c - c \sin [e + f x])^{9/2} \right) / \\
 & \left( 128 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^7 \right) + \\
 & \left( 7 (A - B) \cos [4 (e + f x)] (a (1 + \sin [e + f x]))^{7/2} (c - c \sin [e + f x])^{9/2} \right) / \\
 & \left( 256 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^7 \right) + \\
 & \left( (A - B) \cos [6 (e + f x)] (a (1 + \sin [e + f x]))^{7/2} (c - c \sin [e + f x])^{9/2} \right) / \\
 & \left( 128 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^7 \right) + \\
 & \left( (A - B) \cos [8 (e + f x)] (a (1 + \sin [e + f x]))^{7/2} (c - c \sin [e + f x])^{9/2} \right) / \\
 & \left( 1024 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^7 \right) + \\
 & \left( 7 (10 A - B) \sin [e + f x] (a (1 + \sin [e + f x]))^{7/2} (c - c \sin [e + f x])^{9/2} \right) / \\
 & \left( 128 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^7 \right) + \\
 & \left( 7 A (a (1 + \sin [e + f x]))^{7/2} (c - c \sin [e + f x])^{9/2} \sin [3 (e + f x)] \right) / \\
 & \left( 64 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^7 \right) + \\
 & \left( (7 A + 2 B) (a (1 + \sin [e + f x]))^{7/2} (c - c \sin [e + f x])^{9/2} \sin [5 (e + f x)] \right) / \\
 & \left( 320 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^7 \right) + \\
 & \left( (4 A + 5 B) (a (1 + \sin [e + f x]))^{7/2} (c - c \sin [e + f x])^{9/2} \sin [7 (e + f x)] \right) / \\
 & \left( 1792 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^7 \right) + \\
 & \left( B (a (1 + \sin [e + f x]))^{7/2} (c - c \sin [e + f x])^{9/2} \sin [9 (e + f x)] \right) / \\
 & \left( 2304 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^9 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^7 \right)
 \end{aligned}$$

### Problem 170: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sin [e + f x])^{7/2} (A + B \sin [e + f x])}{(c - c \sin [e + f x])^{11/2}} dx$$

Optimal (type 3, 96 leaves, 2 steps):

$$\frac{(A + B) \cos [e + f x] (a + a \sin [e + f x])^{7/2}}{10 f (c - c \sin [e + f x])^{11/2}} + \frac{(A - 9 B) \cos [e + f x] (a + a \sin [e + f x])^{7/2}}{80 c f (c - c \sin [e + f x])^{9/2}}$$

Result (type 3, 434 leaves):

$$\begin{aligned}
& \left( 8 (A+B) \left( \cos \left[ \frac{1}{2} (e+fx) \right] - \sin \left[ \frac{1}{2} (e+fx) \right] \right) (a(1+\sin[e+fx]))^{7/2} \right) / \\
& \left( 5f \left( \cos \left[ \frac{1}{2} (e+fx) \right] + \sin \left[ \frac{1}{2} (e+fx) \right] \right)^7 (c-c \sin[e+fx])^{11/2} \right) + \\
& \left( (-3A-5B) \left( \cos \left[ \frac{1}{2} (e+fx) \right] - \sin \left[ \frac{1}{2} (e+fx) \right] \right)^3 (a(1+\sin[e+fx]))^{7/2} \right) / \\
& \left( f \left( \cos \left[ \frac{1}{2} (e+fx) \right] + \sin \left[ \frac{1}{2} (e+fx) \right] \right)^7 (c-c \sin[e+fx])^{11/2} \right) + \\
& \left( 2(A+3B) \left( \cos \left[ \frac{1}{2} (e+fx) \right] - \sin \left[ \frac{1}{2} (e+fx) \right] \right)^5 (a(1+\sin[e+fx]))^{7/2} \right) / \\
& \left( f \left( \cos \left[ \frac{1}{2} (e+fx) \right] + \sin \left[ \frac{1}{2} (e+fx) \right] \right)^7 (c-c \sin[e+fx])^{11/2} \right) + \\
& \left( (-A-7B) \left( \cos \left[ \frac{1}{2} (e+fx) \right] - \sin \left[ \frac{1}{2} (e+fx) \right] \right)^7 (a(1+\sin[e+fx]))^{7/2} \right) / \\
& \left( 2f \left( \cos \left[ \frac{1}{2} (e+fx) \right] + \sin \left[ \frac{1}{2} (e+fx) \right] \right)^7 (c-c \sin[e+fx])^{11/2} \right) + \\
& \frac{B \left( \cos \left[ \frac{1}{2} (e+fx) \right] - \sin \left[ \frac{1}{2} (e+fx) \right] \right)^9 (a(1+\sin[e+fx]))^{7/2}}{f \left( \cos \left[ \frac{1}{2} (e+fx) \right] + \sin \left[ \frac{1}{2} (e+fx) \right] \right)^7 (c-c \sin[e+fx])^{11/2}}
\end{aligned}$$

**Problem 171: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a+a \sin[e+fx])^{7/2} (A+B \sin[e+fx])}{(c-c \sin[e+fx])^{13/2}} dx$$

Optimal (type 3, 146 leaves, 3 steps):

$$\begin{aligned}
& \frac{(A+B) \cos[e+fx] (a+a \sin[e+fx])^{7/2}}{12f(c-c \sin[e+fx])^{13/2}} + \\
& \frac{(A-5B) \cos[e+fx] (a+a \sin[e+fx])^{7/2}}{60cf(c-c \sin[e+fx])^{11/2}} + \frac{(A-5B) \cos[e+fx] (a+a \sin[e+fx])^{7/2}}{480c^2f(c-c \sin[e+fx])^{9/2}}
\end{aligned}$$

Result (type 3, 442 leaves):

$$\begin{aligned}
 & \left( 4 (A+B) \left( \cos \left[ \frac{1}{2} (e+fx) \right] - \sin \left[ \frac{1}{2} (e+fx) \right] \right) (a(1+\sin[e+fx]))^{7/2} \right) / \\
 & \left( 3f \left( \cos \left[ \frac{1}{2} (e+fx) \right] + \sin \left[ \frac{1}{2} (e+fx) \right] \right)^7 (c-c \sin[e+fx])^{13/2} \right) - \\
 & \left( 4 (3A+5B) \left( \cos \left[ \frac{1}{2} (e+fx) \right] - \sin \left[ \frac{1}{2} (e+fx) \right] \right)^3 (a(1+\sin[e+fx]))^{7/2} \right) / \\
 & \left( 5f \left( \cos \left[ \frac{1}{2} (e+fx) \right] + \sin \left[ \frac{1}{2} (e+fx) \right] \right)^7 (c-c \sin[e+fx])^{13/2} \right) + \\
 & \left( 3 (A+3B) \left( \cos \left[ \frac{1}{2} (e+fx) \right] - \sin \left[ \frac{1}{2} (e+fx) \right] \right)^5 (a(1+\sin[e+fx]))^{7/2} \right) / \\
 & \left( 2f \left( \cos \left[ \frac{1}{2} (e+fx) \right] + \sin \left[ \frac{1}{2} (e+fx) \right] \right)^7 (c-c \sin[e+fx])^{13/2} \right) + \\
 & \left( (-A-7B) \left( \cos \left[ \frac{1}{2} (e+fx) \right] - \sin \left[ \frac{1}{2} (e+fx) \right] \right)^7 (a(1+\sin[e+fx]))^{7/2} \right) / \\
 & \left( 3f \left( \cos \left[ \frac{1}{2} (e+fx) \right] + \sin \left[ \frac{1}{2} (e+fx) \right] \right)^7 (c-c \sin[e+fx])^{13/2} \right) + \\
 & \frac{B \left( \cos \left[ \frac{1}{2} (e+fx) \right] - \sin \left[ \frac{1}{2} (e+fx) \right] \right)^9 (a(1+\sin[e+fx]))^{7/2}}{2f \left( \cos \left[ \frac{1}{2} (e+fx) \right] + \sin \left[ \frac{1}{2} (e+fx) \right] \right)^7 (c-c \sin[e+fx])^{13/2}}
 \end{aligned}$$

**Problem 172: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a+a \sin[e+fx])^{7/2} (A+B \sin[e+fx])}{(c-c \sin[e+fx])^{15/2}} dx$$

Optimal (type 3, 202 leaves, 4 steps):

$$\begin{aligned}
 & \frac{(A+B) \cos[e+fx] (a+a \sin[e+fx])^{7/2}}{14f (c-c \sin[e+fx])^{15/2}} + \frac{(3A-11B) \cos[e+fx] (a+a \sin[e+fx])^{7/2}}{168cf (c-c \sin[e+fx])^{13/2}} + \\
 & \frac{(3A-11B) \cos[e+fx] (a+a \sin[e+fx])^{7/2}}{840c^2f (c-c \sin[e+fx])^{11/2}} + \frac{(3A-11B) \cos[e+fx] (a+a \sin[e+fx])^{7/2}}{6720c^3f (c-c \sin[e+fx])^{9/2}}
 \end{aligned}$$

Result (type 3, 442 leaves):

$$\begin{aligned}
& \left( 8 (A+B) \left( \cos \left[ \frac{1}{2} (e+fx) \right] - \sin \left[ \frac{1}{2} (e+fx) \right] \right) (a(1+\sin[e+fx]))^{7/2} \right) / \\
& \left( 7f \left( \cos \left[ \frac{1}{2} (e+fx) \right] + \sin \left[ \frac{1}{2} (e+fx) \right] \right)^7 (c-c\sin[e+fx])^{15/2} \right) - \\
& \left( 2(3A+5B) \left( \cos \left[ \frac{1}{2} (e+fx) \right] - \sin \left[ \frac{1}{2} (e+fx) \right] \right)^3 (a(1+\sin[e+fx]))^{7/2} \right) / \\
& \left( 3f \left( \cos \left[ \frac{1}{2} (e+fx) \right] + \sin \left[ \frac{1}{2} (e+fx) \right] \right)^7 (c-c\sin[e+fx])^{15/2} \right) + \\
& \left( 6(A+3B) \left( \cos \left[ \frac{1}{2} (e+fx) \right] - \sin \left[ \frac{1}{2} (e+fx) \right] \right)^5 (a(1+\sin[e+fx]))^{7/2} \right) / \\
& \left( 5f \left( \cos \left[ \frac{1}{2} (e+fx) \right] + \sin \left[ \frac{1}{2} (e+fx) \right] \right)^7 (c-c\sin[e+fx])^{15/2} \right) + \\
& \left( (-A-7B) \left( \cos \left[ \frac{1}{2} (e+fx) \right] - \sin \left[ \frac{1}{2} (e+fx) \right] \right)^7 (a(1+\sin[e+fx]))^{7/2} \right) / \\
& \left( 4f \left( \cos \left[ \frac{1}{2} (e+fx) \right] + \sin \left[ \frac{1}{2} (e+fx) \right] \right)^7 (c-c\sin[e+fx])^{15/2} \right) + \\
& \frac{B \left( \cos \left[ \frac{1}{2} (e+fx) \right] - \sin \left[ \frac{1}{2} (e+fx) \right] \right)^9 (a(1+\sin[e+fx]))^{7/2}}{3f \left( \cos \left[ \frac{1}{2} (e+fx) \right] + \sin \left[ \frac{1}{2} (e+fx) \right] \right)^7 (c-c\sin[e+fx])^{15/2}}
\end{aligned}$$

**Problem 176: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(A+B \sin[e+fx]) \sqrt{c-c \sin[e+fx]}}{\sqrt{a+a \sin[e+fx]}} dx$$

Optimal (type 3, 96 leaves, 5 steps):

$$\frac{(A-B) c \cos[e+fx] \operatorname{Log}[1+\sin[e+fx]]}{f \sqrt{a+a \sin[e+fx]} \sqrt{c-c \sin[e+fx]}} - \frac{B \cos[e+fx] \sqrt{c-c \sin[e+fx]}}{f \sqrt{a+a \sin[e+fx]}}$$

Result (type 3, 136 leaves):

$$\left( \left( \cos \left[ \frac{1}{2} (e+fx) \right] + \sin \left[ \frac{1}{2} (e+fx) \right] \right) \left( -2i(A-B) \operatorname{ArcTan}[e^{i(e+fx)}] + (A-B) (-i f x + \operatorname{Log}[1+e^{2i(e+fx)}]) + B \sin[e+fx] \right) \sqrt{c-c \sin[e+fx]} \right) / \left( f \left( \cos \left[ \frac{1}{2} (e+fx) \right] - \sin \left[ \frac{1}{2} (e+fx) \right] \right) \sqrt{a(1+\sin[e+fx])} \right)$$

**Problem 183: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(A+B \sin[e+fx]) \sqrt{c-c \sin[e+fx]}}{(a+a \sin[e+fx])^{3/2}} dx$$

Optimal (type 3, 100 leaves, 5 steps):

$$-\frac{(A-B) c \cos[e+fx]}{f (a+a \sin[e+fx])^{3/2} \sqrt{c-c \sin[e+fx]}} + \frac{B c \cos[e+fx] \operatorname{Log}[1+\sin[e+fx]]}{a f \sqrt{a+a \sin[e+fx]} \sqrt{c-c \sin[e+fx]}}$$

Result (type 3, 161 leaves):

$$\left( \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) \sqrt{c - c \sin[e + f x]} (-A + B - i B f x + B \log[1 + e^{2i(e+fx)}] + B(-i f x + \log[1 + e^{2i(e+fx)}]) \sin[e + f x] - 2i B \operatorname{ArcTan}[e^{i(e+fx)}] (1 + \sin[e + f x])) \right) / \left( f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right) (a (1 + \sin[e + f x]))^{3/2} \right)$$

**Problem 195: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int (a + a \sin[e + f x])^m (A + B \sin[e + f x]) (c - c \sin[e + f x])^n dx$$

Optimal (type 5, 174 leaves, 5 steps):

$$\left( 2^{\frac{1}{2}+n} c (B(m-n) + A(1+m+n)) \cos[e + f x] \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}(1+2m), \frac{1}{2}(1-2n), \frac{1}{2}(3+2m), \frac{1}{2}(1+\sin[e + f x]) \right] (1 - \sin[e + f x])^{\frac{1}{2}-n} (a + a \sin[e + f x])^m (c - c \sin[e + f x])^{-1+n} \right) / \left( f (1+2m) (1+m+n) - \frac{B \cos[e + f x] (a + a \sin[e + f x])^m (c - c \sin[e + f x])^n}{f (1+m+n)} \right)$$

Result (type 6, 15882 leaves):

$$\begin{aligned} & - \left( \left( 4^{1+n} (3+2n) \cos \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{-2m} \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{-2n} (a + a \sin[e + f x])^m \right. \right. \\ & \quad (c - c \sin[e + f x])^n \left( A \cos \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{2m} \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{2n} + \right. \\ & \quad \left. \left. B \cos \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{2m} \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{2n} \sin[e + f x] \right) \right. \\ & \quad \left. \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \left( \frac{\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]}{1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{2n} \left( \frac{1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{2m} \right. \\ & \quad \left( - \left( \left( A \operatorname{AppellF1} \left[ \frac{1}{2} + n, -2m, 1 + 2(m+n), \frac{3}{2} + n, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \right. \\ & \quad \left. \left. \left. - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \left( 1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^2 \right) / \right. \\ & \quad \left( - (3+2n) \operatorname{AppellF1} \left[ \frac{1}{2} + n, -2m, 1 + 2(m+n), \frac{3}{2} + n, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\ & \quad \left. \left. - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \left( 2m \operatorname{AppellF1} \left[ \frac{3}{2} + n, 1 - 2m, 1 + 2(m+n), \right. \right. \right. \\ & \quad \left. \left. \left. \frac{5}{2} + n, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + (1 + 2m + 2n) \right. \right. \end{aligned}$$

$$\begin{aligned}
& \text{AppellF1}\left[\frac{3}{2}+n, -2m, 2(1+m+n), \frac{5}{2}+n, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
& \quad \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2) - \\
& \left( \text{B AppellF1}\left[\frac{1}{2}+n, -2m, 1+2(m+n), \frac{3}{2}+n, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \left(1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^2 \right) / \left( -(3+2n) \text{AppellF1}\left[\frac{1}{2}+n, \right. \right. \\
& \quad \left. \left. -2m, 1+2(m+n), \frac{3}{2}+n, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\
& \quad \left. 2 \left( 2m \text{AppellF1}\left[\frac{3}{2}+n, 1-2m, 1+2(m+n), \frac{5}{2}+n, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (1+2m+2n) \text{AppellF1}\left[\frac{3}{2}+n, -2m, 2(1+m+n), \frac{5}{2}+ \right. \right. \\
& \quad \left. \left. n, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) + \right. \\
& \quad \left. \left( 8 \text{B AppellF1}\left[\frac{1}{2}+n, -2m, 3+2(m+n), \frac{3}{2}+n, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) / \left( (3+2n) \text{AppellF1}\left[\frac{1}{2}+n, -2m, \right. \right. \\
& \quad \left. \left. 3+2(m+n), \frac{3}{2}+n, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \right. \\
& \quad \left. 2 \left( 2m \text{AppellF1}\left[\frac{3}{2}+n, 1-2m, 3+2(m+n), \frac{5}{2}+n, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (3+2m+2n) \text{AppellF1}\left[\frac{3}{2}+n, -2m, 2(2+m+n), \frac{5}{2}+ \right. \right. \\
& \quad \left. \left. n, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) + \right. \\
& \quad \left. \left( 8 \text{B AppellF1}\left[\frac{1}{2}+n, -2m, 2(1+m+n), \frac{3}{2}+n, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \left(1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) \right) / \right. \\
& \quad \left. \left( -(3+2n) \text{AppellF1}\left[\frac{1}{2}+n, -2m, 2(1+m+n), \frac{3}{2}+n, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\
& \quad \left. 4 \left( m \text{AppellF1}\left[\frac{3}{2}+n, 1-2m, 2(1+m+n), \frac{5}{2}+n, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (1+m+n) \text{AppellF1}\left[\frac{3}{2}+n, -2m, 3+2(m+n), \frac{5}{2}+n, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \right) \Bigg) / \\
& \left( f(1+2n) \left(1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^3 \left( -\frac{1}{(1+2n) \left(1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^4} \right. \right.
\end{aligned}$$



$$\begin{aligned}
 & 3 \times 2^{1+2n} (3+2n) \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \\
 & \left(\frac{\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}\right)^{2n} \left(\frac{1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}\right)^{2m} \\
 & \left(-\left(\left(\operatorname{AppellF1}\left[\frac{1}{2}+n, -2m, 1+2(m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right.\right.\right.\right. \right. \\
 & \quad \left.\left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^2\right)\right)\right) / \\
 & \left(-\left(3+2n\right) \operatorname{AppellF1}\left[\frac{1}{2}+n, -2m, 1+2(m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right.\right.\right. \\
 & \quad \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right)+2\left(2m \operatorname{AppellF1}\left[\frac{3}{2}+n, 1-2m, 1+2(m+n), \right.\right.\right. \\
 & \quad \left.\left.\frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right)+\left(1+2m+2n\right) \\
 & \quad \operatorname{AppellF1}\left[\frac{3}{2}+n, -2m, 2(1+m+n), \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
 & \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) - \\
 & \left(\operatorname{B AppellF1}\left[\frac{1}{2}+n, -2m, 1+2(m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right.\right.\right. \\
 & \quad \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^2\right)\right) / \\
 & \left(-\left(3+2n\right) \operatorname{AppellF1}\left[\frac{1}{2}+n, -2m, 1+2(m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right.\right.\right. \\
 & \quad \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right)+2\left(2m \operatorname{AppellF1}\left[\frac{3}{2}+n, 1-2m, 1+2(m+n), \right.\right.\right. \\
 & \quad \left.\left.\frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right)+\left(1+2m+2n\right) \\
 & \quad \operatorname{AppellF1}\left[\frac{3}{2}+n, -2m, 2(1+m+n), \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
 & \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)+\left(8 \operatorname{B AppellF1}\left[\frac{1}{2}+n, \right.\right. \\
 & \quad \left.\left.-2m, 3+2(m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) / \\
 & \left(\left(3+2n\right) \operatorname{AppellF1}\left[\frac{1}{2}+n, -2m, 3+2(m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right.\right.\right. \\
 & \quad \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right)-2\left(2m \operatorname{AppellF1}\left[\frac{3}{2}+n, 1-2m, 3+2(m+n), \right.\right.\right. \\
 & \quad \left.\left.\frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right)+\left(3+2m+2n\right) \\
 & \quad \operatorname{AppellF1}\left[\frac{3}{2}+n, -2m, 2(2+m+n), \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
 & \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)+
 \end{aligned}$$

$$\begin{aligned}
& \left( 8 B \operatorname{AppellF1} \left[ \frac{1}{2} + n, -2 m, 2 (1 + m + n), \frac{3}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \left( 1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) / \\
& \left( - (3 + 2 n) \operatorname{AppellF1} \left[ \frac{1}{2} + n, -2 m, 2 (1 + m + n), \frac{3}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 4 \left( m \operatorname{AppellF1} \left[ \frac{3}{2} + n, 1 - 2 m, 2 (1 + m + n), \right. \right. \right. \\
& \quad \left. \left. \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \right. \\
& \quad \left. (1 + m + n) \operatorname{AppellF1} \left[ \frac{3}{2} + n, -2 m, 3 + 2 (m + n), \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \\
& \frac{1}{(1 + 2 n) \left( 1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^3} 4^n (3 + 2 n) \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \\
& \left( \frac{\operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]}{1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{2 n} \\
& \left( \frac{1 - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{2 m} \\
& \left( - \left( \left( A \operatorname{AppellF1} \left[ \frac{1}{2} + n, -2 m, 1 + 2 (m + n), \frac{3}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \left( 1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \right) / \\
& \left( - (3 + 2 n) \operatorname{AppellF1} \left[ \frac{1}{2} + n, -2 m, 1 + 2 (m + n), \frac{3}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \left( 2 m \operatorname{AppellF1} \left[ \frac{3}{2} + n, 1 - 2 m, 1 + 2 (m + n), \right. \right. \right. \\
& \quad \left. \left. \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (1 + 2 m + 2 n) \right. \\
& \quad \left. \operatorname{AppellF1} \left[ \frac{3}{2} + n, -2 m, 2 (1 + m + n), \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) - \\
& \left( B \operatorname{AppellF1} \left[ \frac{1}{2} + n, -2 m, 1 + 2 (m + n), \frac{3}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \left( 1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) / \\
& \left( - (3 + 2 n) \operatorname{AppellF1} \left[ \frac{1}{2} + n, -2 m, 1 + 2 (m + n), \frac{3}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \left( 2 m \operatorname{AppellF1} \left[ \frac{3}{2} + n, 1 - 2 m, 1 + 2 (m + n), \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 + (1 + 2m + 2n) \\
 & \operatorname{AppellF1}\left[\frac{3}{2} + n, -2m, 2(1 + m + n), \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \\
 & \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 + \\
 & \left(8 \operatorname{B AppellF1}\left[\frac{1}{2} + n, -2m, 3 + 2(m + n), \frac{3}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right]\right) / \\
 & \left( (3 + 2n) \operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 3 + 2(m + n), \frac{3}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] - 2 \left(2m \operatorname{AppellF1}\left[\frac{3}{2} + n, 1 - 2m, 3 + 2(m + n), \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (3 + 2m + 2n) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{3}{2} + n, -2m, 2(2 + m + n), \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right) + \\
 & \left(8 \operatorname{B AppellF1}\left[\frac{1}{2} + n, -2m, 2(1 + m + n), \frac{3}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \left(1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)\right) / \\
 & \left( -(3 + 2n) \operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 2(1 + m + n), \frac{3}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + 4 \left(m \operatorname{AppellF1}\left[\frac{3}{2} + n, 1 - 2m, 2(1 + m + n), \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \right. \\
 & \quad \left. (1 + m + n) \operatorname{AppellF1}\left[\frac{3}{2} + n, -2m, 3 + 2(m + n), \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right) + \\
 & \frac{1}{(1 + 2n) \left(1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^3} 2^{3+2n} n (3 + 2n) \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] \\
 & \left( \frac{\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]}{1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2} \right)^{-1+2n} \\
 & \left( \frac{1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2} \right)^{2m} \\
 & \left( -\frac{\operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{2 \left(1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^2} + \frac{\operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{4 \left(1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)} \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left( - (3+2n) \operatorname{AppellF1} \left[ \frac{1}{2} + n, -2m, 2(1+m+n), \frac{3}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] + 4 \left( m \operatorname{AppellF1} \left[ \frac{3}{2} + n, 1-2m, 2(1+m+n), \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, -\operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] + \right. \\
 & \quad \left. (1+m+n) \operatorname{AppellF1} \left[ \frac{3}{2} + n, -2m, 3+2(m+n), \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right) + \\
 & \frac{1}{(1+2n) \left( 1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right)^3} 2^{3+2n} m (3+2n) \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right] \\
 & \left( \frac{\operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]}{1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2} \right)^{2n} \\
 & \left( \frac{1 - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2}{1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2} \right)^{-1+2m} \\
 & \left( - \left( \left( \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right] \left( 1 - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right) \right) \right) / \right. \\
 & \quad \left. \left( 2 \left( 1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right)^2 \right) - \frac{\operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]}{2 \left( 1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right)} \right) \\
 & \left( - \left( \left( \operatorname{A AppellF1} \left[ \frac{1}{2} + n, -2m, 1+2(m+n), \frac{3}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] \left( 1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right)^2 \right) \right) / \right. \\
 & \quad \left( - (3+2n) \operatorname{AppellF1} \left[ \frac{1}{2} + n, -2m, 1+2(m+n), \frac{3}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] + 2 \left( 2m \operatorname{AppellF1} \left[ \frac{3}{2} + n, 1-2m, 1+2(m+n), \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, -\operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] + (1+2m+2n) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[ \frac{3}{2} + n, -2m, 2(1+m+n), \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right) - \\
 & \left( \operatorname{B AppellF1} \left[ \frac{1}{2} + n, -2m, 1+2(m+n), \frac{3}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] \left( 1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right)^2 \right) / \right. \\
 & \quad \left( - (3+2n) \operatorname{AppellF1} \left[ \frac{1}{2} + n, -2m, 1+2(m+n), \frac{3}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + 2\left(2m \operatorname{AppellF1}\left[\frac{3}{2} + n, 1 - 2m, 1 + 2(m+n), \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (1 + 2m + 2n)\right. \\
& \operatorname{AppellF1}\left[\frac{3}{2} + n, -2m, 2(1 + m + n), \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
& \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \\
& \left(8B \operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 3 + 2(m+n), \frac{3}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) / \\
& \left((3 + 2n) \operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 3 + 2(m+n), \frac{3}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - 2\left(2m \operatorname{AppellF1}\left[\frac{3}{2} + n, 1 - 2m, 3 + 2(m+n), \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (3 + 2m + 2n)\right. \right. \\
& \operatorname{AppellF1}\left[\frac{3}{2} + n, -2m, 2(2 + m + n), \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
& \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \\
& \left(8B \operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 2(1 + m + n), \frac{3}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) / \\
& \left(- (3 + 2n) \operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 2(1 + m + n), \frac{3}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + 4\left(m \operatorname{AppellF1}\left[\frac{3}{2} + n, 1 - 2m, 2(1 + m + n), \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (1 + m + n) \operatorname{AppellF1}\left[\frac{3}{2} + n, -2m, 3 + 2(m+n), \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \\
& \frac{1}{(1 + 2n) \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^3} 4^{1+n} (3 + 2n) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \\
& \left(\frac{\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}\right)^{2n} \\
& \left(\frac{1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}\right)^{2m}
\end{aligned}$$

$$\begin{aligned}
 & \left( - \left( \left( A \operatorname{AppellF1} \left[ \frac{1}{2} + n, -2m, 1 + 2(m+n), \frac{3}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \right]^2, \right. \right. \right. \\
 & \quad - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \\
 & \quad \left. \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \left( 1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \right) / \\
 & \left( - (3 + 2n) \operatorname{AppellF1} \left[ \frac{1}{2} + n, -2m, 1 + 2(m+n), \frac{3}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \right]^2, \right. \\
 & \quad - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + 2 \left( 2m \operatorname{AppellF1} \left[ \frac{3}{2} + n, 1 - 2m, 1 + 2(m+n), \right. \right. \\
 & \quad \left. \left. \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + (1 + 2m + 2n) \\
 & \quad \operatorname{AppellF1} \left[ \frac{3}{2} + n, -2m, 2(1 + m + n), \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \right]^2, \\
 & \quad \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) - \\
 & \left( B \operatorname{AppellF1} \left[ \frac{1}{2} + n, -2m, 1 + 2(m+n), \frac{3}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \right]^2, \right. \\
 & \quad - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \\
 & \quad \left. \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \left( 1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \right) / \\
 & \left( - (3 + 2n) \operatorname{AppellF1} \left[ \frac{1}{2} + n, -2m, 1 + 2(m+n), \frac{3}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \right]^2, \right. \\
 & \quad - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + 2 \left( 2m \operatorname{AppellF1} \left[ \frac{3}{2} + n, 1 - 2m, 1 + 2(m+n), \right. \right. \\
 & \quad \left. \left. \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + (1 + 2m + 2n) \\
 & \quad \operatorname{AppellF1} \left[ \frac{3}{2} + n, -2m, 2(1 + m + n), \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \right]^2, \\
 & \quad \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) - \\
 & \left( A \left( - \frac{1}{\frac{3}{2} + n} m \left( \frac{1}{2} + n \right) \operatorname{AppellF1} \left[ \frac{3}{2} + n, 1 - 2m, 1 + 2(m+n), \frac{5}{2} + n, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right. \\
 & \quad \left. \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] - \frac{1}{2 \left( \frac{3}{2} + n \right)} \left( \frac{1}{2} + n \right) (1 + 2(m+n)) \operatorname{AppellF1} \left[ \frac{3}{2} + n, \right. \right. \\
 & \quad \left. \left. -2m, 2 + 2(m+n), \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^2 \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( - (3 + 2 n) \operatorname{AppellF1} \left[ \frac{1}{2} + n, -2 m, 1 + 2 (m + n), \frac{3}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \left( 2 m \operatorname{AppellF1} \left[ \frac{3}{2} + n, 1 - 2 m, 1 + 2 (m + n), \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (1 + 2 m + 2 n) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[ \frac{3}{2} + n, -2 m, 2 (1 + m + n), \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) - \\
 & \left( B \left( - \frac{1}{\frac{3}{2} + n} m \left( \frac{1}{2} + n \right) \operatorname{AppellF1} \left[ \frac{3}{2} + n, 1 - 2 m, 1 + 2 (m + n), \frac{5}{2} + n, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right. \\
 & \quad \left. \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] - \frac{1}{2 \left( \frac{3}{2} + n \right)} \left( \frac{1}{2} + n \right) (1 + 2 (m + n)) \operatorname{AppellF1} \left[ \frac{3}{2} + n, \right. \right. \\
 & \quad \left. \left. -2 m, 2 + 2 (m + n), \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^2 \right) / \\
 & \left( - (3 + 2 n) \operatorname{AppellF1} \left[ \frac{1}{2} + n, -2 m, 1 + 2 (m + n), \frac{3}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \left( 2 m \operatorname{AppellF1} \left[ \frac{3}{2} + n, 1 - 2 m, 1 + 2 (m + n), \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (1 + 2 m + 2 n) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[ \frac{3}{2} + n, -2 m, 2 (1 + m + n), \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \\
 & \left( 8 B \left( - \frac{1}{\frac{3}{2} + n} m \left( \frac{1}{2} + n \right) \operatorname{AppellF1} \left[ \frac{3}{2} + n, 1 - 2 m, 3 + 2 (m + n), \frac{5}{2} + n, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right. \\
 & \quad \left. \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] - \frac{1}{2 \left( \frac{3}{2} + n \right)} \left( \frac{1}{2} + n \right) (3 + 2 (m + n)) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[ \frac{3}{2} + n, -2 m, 4 + 2 (m + n), \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \right) \right) /
 \end{aligned}$$



$$\begin{aligned}
 & \left( (3+2n) \operatorname{AppellF1}\left[\frac{1}{2}+n, -2m, 3+2(m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - 2\left(2m \operatorname{AppellF1}\left[\frac{3}{2}+n, 1-2m, 3+2(m+n), \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (3+2m+2n) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}+n, -2m, 2(2+m+n), \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) + \\
 & \left(4B \operatorname{AppellF1}\left[\frac{1}{2}+n, -2m, 2(1+m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right) / \\
 & \left(- (3+2n) \operatorname{AppellF1}\left[\frac{1}{2}+n, -2m, 2(1+m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 4\left(m \operatorname{AppellF1}\left[\frac{3}{2}+n, 1-2m, 2(1+m+n), \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (1+m+n) \operatorname{AppellF1}\left[\frac{3}{2}+n, -2m, 3+2(m+n), \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) + \\
 & \left(8B \left(-\frac{1}{\frac{3}{2}+n} m \left(\frac{1}{2}+n\right) \operatorname{AppellF1}\left[\frac{3}{2}+n, 1-2m, 2(1+m+n), \frac{5}{2}+n, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \frac{1}{\frac{3}{2}+n} \left(\frac{1}{2}+n\right) (1+m+n) \operatorname{AppellF1}\left[\frac{3}{2}+n, -2m, \right. \right. \right. \\
 & \quad \left. \left. 1+2(1+m+n), \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right) \left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\right) / \\
 & \left(- (3+2n) \operatorname{AppellF1}\left[\frac{1}{2}+n, -2m, 2(1+m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 4\left(m \operatorname{AppellF1}\left[\frac{3}{2}+n, 1-2m, 2(1+m+n), \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (1+m+n) \operatorname{AppellF1}\left[\frac{3}{2}+n, -2m, 3+2(m+n), \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) -
 \end{aligned}$$

$$\begin{aligned}
& \left( 8 B \operatorname{AppellF1} \left[ \frac{1}{2} + n, -2 m, 2 (1 + m + n), \frac{3}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \left( 1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right. \\
& \quad \left( 2 \left( m \operatorname{AppellF1} \left[ \frac{3}{2} + n, 1 - 2 m, 2 (1 + m + n), \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (1 + m + n) \operatorname{AppellF1} \left[ \frac{3}{2} + n, -2 m, \right. \right. \\
& \quad \left. \left. 3 + 2 (m + n), \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \\
& \quad \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] - (3 + 2 n) \left( -\frac{1}{\frac{3}{2} + n} m \left( \frac{1}{2} + n \right) \right. \\
& \quad \left. \operatorname{AppellF1} \left[ \frac{3}{2} + n, 1 - 2 m, 2 (1 + m + n), \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \right) - \\
& \quad \frac{1}{\frac{3}{2} + n} \left( \frac{1}{2} + n \right) (1 + m + n) \operatorname{AppellF1} \left[ \frac{3}{2} + n, -2 m, 1 + 2 (1 + m + n), \right. \\
& \quad \left. \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \\
& \quad \left. \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \right) + 4 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \\
& \quad \left( m \left( -\frac{1}{\frac{5}{2} + n} \left( \frac{3}{2} + n \right) (1 + m + n) \operatorname{AppellF1} \left[ \frac{5}{2} + n, 1 - 2 m, 1 + 2 (1 + m + n), \right. \right. \right. \\
& \quad \left. \left. \frac{7}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \\
& \quad \left. \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] + \frac{1}{2 \left( \frac{5}{2} + n \right)} \right. \\
& \quad \left. (1 - 2 m) \left( \frac{3}{2} + n \right) \operatorname{AppellF1} \left[ \frac{5}{2} + n, 2 - 2 m, 2 (1 + m + n), \frac{7}{2} + n, \right. \right. \\
& \quad \left. \left. \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \\
& \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \right) \right) + \\
& \quad (1 + m + n) \left( -\frac{1}{\frac{5}{2} + n} m \left( \frac{3}{2} + n \right) \operatorname{AppellF1} \left[ \frac{5}{2} + n, 1 - 2 m, 3 + 2 (m + n), \right. \right. \\
& \quad \left. \left. \frac{7}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right)
\end{aligned}$$

$$\begin{aligned}
 & \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{2\left(\frac{5}{2} + n\right)} \\
 & \left(\frac{3}{2} + n\right) (3 + 2(m+n)) \operatorname{AppellF1}\left[\frac{5}{2} + n, -2m, 4 + 2(m+n), \right. \\
 & \left. \frac{7}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
 & \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right)\right) / \\
 & \left(- (3 + 2n) \operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 2(1+m+n), \frac{3}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 4\left(m \operatorname{AppellF1}\left[\frac{3}{2} + n, 1 - 2m, 2(1+m+n), \right. \right. \right. \right. \\
 & \left. \left. \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (1+m+n) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{3}{2} + n, -2m, 3 + 2(m+n), \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2 + \right. \\
 & \left. \left( A \operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 1 + 2(m+n), \frac{3}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2 \right. \right. \\
 & \left. \left. \left( \left( 2m \operatorname{AppellF1}\left[\frac{3}{2} + n, 1 - 2m, 1 + 2(m+n), \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (1 + 2m + 2n) \operatorname{AppellF1}\left[\frac{3}{2} + n, -2m, \right. \right. \right. \right. \\
 & \left. \left. \left. 2(1+m+n), \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right) \right. \\
 & \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - (3 + 2n) \left(-\frac{1}{\frac{3}{2} + n} m \left(\frac{1}{2} + n\right) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{3}{2} + n, 1 - 2m, 1 + 2(m+n), \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \right. \\
 & \left. \left. \frac{1}{2\left(\frac{3}{2} + n\right)} \left(\frac{1}{2} + n\right) (1 + 2(m+n)) \operatorname{AppellF1}\left[\frac{3}{2} + n, -2m, 2 + 2(m+n), \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right. \right. \\
 & \left. \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) + 2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
& \left( 2m \left( -\frac{1}{2 \left( \frac{5}{2} + n \right)} \left( \frac{3}{2} + n \right) (1 + 2(m+n)) \operatorname{AppellF1} \left[ \frac{5}{2} + n, 1 - 2m, 2 + \right. \right. \right. \\
& \quad \left. \left. \left. 2(m+n), \frac{7}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, -\operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right. \right. \\
& \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right] + \frac{1}{2 \left( \frac{5}{2} + n \right)} \right. \right. \\
& \quad \left. \left. (1 - 2m) \left( \frac{3}{2} + n \right) \operatorname{AppellF1} \left[ \frac{5}{2} + n, 2 - 2m, 1 + 2(m+n), \frac{7}{2} + n, \right. \right. \right. \\
& \quad \left. \left. \left. \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, -\operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right. \right. \\
& \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right] \right) \right) + \\
& \quad (1 + 2m + 2n) \left( -\frac{1}{\frac{5}{2} + n} m \left( \frac{3}{2} + n \right) \operatorname{AppellF1} \left[ \frac{5}{2} + n, 1 - 2m, 2(1+m+n), \right. \right. \\
& \quad \left. \left. \frac{7}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, -\operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right. \\
& \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right] - \frac{1}{\frac{5}{2} + n} \right. \right. \\
& \quad \left. \left. \left( \frac{3}{2} + n \right) (1+m+n) \operatorname{AppellF1} \left[ \frac{5}{2} + n, -2m, 1 + 2(1+m+n), \right. \right. \right. \\
& \quad \left. \left. \left. \frac{7}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, -\operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right. \right. \\
& \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right] \right) \right) \right) \Big/ \\
& \quad \left( -(3+2n) \operatorname{AppellF1} \left[ \frac{1}{2} + n, -2m, 1 + 2(m+n), \frac{3}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] + 2 \left( 2m \operatorname{AppellF1} \left[ \frac{3}{2} + n, 1 - 2m, 1 + 2(m+n), \right. \right. \right. \\
& \quad \left. \left. \left. \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, -\operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] + (1 + 2m + 2n) \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2} + n, -2m, 2(1+m+n), \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right)^2 + \\
& \quad \left( B \operatorname{AppellF1} \left[ \frac{1}{2} + n, -2m, 1 + 2(m+n), \frac{3}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right)^2
\end{aligned}$$

$$\begin{aligned}
 & \left( \left( 2 m \operatorname{AppellF1} \left[ \frac{3}{2} + n, 1 - 2 m, 1 + 2 (m + n), \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (1 + 2 m + 2 n) \operatorname{AppellF1} \left[ \frac{3}{2} + n, -2 m, \right. \right. \right. \\
 & \quad \left. \left. \left. 2 (1 + m + n), \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] - (3 + 2 n) \left( -\frac{1}{\frac{3}{2} + n} m \left( \frac{1}{2} + n \right) \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2} + n, 1 - 2 m, 1 + 2 (m + n), \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] - \right. \right. \right. \\
 & \quad \left. \left. \frac{1}{2 \left( \frac{3}{2} + n \right)} \left( \frac{1}{2} + n \right) (1 + 2 (m + n)) \operatorname{AppellF1} \left[ \frac{3}{2} + n, -2 m, 2 + 2 (m + n), \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \right. \\
 & \quad \left. \left. \left. \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \right) \right) + 2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right. \\
 & \quad \left( 2 m \left( -\frac{1}{2 \left( \frac{5}{2} + n \right)} \left( \frac{3}{2} + n \right) (1 + 2 (m + n)) \operatorname{AppellF1} \left[ \frac{5}{2} + n, 1 - 2 m, 2 + \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 2 (m + n), \frac{7}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \right. \\
 & \quad \left. \left. \left. \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] + \frac{1}{2 \left( \frac{5}{2} + n \right)} \right. \right. \right. \\
 & \quad \left. \left. \left. (1 - 2 m) \left( \frac{3}{2} + n \right) \operatorname{AppellF1} \left[ \frac{5}{2} + n, 2 - 2 m, 1 + 2 (m + n), \frac{7}{2} + n, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \right. \\
 & \quad \left. \left. \left. \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \right) \right) \right. \\
 & \quad \left. (1 + 2 m + 2 n) \left( -\frac{1}{\frac{5}{2} + n} m \left( \frac{3}{2} + n \right) \operatorname{AppellF1} \left[ \frac{5}{2} + n, 1 - 2 m, 2 (1 + m + n), \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{7}{2} + n, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \right. \\
 & \quad \left. \left. \left. \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] - \frac{1}{\frac{5}{2} + n} \right. \right. \right. \\
 & \quad \left. \left. \left. \left( \frac{3}{2} + n \right) (1 + m + n) \operatorname{AppellF1} \left[ \frac{5}{2} + n, -2 m, 1 + 2 (1 + m + n), \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \frac{7}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \\
& \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] \Bigg) \Bigg) \Bigg) \Bigg) \Bigg) / \\
& \left( -(3+2n) \operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 1+2(m+n), \frac{3}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, \right. \\
& \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + 2\left(2m \operatorname{AppellF1}\left[\frac{3}{2} + n, 1-2m, 1+2(m+n), \right. \right. \\
& \quad \left. \left. \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (1+2m+2n) \right. \\
& \quad \left. \operatorname{AppellF1}\left[\frac{3}{2} + n, -2m, 2(1+m+n), \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, \right. \\
& \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^2 - \\
& \left( 8B \operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 3+2(m+n), \frac{3}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, \right. \\
& \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right. \\
& \left( -\left(2m \operatorname{AppellF1}\left[\frac{3}{2} + n, 1-2m, 3+2(m+n), \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (3+2m+2n) \operatorname{AppellF1}\left[\frac{3}{2} + n, -2m, \right. \right. \\
& \quad \left. \left. 2(2+m+n), \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \\
& \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] + (3+2n) \left( -\frac{1}{\frac{3}{2} + n} m \left(\frac{1}{2} + n\right) \right. \\
& \quad \left. \operatorname{AppellF1}\left[\frac{3}{2} + n, 1-2m, 3+2(m+n), \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, \right. \\
& \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - \right. \\
& \quad \left. \frac{1}{2\left(\frac{3}{2} + n\right)} \left(\frac{1}{2} + n\right) (3+2(m+n)) \operatorname{AppellF1}\left[\frac{3}{2} + n, -2m, 4+2(m+n), \right. \right. \\
& \quad \left. \left. \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] \right) - 2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \\
& \left( 2m \left( -\frac{1}{2\left(\frac{5}{2} + n\right)} \left(\frac{3}{2} + n\right) (3+2(m+n)) \operatorname{AppellF1}\left[\frac{5}{2} + n, 1-2m, 4+ \right. \right. \right. \\
& \quad \left. \left. \left. 2(m+n), \frac{7}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right)
\end{aligned}$$

$$\begin{aligned}
 & \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{1}{2\left(\frac{5}{2} + n\right)} \\
 & (1 - 2m) \left(\frac{3}{2} + n\right) \text{AppellF1}\left[\frac{5}{2} + n, 2 - 2m, 3 + 2(m + n), \frac{7}{2} + n, \right. \\
 & \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
 & \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \Bigg) + \\
 & (3 + 2m + 2n) \left( -\frac{1}{\frac{5}{2} + n} m \left(\frac{3}{2} + n\right) \text{AppellF1}\left[\frac{5}{2} + n, 1 - 2m, 2(2 + m + n), \right. \right. \\
 & \left. \left. \frac{7}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{\frac{5}{2} + n} \right. \\
 & \left. \left(\frac{3}{2} + n\right) (2 + m + n) \text{AppellF1}\left[\frac{5}{2} + n, -2m, 1 + 2(2 + m + n), \right. \right. \\
 & \left. \left. \frac{7}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \left. \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right) \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \left( (3 + 2n) \text{AppellF1}\left[\frac{1}{2} + n, -2m, 3 + 2(m + n), \frac{3}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - 2 \left( 2m \text{AppellF1}\left[\frac{3}{2} + n, 1 - 2m, 3 + 2(m + n), \right. \right. \right. \\
 & \left. \left. \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (3 + 2m + 2n) \right. \right. \\
 & \left. \left. \text{AppellF1}\left[\frac{3}{2} + n, -2m, 2(2 + m + n), \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) \Bigg) \Bigg) \Bigg) \Bigg)
 \end{aligned}$$

**Problem 196: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int (a + a \sin[e + fx])^m (A + B \sin[e + fx]) (c - c \sin[e + fx])^3 dx$$

Optimal (type 5, 145 leaves, 5 steps):

$$\frac{1}{7 f (4+m)} 2^{\frac{1}{2}+m} a^4 c^3 (B (3-m) - A (4+m)) \operatorname{Cos}[e+f x]^7$$

$$\operatorname{Hypergeometric2F1}\left[\frac{7}{2}, \frac{1}{2}-m, \frac{9}{2}, \frac{1}{2}(1-\operatorname{Sin}[e+f x])\right] (1+\operatorname{Sin}[e+f x])^{\frac{1}{2}-m}$$

$$(a+a \operatorname{Sin}[e+f x])^{-4+m} - \frac{a^3 B c^3 \operatorname{Cos}[e+f x]^7 (a+a \operatorname{Sin}[e+f x])^{-3+m}}{f (4+m)}$$

Result (type 6, 31879 leaves): Display of huge result suppressed!

### Problem 197: Attempted integration timed out after 120 seconds.

$$\int (a+a \operatorname{Sin}[e+f x])^m (A+B \operatorname{Sin}[e+f x]) (c-c \operatorname{Sin}[e+f x])^2 dx$$

Optimal (type 5, 145 leaves, 5 steps):

$$\frac{1}{5 f (3+m)} 2^{\frac{1}{2}+m} a^3 c^2 (B (2-m) - A (3+m)) \operatorname{Cos}[e+f x]^5$$

$$\operatorname{Hypergeometric2F1}\left[\frac{5}{2}, \frac{1}{2}-m, \frac{7}{2}, \frac{1}{2}(1-\operatorname{Sin}[e+f x])\right] (1+\operatorname{Sin}[e+f x])^{\frac{1}{2}-m}$$

$$(a+a \operatorname{Sin}[e+f x])^{-3+m} - \frac{a^2 B c^2 \operatorname{Cos}[e+f x]^5 (a+a \operatorname{Sin}[e+f x])^{-2+m}}{f (3+m)}$$

Result (type 1, 1 leaves):

???

### Problem 198: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int (a+a \operatorname{Sin}[e+f x])^m (A+B \operatorname{Sin}[e+f x]) (c-c \operatorname{Sin}[e+f x]) dx$$

Optimal (type 5, 139 leaves, 5 steps):

$$\frac{1}{3 f (2+m)}$$

$$2^{\frac{1}{2}+m} a^2 c (B (1-m) - A (2+m)) \operatorname{Cos}[e+f x]^3 \operatorname{Hypergeometric2F1}\left[\frac{3}{2}, \frac{1}{2}-m, \frac{5}{2}, \frac{1}{2}(1-\operatorname{Sin}[e+f x])\right]$$

$$(1+\operatorname{Sin}[e+f x])^{\frac{1}{2}-m} (a+a \operatorname{Sin}[e+f x])^{-2+m} - \frac{a B c \operatorname{Cos}[e+f x]^3 (a+a \operatorname{Sin}[e+f x])^{-1+m}}{f (2+m)}$$

Result (type 5, 460 leaves):



$$\begin{aligned}
 & \frac{1}{f \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2} \\
 & i 4^{-1-m} c e^{i f m x} \left( 1 + i e^{-i (e+f x)} \right)^{-2m} \left( e^{-\frac{1}{4} i (2e+\pi+2fx)} \left( i + e^{i (e+f x)} \right) \right)^{2m} \\
 & \left( -\frac{1}{2+m} i B e^{-i (2e+f (2+m) x)} \text{Hypergeometric2F1}[-2-m, -2m, -1-m, -i e^{-i (e+f x)}] + \right. \\
 & \quad \frac{1}{1+m} 2 (-i A + B) e^{-i (e+f (1+m) x)} \text{Hypergeometric2F1}[-1-m, -2m, -m, -i e^{-i (e+f x)}] + \\
 & \quad \frac{1}{-1+m} 2 i A e^{i (e-f (-1+m) x)} \text{Hypergeometric2F1}[1-m, -2m, 2-m, -i e^{-i (e+f x)}] + \\
 & \quad \frac{1}{-1+m} 2 B e^{i (e-f (-1+m) x)} \text{Hypergeometric2F1}[1-m, -2m, 2-m, -i e^{-i (e+f x)}] + \\
 & \quad \left. \frac{1}{-2+m} i B e^{2i e - i f (-2+m) x} \text{Hypergeometric2F1}[2-m, -2m, 3-m, -i e^{-i (e+f x)}] + \right. \\
 & \quad \left. \frac{4 A e^{-i f m x} \text{Hypergeometric2F1}[-2m, -m, 1-m, -i e^{-i (e+f x)}]}{m} \right) \\
 & (-1 + \sin[e + f x]) (a (1 + \sin[e + f x]))^m \sin\left[\frac{1}{4} (2e + \pi + 2fx)\right]^{-2m}
 \end{aligned}$$

**Problem 199: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (a + a \sin[e + f x])^m (A + B \sin[e + f x]) dx$$

Optimal (type 5, 117 leaves, 3 steps):

$$\begin{aligned}
 & -\frac{B \cos[e + f x] (a + a \sin[e + f x])^m}{f (1+m)} - \frac{1}{f (1+m)} 2^{\frac{1}{2}+m} (A + A m + B m) \cos[e + f x] \\
 & \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{2} - m, \frac{3}{2}, \frac{1}{2} (1 - \sin[e + f x])\right] (1 + \sin[e + f x])^{-\frac{1}{2}-m} (a + a \sin[e + f x])^m
 \end{aligned}$$

Result (type 5, 295 leaves):

$$\begin{aligned}
 & -\frac{1}{f} (a (1 + \sin[e + f x]))^m \\
 & \left( \frac{1}{-1+m^2} 2^{-1-2m} B e^{-i (e+f x)} \left( 1 + i e^{-i (e+f x)} \right)^{-2m} \left( e^{-\frac{1}{4} i (2e+\pi+2fx)} \left( i + e^{i (e+f x)} \right) \right)^{2m} \right. \\
 & \quad \left( e^{2i (e+f x)} (-1+m) \text{Hypergeometric2F1}[-1-m, -2m, -m, -i e^{-i (e+f x)}] - \right. \\
 & \quad \left. (1+m) \text{Hypergeometric2F1}[1-m, -2m, 2-m, -i e^{-i (e+f x)}] \right) + \\
 & \quad \left( 2 \sqrt{2} A \cos\left[\frac{1}{4} (2e - \pi + 2fx)\right] \right)^{1+2m} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{2} + m, \frac{3}{2} + m, \right. \\
 & \quad \left. \sin\left[\frac{1}{4} (2e + \pi + 2fx)\right]^2 \sin\left[\frac{1}{4} (2e - \pi + 2fx)\right] \right) / \\
 & \quad \left( (1+2m) \sqrt{1 - \sin[e + f x]} \right) \sin\left[\frac{1}{4} (2e + \pi + 2fx)\right]^{-2m}
 \end{aligned}$$

**Problem 200: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sin[e + f x])^m (A + B \sin[e + f x])}{c - c \sin[e + f x]} dx$$

Optimal (type 5, 123 leaves, 5 steps):

$$\frac{1}{c f m} 2^{\frac{1}{2}+m} (B + A m + B m) \text{Hypergeometric2F1}\left[-\frac{1}{2}, \frac{1}{2} - m, \frac{1}{2}, \frac{1}{2} (1 - \sin[e + f x])\right] \text{Sec}[e + f x] \\ (1 + \sin[e + f x])^{\frac{1}{2}-m} (a + a \sin[e + f x])^m - \frac{B \text{Sec}[e + f x] (a + a \sin[e + f x])^{1+m}}{a c f m}$$

Result (type 6, 8388 leaves):

$$- \left( \left( \cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^{-2m} \cot\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right] \left( \cos\left[\frac{1}{2} (e + f x)\right] - \sin\left[\frac{1}{2} (e + f x)\right] \right)^2 \right. \right. \\ \left. \left( a + a \sin[e + f x] \right)^m \left( \frac{A \cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^{2m}}{\left( \cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] \right)^2} + \right. \\ \left. \frac{B \cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^{2m} \sin[e + f x]}{\left( \cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] \right)^2} \right) \\ \left( \frac{1 - \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2}{1 + \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2} \right)^{2m} \left( - \left( \left( (A + B) \text{AppellF1}\left[-\frac{1}{2}, -2m, 2m, \frac{1}{2}, \right. \right. \right. \right. \\ \left. \left. \left. \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right) \right) / \right. \\ \left. \left( \text{AppellF1}\left[-\frac{1}{2}, -2m, 2m, \frac{1}{2}, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right] - \right. \right. \\ \left. \left. 4m \left( \text{AppellF1}\left[\frac{1}{2}, 1 - 2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \right. \right. \\ \left. \left. \left. -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right] + \text{AppellF1}\left[\frac{1}{2}, -2m, 1 + 2m, \frac{3}{2}, \right. \right. \right. \right. \\ \left. \left. \left. \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right] \right) \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right) \right) + \\ \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \left( \left( 3 (A + B) \text{AppellF1}\left[\frac{1}{2}, -2m, 2m, \frac{3}{2}, \right. \right. \right. \right. \\ \left. \left. \left. \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right) \right) / \right. \\ \left. \left( 3 \text{AppellF1}\left[\frac{1}{2}, -2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right] - \right. \right. \\ \left. \left. 4m \left( \text{AppellF1}\left[\frac{3}{2}, 1 - 2m, 2m, \frac{5}{2}, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \right. \right. \right.$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \operatorname{AppellF1}\left[\frac{3}{2},-2 m, 1+2 m, \frac{5}{2},\right. \\
 & \left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)- \\
 & \left(8 B \operatorname{AppellF1}\left[\frac{1}{2},-2 m, 1+2 m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right] / \left(\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\left(\operatorname{AppellF1}\left[\frac{1}{2},-2 m,\right.\right.\right. \\
 & \left.\left.\left.1+2 m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]-\frac{2}{3}\left(2 m \operatorname{AppellF1}\left[\right.\right.\right. \right. \\
 & \left.\left.\left.\frac{3}{2}, 1-2 m, 1+2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \right.\right. \\
 & \left.\left.\left.(1+2 m) \operatorname{AppellF1}\left[\frac{3}{2},-2 m, 2+2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \right. \\
 & \left.\left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\right)\right)\right) / \\
 & \left(2 f(c-c \operatorname{Sin}[e+f x])\left(-\frac{1}{8} \operatorname{Csc}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\left(\frac{1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}\right)^{2 m}\right.\right. \\
 & \left.\left.-\left(\left((A+B) \operatorname{AppellF1}\left[-\frac{1}{2},-2 m, 2 m, \frac{1}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right.\right. \right. \\
 & \left.\left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\right) / \left(\operatorname{AppellF1}\left[-\frac{1}{2},-2 m, 2 m, \frac{1}{2},\right.\right.\right. \right. \\
 & \left.\left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)-4 m\left(\operatorname{AppellF1}\left[\frac{1}{2},\right.\right.\right. \right. \\
 & \left.\left.\left.\left.1-2 m, 2 m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \right.\right.\right. \\
 & \left.\left.\left.\operatorname{AppellF1}\left[\frac{1}{2},-2 m, 1+2 m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \right. \\
 & \left.\left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\right)\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+ \\
 & \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\left(\left(3(A+B) \operatorname{AppellF1}\left[\frac{1}{2},-2 m, 2 m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \right. \\
 & \left.\left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\right) / \left(3 \operatorname{AppellF1}\left[\frac{1}{2},-2 m, 2 m, \frac{3}{2},\right.\right.\right. \right. \\
 & \left.\left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)-4 m\left(\operatorname{AppellF1}\left[\frac{3}{2}, 1-2 m,\right.\right.\right. \right. \\
 & \left.\left.\left.\left.2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \operatorname{AppellF1}\left[\frac{3}{2},\right.\right.\right. \right. \\
 & \left.\left.\left.\left.-2 m, 1+2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\right)\right) \\
 & \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)-\left(8 B \operatorname{AppellF1}\left[\frac{1}{2},-2 m, 1+2 m, \frac{3}{2},\right.\right. \\
 & \left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \left( 1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \left( \text{AppellF1} \left[ \frac{1}{2}, -2 m, 1 + 2 m, \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] - \frac{2}{3} \left( 2 m \text{AppellF1} \left[ \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. 1 - 2 m, 1 + 2 m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right)^2 + \right. \\
 & \quad \left. (1 + 2 m) \text{AppellF1} \left[ \frac{3}{2}, -2 m, 2 + 2 m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) + \\
 & m \cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \left( \frac{1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{-1+2 m} \\
 & \left( - \left( \left( \sec \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \right) / \right. \\
 & \quad \left. \left( 2 \left( 1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^2 \right) \right) - \frac{\sec \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]}{2 \left( 1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)} \right) \\
 & \left( - \left( \left( (A + B) \text{AppellF1} \left[ -\frac{1}{2}, -2 m, 2 m, \frac{1}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) / \left( \text{AppellF1} \left[ -\frac{1}{2}, -2 m, 2 m, \frac{1}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] - 4 m \left( \text{AppellF1} \left[ \frac{1}{2}, \right. \right. \right. \\
 & \quad \left. \left. 1 - 2 m, 2 m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \right. \right. \\
 & \quad \left. \left. \text{AppellF1} \left[ \frac{1}{2}, -2 m, 1 + 2 m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \\
 & \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \left( \left( 3 (A + B) \text{AppellF1} \left[ \frac{1}{2}, -2 m, 2 m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) / \left( 3 \text{AppellF1} \left[ \frac{1}{2}, -2 m, 2 m, \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] - 4 m \left( \text{AppellF1} \left[ \frac{3}{2}, 1 - 2 m, \right. \right. \right. \\
 & \quad \left. \left. 2 m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \text{AppellF1} \left[ \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. -2 m, 1 + 2 m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \right) \\
 & \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 - \left( 8 B \text{AppellF1} \left[ \frac{1}{2}, -2 m, 1 + 2 m, \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \left( 1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \left( \text{AppellF1} \left[ \frac{1}{2}, -2m, 1+2m, \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] - \frac{2}{3} \left( 2m \text{AppellF1} \left[ \frac{3}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 1-2m, 1+2m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right)^2 + \right. \\
 & \quad \left. (1+2m) \text{AppellF1} \left[ \frac{3}{2}, -2m, 2+2m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) + \\
 & \frac{1}{2} \cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \left( \frac{1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{2m} \\
 & \left( - \left( (A+B) \left( m \text{AppellF1} \left[ \frac{1}{2}, 1-2m, 2m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \text{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] + \right. \right. \right. \\
 & \quad \left. \left. \left. m \text{AppellF1} \left[ \frac{1}{2}, -2m, 1+2m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \text{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \right) \right) \right) / \\
 & \left( \text{AppellF1} \left[ -\frac{1}{2}, -2m, 2m, \frac{1}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] - \right. \\
 & \quad \left. 4m \left( \text{AppellF1} \left[ \frac{1}{2}, 1-2m, 2m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \text{AppellF1} \left[ \frac{1}{2}, -2m, 1+2m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) + \\
 & \left( (A+B) \text{AppellF1} \left[ -\frac{1}{2}, -2m, 2m, \frac{1}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \\
 & \left( m \text{AppellF1} \left[ \frac{1}{2}, 1-2m, 2m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \\
 & \quad \text{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] + m \text{AppellF1} \left[ \frac{1}{2}, -2m, \right. \\
 & \quad \left. 1+2m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \\
 & \quad \text{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] - 2m \left( \text{AppellF1} \left[ \frac{1}{2}, 1-2m, \right. \right. \\
 & \quad \left. \left. 2m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \text{AppellF1} \left[ \frac{1}{2}, \right. \right. \\
 & \quad \left. \left. -2m, 1+2m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \\
 & \quad \text{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] - 4m \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2
 \end{aligned}$$

$$\begin{aligned}
 & \left( -\frac{2}{3} m \operatorname{AppellF1}\left[\frac{3}{2}, 1-2m, 1+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + \right. \\
 & \quad \frac{1}{6} (1-2m) \operatorname{AppellF1}\left[\frac{3}{2}, 2-2m, 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \right. \\
 & \quad \left. \frac{1}{6} (1+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2m, 2+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\
 & \quad \left. \left. \frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \Bigg/ \\
 & \left( \operatorname{AppellF1}\left[-\frac{1}{2}, -2m, 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \right. \\
 & \quad 4m \left( \operatorname{AppellF1}\left[\frac{1}{2}, 1-2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \operatorname{AppellF1}\left[\frac{1}{2}, -2m, 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. \left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right)^2 + \\
 & \quad \left. \frac{1}{2} \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \left( \left( 3(A+B) \operatorname{AppellF1}\left[\frac{1}{2}, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \right) \Bigg/ \right. \\
 & \quad \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \right. \\
 & \quad \left. 4m \left( \operatorname{AppellF1}\left[\frac{3}{2}, 1-2m, 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}, -2m, 1+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) - \right. \\
 & \quad \left. \left( 8B \operatorname{AppellF1}\left[\frac{1}{2}, -2m, 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \Bigg/ \left( \left( 1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \left( \operatorname{AppellF1}\left[\frac{1}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -2m, 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \right. \right. \\
 & \quad \left. \left. \frac{2}{3} \left( 2m \operatorname{AppellF1}\left[\frac{3}{2}, 1-2m, 1+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (1+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2m, \right. \right. \right. \\
 & \quad \left. \left. \left. 2+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \right) \right) \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \right) + \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2
 \end{aligned}$$



$$\begin{aligned}
 & -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Big) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Big) - \\
 & \left( 3 (A + B) \operatorname{AppellF1}\left[\frac{1}{2}, -2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \left(-2m \left(\operatorname{AppellF1}\left[\frac{3}{2}, 1-2m, 2m, \frac{5}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. -2m, 1+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right) \\
 & \quad \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + 3 \left(-\frac{1}{3} m \operatorname{AppellF1}\left[\right. \right. \\
 & \quad \left. \left. \frac{3}{2}, 1-2m, 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \\
 & \quad \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{3} m \operatorname{AppellF1}\left[\frac{3}{2}, \right. \\
 & \quad \left. -2m, 1+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
 & \quad \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \Big) - \\
 & \quad 4m \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(-\frac{6}{5} m \operatorname{AppellF1}\left[\frac{5}{2}, 1-2m, 1+2m, \right. \right. \\
 & \quad \left. \left. \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \\
 & \quad \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{3}{10} (1-2m) \operatorname{AppellF1}\left[\right. \\
 & \quad \left. \frac{5}{2}, 2-2m, 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \\
 & \quad \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{3}{10} (1+2m) \operatorname{AppellF1}\left[\right. \\
 & \quad \left. \frac{5}{2}, -2m, 2+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right) \Big) \Big) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \right. \\
 & \quad \left. 4m \left(\operatorname{AppellF1}\left[\frac{3}{2}, 1-2m, 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}, -2m, 1+2m, \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right) \\
 & \quad \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Big)^2 + \left( 8B \operatorname{AppellF1}\left[\frac{1}{2}, -2m, 1+2m, \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left( -\frac{1}{3} m \operatorname{AppellF1}\left[\frac{3}{2}, 1-2m, 1+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \right. \\
 & \quad \frac{1}{6} (1+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2m, 2+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \right. \\
 & \quad \frac{1}{3} \left( 2m \operatorname{AppellF1}\left[\frac{3}{2}, 1-2m, 1+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (1+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2m, \right. \right. \\
 & \quad \quad \left. \left. 2+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \\
 & \quad \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \frac{2}{3} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \\
 & \quad \left( 2m \left( -\frac{3}{10} (1+2m) \operatorname{AppellF1}\left[\frac{5}{2}, 1-2m, 2+2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \\
 & \quad \quad \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + \frac{3}{10} (1-2m) \operatorname{AppellF1}\left[\frac{5}{2}, 2-2m, \right. \right. \\
 & \quad \quad \left. \left. 1+2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \\
 & \quad \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) + (1+2m) \\
 & \quad \left( -\frac{3}{5} m \operatorname{AppellF1}\left[\frac{5}{2}, 1-2m, 2+2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \\
 & \quad \quad \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \frac{3}{10} (2+2m) \operatorname{AppellF1}\left[\frac{5}{2}, -2m, \right. \right. \\
 & \quad \quad \left. \left. 3+2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \right) \Big/ \\
 & \left( \left( 1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \left( \operatorname{AppellF1}\left[\frac{1}{2}, -2m, 1+2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \frac{2}{3} \left( 2m \operatorname{AppellF1}\left[\frac{3}{2}, 1- \right. \right. \right. \\
 & \quad \quad \left. \left. 2m, 1+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \right. \\
 & \quad \quad \left. \left. (1+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2m, 2+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right.
 \end{aligned}$$

$$-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2\right)\right)\right)\right)\right)$$

**Problem 201: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sin[e + fx])^m (A + B \sin[e + fx])}{(c - c \sin[e + fx])^2} dx$$

Optimal (type 5, 148 leaves, 5 steps):

$$\frac{1}{3 a c^2 f (1-m)} 2^{\frac{1}{2}+m} (A (1-m) - B (2+m)) \text{Hypergeometric2F1}\left[-\frac{3}{2}, \frac{1}{2}-m, -\frac{1}{2}, \frac{1}{2} (1-\sin[e+fx])\right] \\ \sec[e+fx]^3 (1+\sin[e+fx])^{\frac{1}{2}-m} (a+a \sin[e+fx])^{1+m} + \frac{B \sec[e+fx]^3 (a+a \sin[e+fx])^{2+m}}{a^2 c^2 f (1-m)}$$

Result (type 6, 15419 leaves):

$$-\left(\left(\cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]\right)^{-2m} \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^3 \left(\cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right]\right)^4\right. \\ \left. (a + a \sin[e + fx])^m \left(\frac{A \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^{2m}}{\left(\cos\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + fx\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + fx\right)\right]\right)^4} + \frac{B \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^{2m} \sin[e + fx]}{\left(\cos\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + fx\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + fx\right)\right]\right)^4}\right)\right) \\ \left(\frac{1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{2m}}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}\right) \left(-\left(\left((A+B) \text{AppellF1}\left[-\frac{3}{2}, -2m, 2m, -\frac{1}{2}, \right.\right.\right.\right. \\ \left.\left.\left.\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right) / \right. \\ \left. \left(\text{AppellF1}\left[-\frac{3}{2}, -2m, 2m, -\frac{1}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right.\right. \\ \left. 4m \left(\text{AppellF1}\left[-\frac{1}{2}, 1-2m, 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right.\right. \\ \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \text{AppellF1}\left[-\frac{1}{2}, -2m, 1+2m, \frac{1}{2}, \right.\right. \\ \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right) + \\ \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(-\left(\left(3(3A-5B) \text{AppellF1}\left[-\frac{1}{2}, -2m, 2m, \frac{1}{2}, \right.\right.\right.\right. \\ \left.\left.\left.\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right) / \right.$$



$$\begin{aligned}
& \left( 48 f (c - c \sin[e + f x])^2 \left( -\frac{1}{64} \cot\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \csc\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right. \right. \\
& \left. \left. \frac{1 - \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^{2m}}{1 + \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2} \right) \right. \\
& \left( - \left( \left( (A+B) \operatorname{AppellF1}\left[-\frac{3}{2}, -2m, 2m, -\frac{1}{2}, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \right) / \left( \operatorname{AppellF1}\left[-\frac{3}{2}, -2m, 2m, -\frac{1}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + 4m \left( \operatorname{AppellF1}\left[-\frac{1}{2}, \right. \right. \right. \right. \\
& \quad \left. \left. \left. 1-2m, 2m, \frac{1}{2}, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \right. \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1}\left[-\frac{1}{2}, -2m, 1+2m, \frac{1}{2}, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right) \right) + \\
& \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \left( - \left( \left( 3(3A-5B) \operatorname{AppellF1}\left[-\frac{1}{2}, -2m, 2m, \frac{1}{2}, \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \right) / \left( \operatorname{AppellF1}\left[-\frac{1}{2}, -2m, \right. \right. \right. \\
& \quad \left. \left. \left. 2m, \frac{1}{2}, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] - 4m \left( \operatorname{AppellF1}\left[ \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{1}{2}, 1-2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \right. \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1}\left[\frac{1}{2}, -2m, 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right) \right) + \\
& \left( 2\theta (A+B) m \operatorname{AppellF1}\left[\frac{3}{2}, -2m, 2m, \frac{5}{2}, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \left( \operatorname{AppellF1}\left[\frac{3}{2}, 1-2m, 2m, \frac{5}{2}, \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \right. \\
& \quad \left. \left. \left. -2m, 1+2m, \frac{5}{2}, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \right) \\
& \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^6 - 3 \operatorname{AppellF1}\left[\frac{1}{2}, -2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
& \quad \left. \left. \left. -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \left( -12(3A-5B) m \left( \operatorname{AppellF1}\left[ \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{5}{2}, 1-2m, 2m, \frac{7}{2}, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \right. \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, -2m, 1+2m, \frac{7}{2}, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2+5 \operatorname{AppellF1}\left[\frac{3}{2},\right. \\
 & \left.-2 m, 2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \\
 & \left.\left(\left(B\left(-15+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+A\left(9+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\right)\right) / \\
 & \left(\left(3 \operatorname{AppellF1}\left[\frac{1}{2},-2 m, 2 m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]-\right.\right. \\
 & \left.4 m\left(\operatorname{AppellF1}\left[\frac{3}{2}, 1-2 m, 2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+\operatorname{AppellF1}\left[\frac{3}{2},-2 m, 1+2 m,\right.\right. \\
 & \left.\left.\frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right) \\
 & \left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\left(-5 \operatorname{AppellF1}\left[\frac{3}{2},-2 m, 2 m, \frac{5}{2},\right.\right. \\
 & \left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+4 m\left(\operatorname{AppellF1}\left[\frac{5}{2},\right.\right.\right. \\
 & \left.\left.1-2 m, 2 m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+\right. \\
 & \left.\operatorname{AppellF1}\left[\frac{5}{2},-2 m, 1+2 m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) + \\
 & \frac{1}{24} m \operatorname{Cot}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^3\left(\frac{1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}\right)^{-1+2 m} \\
 & \left(-\left(\left(\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) / \right. \\
 & \left.\left(2\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^2\right)\right) - \\
 & \left.\frac{\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]}{2\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)}\right) \\
 & \left(-\left(\left((A+B) \operatorname{AppellF1}\left[-\frac{3}{2},-2 m, 2 m, -\frac{1}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) / \left(\operatorname{AppellF1}\left[-\frac{3}{2},-2 m, 2 m, -\frac{1}{2},\right.\right.\right. \\
 & \left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+4 m\left(\operatorname{AppellF1}\left[-\frac{1}{2},\right.\right.\right. \\
 & \left.\left.1-2 m, 2 m, \frac{1}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+\right. \\
 & \left.\left.\operatorname{AppellF1}\left[-\frac{1}{2},-2 m, 1+2 m, \frac{1}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) + \\
 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 & \left(-\left(\left(3(3 A-5 B) \operatorname{AppellF1}\left[-\frac{1}{2},-2 m, 2 m, \frac{1}{2},\right.\right.\right.\right. \\
 & \left.\left.\left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\right) / \left(\operatorname{AppellF1}\left[-\frac{1}{2},-2 m,\right.\right.\right. \\
 & \left.\left.\left.2 m, \frac{1}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]-4 m\left(\operatorname{AppellF1}\left[\right.\right.\right. \\
 & \left.\left.\left.\frac{1}{2}, 1-2 m, 2 m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \right.\right.\right. \\
 & \left.\left.\operatorname{AppellF1}\left[\frac{1}{2},-2 m, 1+2 m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \\
 & \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) + \\
 \left(2 \theta(A+B) m \operatorname{AppellF1}\left[\frac{3}{2},-2 m, 2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. & \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) \left(\operatorname{AppellF1}\left[\frac{3}{2}, 1-2 m, 2 m, \frac{5}{2},\right.\right. \\
 & \left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+\operatorname{AppellF1}\left[\frac{3}{2},\right.\right. \\
 & \left.\left.-2 m, 1+2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) \\
 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^6 & -3 \operatorname{AppellF1}\left[\frac{1}{2},-2 m, 2 m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\left(-12(3 A-5 B) m\left(\operatorname{AppellF1}\left[\right.\right.\right. \\
 & \left.\left.\left.\frac{5}{2}, 1-2 m, 2 m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+ \right.\right.\right. \\
 & \left.\left.\operatorname{AppellF1}\left[\frac{5}{2},-2 m, 1+2 m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \\
 & \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2+5 \operatorname{AppellF1}\left[\frac{3}{2},\right.\right. \\
 & \left.\left.-2 m, 2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) \\
 \left(B\left(-15+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+A\left(9+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) & \left.\right) / \\
 \left(\left(3 \operatorname{AppellF1}\left[\frac{1}{2},-2 m, 2 m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)-\right.\right. & \\
 & \left.\left.4 m\left(\operatorname{AppellF1}\left[\frac{3}{2}, 1-2 m, 2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \right. \\
 & \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+\operatorname{AppellF1}\left[\frac{3}{2},-2 m, 1+2 m,\right.\right.\right. \\
 & \left.\left.\left.\frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\right) \\
 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 & \left(-5 \operatorname{AppellF1}\left[\frac{3}{2},-2 m, 2 m, \frac{5}{2},\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + 4m \left( \text{AppellF1}\left[\frac{5}{2}, \right. \right. \\
 & \quad \left. \left. 1 - 2m, 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] + \right. \\
 & \quad \left. \text{AppellF1}\left[\frac{5}{2}, -2m, 1 + 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) + \\
 & \frac{1}{48} \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^3 \left( \frac{1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{2m} \\
 & \left( - \left( \left( (A+B) \left( -3m \text{AppellF1}\left[-\frac{1}{2}, 1 - 2m, 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \right. \right. \\
 & \quad \left. \left. \left. 3m \text{AppellF1}\left[-\frac{1}{2}, -2m, 1 + 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right) \right) / \\
 & \left( \text{AppellF1}\left[-\frac{3}{2}, -2m, 2m, -\frac{1}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] + \right. \\
 & \quad \left. 4m \left( \text{AppellF1}\left[-\frac{1}{2}, 1 - 2m, 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] + \text{AppellF1}\left[-\frac{1}{2}, -2m, 1 + 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) + \\
 & \left( (A+B) \text{AppellF1}\left[-\frac{3}{2}, -2m, 2m, -\frac{1}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \left( -3m \text{AppellF1}\left[-\frac{1}{2}, 1 - 2m, 2m, \frac{1}{2}, \right. \right. \right. \right. \\
 & \quad \quad \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - 3m \text{AppellF1}\left[-\frac{1}{2}, -2m, 1 + 2m, \frac{1}{2}, \right. \right. \\
 & \quad \quad \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + 2m \left( \text{AppellF1}\left[-\frac{1}{2}, 1 - 2m, 2m, \frac{1}{2}, \right. \right. \right. \\
 & \quad \quad \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + \text{AppellF1}\left[-\frac{1}{2}, \right. \\
 & \quad \quad \left. -2m, 1 + 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \right) \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + 4m \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right)
 \end{aligned}$$





$$\begin{aligned}
 & \frac{5}{2}, 1-2m, 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \Big]^2 + \\
 & \text{AppellF1}\left[\frac{5}{2}, -2m, 1+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 + 5 \text{AppellF1}\left[\frac{3}{2}, \right. \\
 & \quad \left. -2m, 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \\
 & \quad \left. \left( B\left(-15+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) + A\left(9+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\right)\right) \Big] \Big/ \\
 & \left( \left( 3 \text{AppellF1}\left[\frac{1}{2}, -2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right)^2 - \right. \\
 & \quad \left. 4m \left( \text{AppellF1}\left[\frac{3}{2}, 1-2m, 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \text{AppellF1}\left[\frac{3}{2}, -2m, 1+2m, \right. \right. \\
 & \quad \quad \left. \left. \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \right) \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \left( -5 \text{AppellF1}\left[\frac{3}{2}, -2m, 2m, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 4m \left( \text{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. 1-2m, 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\
 & \quad \quad \left. \text{AppellF1}\left[\frac{5}{2}, -2m, 1+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \Big) \Big) + \\
 & \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \left( - \left( \left( 3(3A-5B) \left( m \text{AppellF1}\left[\frac{1}{2}, 1-2m, 2m, \frac{3}{2}, \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \right. \right. \\
 & \quad \left. \left. \text{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + m \text{AppellF1}\left[\frac{1}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. -2m, 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \right. \right. \\
 & \quad \left. \left. \text{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \right) \Big) \Big/ \left( \text{AppellF1}\left[-\frac{1}{2}, \right. \right. \\
 & \quad \left. \left. -2m, 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right] - \right. \\
 & \quad \left. 4m \left( \text{AppellF1}\left[\frac{1}{2}, 1-2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \text{AppellF1}\left[\frac{1}{2}, -2m, 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \Big) \Big) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( 3 (3A - 5B) \operatorname{AppellF1} \left[ -\frac{1}{2}, -2m, 2m, \frac{1}{2}, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \left. \right) \left( m \operatorname{AppellF1} \left[ \frac{1}{2}, 1 - 2m, 2m, \frac{3}{2}, \right. \right. \\
 & \quad \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \left. \right) \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \\
 & \quad \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right] + m \operatorname{AppellF1} \left[ \frac{1}{2}, -2m, 1 + 2m, \frac{3}{2}, \right. \\
 & \quad \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \left. \right) \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \\
 & \quad \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right] - 2m \left( \operatorname{AppellF1} \left[ \frac{1}{2}, 1 - 2m, 2m, \frac{3}{2}, \right. \right. \\
 & \quad \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \left. \right) + \operatorname{AppellF1} \left[ \frac{1}{2}, \right. \\
 & \quad \left. - 2m, 1 + 2m, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right) \\
 & \quad \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right] - 4m \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \\
 & \quad \left( -\frac{2}{3} m \operatorname{AppellF1} \left[ \frac{3}{2}, 1 - 2m, 1 + 2m, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right) \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right. \\
 & \quad \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right] + \frac{1}{6} (1 - 2m) \operatorname{AppellF1} \left[ \frac{3}{2}, 2 - 2m, \right. \\
 & \quad \left. 2m, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right) \\
 & \quad \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right] - \frac{1}{6} (1 + 2m) \operatorname{AppellF1} \left[ \right. \\
 & \quad \left. \frac{3}{2}, -2m, 2 + 2m, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right) \\
 & \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right] \right) \right) \right) / \\
 & \left( \operatorname{AppellF1} \left[ -\frac{1}{2}, -2m, 2m, \frac{1}{2}, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] - \right. \\
 & \quad \left. 4m \left( \operatorname{AppellF1} \left[ \frac{1}{2}, 1 - 2m, 2m, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right) + \operatorname{AppellF1} \left[ \frac{1}{2}, -2m, 1 + 2m, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{\pi}{2} - fx \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right) \right) \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right)^2 - \\
 & \left( \left( -2m \left( \operatorname{AppellF1} \left[ \frac{3}{2}, 1 - 2m, 2m, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right) + \operatorname{AppellF1} \left[ \frac{3}{2}, -2m, 1 + 2m, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + 3\left(-\frac{1}{3} m \text{AppellF1}\left[\frac{3}{2}, 1 - 2m, 2m, \frac{5}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right. \\
 & \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{3} m \text{AppellF1}\left[\frac{3}{2}, -2m, 1 + 2m, \frac{5}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
 & \left.\text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) - \\
 & 4m \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(-\frac{6}{5} m \text{AppellF1}\left[\frac{5}{2}, 1 - 2m, 1 + 2m, \frac{7}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right. \\
 & \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{3}{10} (1 - 2m) \text{AppellF1}\left[\frac{5}{2}, 2 - 2m, 2m, \frac{7}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
 & \left.\text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{3}{10} (1 + 2m) \text{AppellF1}\left[\frac{5}{2}, -2m, 2 + 2m, \frac{7}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right. \\
 & \left.\text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) \\
 & \left(2\theta (A + B) m \text{AppellF1}\left[\frac{3}{2}, -2m, 2m, \frac{5}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right. \\
 & \left.\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \left(\text{AppellF1}\left[\frac{3}{2}, 1 - 2m, 2m, \frac{5}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \text{AppellF1}\left[\frac{3}{2}, -2m, 1 + 2m, \frac{5}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \\
 & \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^6 - 3 \text{AppellF1}\left[\frac{1}{2}, -2m, 2m, \frac{3}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \\
 & \left(-12 (3A - 5B) m \left(\text{AppellF1}\left[\frac{5}{2}, 1 - 2m, 2m, \frac{7}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \text{AppellF1}\left[\frac{5}{2}, -2m, 1 + 2m, \frac{7}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \right. \\
 & \left.\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + 5 \text{AppellF1}\left[\frac{3}{2}, -2m, 2m, \frac{5}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
 & \left.\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( B \left( -15 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + A \left( 9 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \left( \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -2 m, 2 m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] - \right. \right. \\
 & 4 m \left( \operatorname{AppellF1} \left[ \frac{3}{2}, 1 - 2 m, 2 m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \operatorname{AppellF1} \left[ \frac{3}{2}, -2 m, 1 + 2 m, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \\
 & \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^2 \left( -5 \operatorname{AppellF1} \left[ \frac{3}{2}, -2 m, 2 m, \frac{5}{2}, \right. \right. \\
 & \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 4 m \left( \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, 1 - 2 m, 2 m, \frac{7}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \right. \\
 & \quad \left. \operatorname{AppellF1} \left[ \frac{5}{2}, -2 m, 1 + 2 m, \frac{7}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \Bigg) - \\
 & \left( \left( 2 m \left( \operatorname{AppellF1} \left[ \frac{5}{2}, 1 - 2 m, 2 m, \frac{7}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \operatorname{AppellF1} \left[ \frac{5}{2}, -2 m, 1 + 2 m, \right. \right. \right. \\
 & \quad \left. \left. \frac{7}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \right) \\
 & \sec \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] - 5 \left( -\frac{3}{5} m \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, 1 - 2 m, 2 m, \frac{7}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \\
 & \sec \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] - \frac{3}{5} m \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \\
 & \quad \left. -2 m, 1 + 2 m, \frac{7}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \\
 & \sec \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \Bigg) + \\
 & 4 m \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \left( -\frac{10}{7} m \operatorname{AppellF1} \left[ \frac{7}{2}, 1 - 2 m, 1 + 2 m, \right. \right. \\
 & \quad \left. \left. \frac{9}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \\
 & \sec \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] + \frac{5}{14} (1 - 2 m) \operatorname{AppellF1} \left[ \right. \\
 & \quad \left. \frac{7}{2}, 2 - 2 m, 2 m, \frac{9}{2}, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \\
 & \sec \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] - \frac{5}{14} (1 + 2 m) \operatorname{AppellF1} \left[ \right.
 \end{aligned}$$

$$\begin{aligned}
& \frac{7}{2}, -2m, 2+2m, \frac{9}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \\
& \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \Bigg) \\
& \left( 2\theta(A+B)m \operatorname{AppellF1}\left[\frac{3}{2}, -2m, 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \left( \operatorname{AppellF1}\left[\frac{3}{2}, 1-2m, 2m, \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
& \quad \left. \left. -2m, 1+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \right) \\
& \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^6 - 3 \operatorname{AppellF1}\left[\frac{1}{2}, -2m, 2m, \frac{3}{2}, \right. \\
& \quad \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \\
& \quad \left( -12(3A-5B)m \left( \operatorname{AppellF1}\left[\frac{5}{2}, 1-2m, 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \operatorname{AppellF1}\left[\frac{5}{2}, -2m, 1+2m, \right. \right. \right. \\
& \quad \left. \left. \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \right) \\
& \quad \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 + 5 \operatorname{AppellF1}\left[\frac{3}{2}, -2m, 2m, \frac{5}{2}, \right. \\
& \quad \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \\
& \quad \left( B \left( -15 + \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) + A \left( 9 + \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \right) \Bigg) \Bigg) / \\
& \left( \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \right. \right. \\
& \quad \left. \left. 4m \left( \operatorname{AppellF1}\left[\frac{3}{2}, 1-2m, 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}, -2m, 1+2m, \right. \right. \right. \\
& \quad \left. \left. \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \right) \\
& \quad \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \left( -5 \operatorname{AppellF1}\left[\frac{3}{2}, -2m, 2m, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 4m \left( \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. 1-2m, 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\
& \quad \left. \operatorname{AppellF1}\left[\frac{5}{2}, -2m, 1+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \Bigg) +
\end{aligned}$$



$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \operatorname{AppellF1}\left[\frac{5}{2},-2 m, 1+2 m,\right. \\
 & \left.\frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \\
 & \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2+5 \operatorname{AppellF1}\left[\frac{3}{2},-2 m, 2 m, \frac{5}{2},\right. \\
 & \left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \\
 & \left(\operatorname{B}\left(-15+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+\operatorname{A}\left(9+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\right)- \\
 & 3 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\left(-\frac{1}{3} m \operatorname{AppellF1}\left[\frac{3}{2}, 1-2 m, 2 m, \frac{5}{2},\right. \right. \\
 & \left. \left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]-\right. \\
 & \left. \frac{1}{3} m \operatorname{AppellF1}\left[\frac{3}{2},-2 m, 1+2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right. \right. \\
 & \left. \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right) \\
 & \left(-12(3 A-5 B) m\left(\operatorname{AppellF1}\left[\frac{5}{2}, 1-2 m, 2 m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right. \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \operatorname{AppellF1}\left[\frac{5}{2},-2 m, 1+2 m,\right. \right. \\
 & \left. \left.\frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \right) \\
 & \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2+5 \operatorname{AppellF1}\left[\frac{3}{2},-2 m, 2 m, \frac{5}{2},\right. \\
 & \left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \\
 & \left(\operatorname{B}\left(-15+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+\operatorname{A}\left(9+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\right)- \\
 & 3 \operatorname{AppellF1}\left[\frac{1}{2},-2 m, 2 m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \\
 & \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\left(-6(3 A-5 B) m\left(\operatorname{AppellF1}\left[\frac{5}{2}, 1-2 m, 2 m, \frac{7}{2},\right. \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \operatorname{AppellF1}\left[\frac{5}{2},\right. \right. \\
 & \left. \left.-2 m, 1+2 m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \right) \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]+5 \operatorname{AppellF1}\left[\frac{3}{2},\right. \\
 & \left.-2 m, 2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \\
 & \left(\frac{1}{2} \operatorname{A} \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]+ \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{2} B \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] - \\
 12 & (3 A-5 B) m \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\left(-\frac{10}{7} m \operatorname{AppellF1}\left[\frac{7}{2}, 1-2 m, \right.\right. \\
 & \left.1+2 m, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] + \\
 \frac{5}{14} & (1-2 m) \operatorname{AppellF1}\left[\frac{7}{2}, 2-2 m, 2 m, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \\
 & \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \\
 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] - \frac{5}{14} & (1+2 m) \operatorname{AppellF1}\left[\frac{7}{2}, -2 m, \right. \\
 & \left.2+2 m, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \\
 \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] & + 5\left(-\frac{3}{5} m \operatorname{AppellF1}\left[\frac{5}{2}, \right.\right. \\
 & \left.\frac{5}{2}, 1-2 m, 2 m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \\
 \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] - \frac{3}{5} m & \operatorname{AppellF1}\left[\frac{5}{2}, \right. \\
 & \left.-2 m, 1+2 m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \\
 \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] & \\
 \left(B\left(-15+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+A\left(9+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) & \left. \right) / \\
 \left(\left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2 m, 2 m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] - \right. & \\
 4 m\left(\operatorname{AppellF1}\left[\frac{3}{2}, 1-2 m, 2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. & \\
 \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \operatorname{AppellF1}\left[\frac{3}{2}, -2 m, 1+2 m, \right. & \\
 \left. \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) & \\
 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\left(-5 \operatorname{AppellF1}\left[\frac{3}{2}, -2 m, 2 m, \frac{5}{2}, \right. & \\
 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+4 m\left(\operatorname{AppellF1}\left[\frac{5}{2}, \right. & \\
 1-2 m, 2 m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) & \\
 \left. + \operatorname{AppellF1}\left[\frac{5}{2}, -2 m, 1+2 m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. & \right.
 \end{aligned}$$



$$-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)^2\right]\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)^2\right]\right)\right)\right)\right)\right)\right)$$

**Problem 202: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sin[e + fx])^m (A + B \sin[e + fx])}{(c - c \sin[e + fx])^3} dx$$

Optimal (type 5, 148 leaves, 5 steps):

$$\frac{1}{5 a^2 c^3 f (2-m)} 2^{\frac{1}{2}+m} (A (2-m) - B (3+m)) \text{Hypergeometric2F1}\left[-\frac{5}{2}, \frac{1}{2}-m, -\frac{3}{2}, \frac{1}{2}(1-\sin[e+fx])\right]$$

$$\text{Sec}[e+fx]^5 (1+\sin[e+fx])^{\frac{1}{2}-m} (a+a \sin[e+fx])^{2+m} + \frac{B \text{Sec}[e+fx]^5 (a+a \sin[e+fx])^{3+m}}{a^3 c^3 f (2-m)}$$

Result (type 6, 34716 leaves): Display of huge result suppressed!

**Problem 203: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sin[e + fx])^m (A + B \sin[e + fx])}{\sqrt{c - c \sin[e + fx]}} dx$$

Optimal (type 5, 118 leaves, 4 steps):

$$-\frac{2 B \cos[e+fx] (a+a \sin[e+fx])^m}{f (1+2m) \sqrt{c-c \sin[e+fx]}} +$$

$$\left( (A+B) \cos[e+fx] \text{Hypergeometric2F1}\left[1, \frac{1}{2}+m, \frac{3}{2}+m, \frac{1}{2}(1+\sin[e+fx])\right] \right)$$

$$(a+a \sin[e+fx])^m \left/ (f (1+2m) \sqrt{c-c \sin[e+fx]}\right)$$

Result (type 6, 7013 leaves):

$$-\left(\left(\sqrt{2}\left(\cos\left[\frac{1}{2}(e+fx)\right]-\sin\left[\frac{1}{2}(e+fx)\right]\right)\right)\right)$$

$$(a+a \sin[e+fx])^m \left( \frac{A \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m}}{\cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]-\sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]} + \right.$$

$$\left. \frac{B \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \sin[e+fx]}{\cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]-\sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]} \right)$$

$$\left( 2 B \left( \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]-\cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{-2m} \right) + \right.$$





$$\begin{aligned}
 & \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \left( -1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) - \\
 & \left( A (1+m) \operatorname{AppellF1} \left[ 1+2m, 2m, 1, 2+2m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right], \right. \\
 & \quad \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \operatorname{Cot} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \\
 & \quad \operatorname{Csc} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) / \\
 & \left( 2 \left( -2 (1+m) \operatorname{AppellF1} \left[ 1+2m, 2m, 1, 2+2m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right], \right. \right. \\
 & \quad \left. \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \left( \operatorname{AppellF1} \left[ 2+2m, 2m, 2, 3+2m, \right. \right. \right. \\
 & \quad \left. \left. \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right], 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \right. \\
 & \quad \left. m \operatorname{AppellF1} \left[ 2+2m, 1+2m, 1, 3+2m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right], \right. \\
 & \quad \left. \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \left( -1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \right) - \\
 & \left( B (1+m) \operatorname{AppellF1} \left[ 1+2m, 2m, 1, 2+2m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right], \right. \\
 & \quad \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \operatorname{Cot} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \\
 & \quad \operatorname{Csc} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) / \\
 & \left( 2 \left( -2 (1+m) \operatorname{AppellF1} \left[ 1+2m, 2m, 1, 2+2m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right], \right. \right. \\
 & \quad \left. \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \left( \operatorname{AppellF1} \left[ 2+2m, 2m, 2, 3+2m, \right. \right. \right. \\
 & \quad \left. \left. \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right], 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \right. \\
 & \quad \left. m \operatorname{AppellF1} \left[ 2+2m, 1+2m, 1, 3+2m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right], \right. \\
 & \quad \left. \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \left( -1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \right) + \\
 & \left( A (1+m) \operatorname{Cot} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \left( -\frac{1}{2(2+2m)} (1+2m) \operatorname{AppellF1} \left[ 2+2m, \right. \right. \right. \\
 & \quad \left. \left. 2m, 2, 3+2m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right], 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \\
 & \quad \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] - \frac{1}{2(2+2m)} \\
 & \quad m (1+2m) \operatorname{AppellF1} \left[ 2+2m, 1+2m, 1, 3+2m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right], \\
 & \quad \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \right) \\
 & \left. \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) / \left( -2 (1+m) \operatorname{AppellF1} \left[ 1+2m, 2m, 1, 2+2m, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 + \left( \text{AppellF1} [2 + 2 m, \right. \\
 & \quad 2 m, 2, 3 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \\
 & \quad m \text{AppellF1} [2 + 2 m, 1 + 2 m, 1, 3 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), \\
 & \quad \quad 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \left( -1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \\
 & \left( B (1 + m) \cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \left( -\frac{1}{2 (2 + 2 m)} (1 + 2 m) \text{AppellF1} [2 + 2 m, \right. \right. \\
 & \quad 2 m, 2, 3 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \\
 & \quad \text{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] - \frac{1}{2 (2 + 2 m)} \\
 & \quad m (1 + 2 m) \text{AppellF1} [2 + 2 m, 1 + 2 m, 1, 3 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), \\
 & \quad \quad 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \text{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \right) \\
 & \left. \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) / \left( -2 (1 + m) \text{AppellF1} [1 + 2 m, 2 m, 1, 2 + 2 m, \right. \\
 & \quad \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \left( \text{AppellF1} [2 + 2 m, \right. \\
 & \quad 2 m, 2, 3 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \\
 & \quad m \text{AppellF1} [2 + 2 m, 1 + 2 m, 1, 3 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), \\
 & \quad \quad 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \left( -1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) - \\
 & \left( A (1 + m) \text{AppellF1} [1 + 2 m, 2 m, 1, 2 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), \right. \\
 & \quad \quad 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \\
 & \left. \left( \frac{1}{2} \left( \text{AppellF1} [2 + 2 m, 2 m, 2, 3 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), \right. \right. \right. \right. \\
 & \quad \quad \quad 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + m \text{AppellF1} [2 + 2 m, 1 + 2 m, 1, 3 + 2 m, \\
 & \quad \quad \quad \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \\
 & \quad \quad \quad \text{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] - 2 (1 + m) \\
 & \quad \quad \quad \left( -\frac{1}{2 (2 + 2 m)} (1 + 2 m) \text{AppellF1} [2 + 2 m, 2 m, 2, 3 + 2 m, \right. \\
 & \quad \quad \quad \left. \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{2(2+2m)} m(1+2m) \\
 & \text{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \right. \\
 & \quad \left. \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \Bigg) + \\
 & \left(-1 + \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \left(-\frac{1}{3+2m}(2+2m) \text{AppellF1}\left[3+2m, 2m, \right. \right. \\
 & \quad \left. \left. 3, 4+2m, \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \left. \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{2(3+2m)} m(2+2m) \right. \\
 & \quad \left. \text{AppellF1}\left[3+2m, 1+2m, 2, 4+2m, \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), \right. \right. \\
 & \quad \left. \left. 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right. + \\
 & \quad \left. m\left(-\frac{1}{2(3+2m)}(2+2m) \text{AppellF1}\left[3+2m, 1+2m, 2, 4+2m, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \quad \left. \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{4(3+2m)} \right. \\
 & \quad \quad \left. (1+2m)(2+2m) \text{AppellF1}\left[3+2m, 2+2m, 1, 4+2m, \right. \right. \\
 & \quad \quad \left. \left. \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \quad \left. \left. \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right)\right)\right) \Bigg) / \\
 & \left(-2(1+m) \text{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), \right. \right. \\
 & \quad \left. \left. 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \left(\text{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \quad \quad \left. m \text{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), \right. \right. \\
 & \quad \quad \left. \left. 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \left(-1 + \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2 - \right. \\
 & \left. \left(B(1+m) \text{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), \right. \right. \right. \\
 & \quad \left. \left. 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \text{Cot}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right. \\
 & \quad \left. \left. \left(\frac{1}{2}\left(\text{AppellF1}\left[2+2m, 2m, 2, 3+2m, \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), \right. \right. \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2] + m \operatorname{AppellF1}\left[2 + 2 m, 1 + 2 m, 1, 3 + 2 m, \right. \\
 & \left. \frac{1}{2}\left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right), 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - 2(1 + m) \\
 & \left(-\frac{1}{2(2 + 2 m)}(1 + 2 m) \operatorname{AppellF1}\left[2 + 2 m, 2 m, 2, 3 + 2 m, \right. \right. \\
 & \left. \left. \frac{1}{2}\left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right), 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{1}{2(2 + 2 m)} m(1 + 2 m) \right. \\
 & \left. \operatorname{AppellF1}\left[2 + 2 m, 1 + 2 m, 1, 3 + 2 m, \frac{1}{2}\left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right), 1 - \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right] + \\
 & \left(-1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right) \left(-\frac{1}{3 + 2 m}(2 + 2 m) \operatorname{AppellF1}\left[3 + 2 m, 2 m, \right. \right. \\
 & \left. \left. 3, 4 + 2 m, \frac{1}{2}\left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right), 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{1}{2(3 + 2 m)} m(2 + 2 m) \right. \\
 & \left. \operatorname{AppellF1}\left[3 + 2 m, 1 + 2 m, 2, 4 + 2 m, \frac{1}{2}\left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right), \right. \right. \\
 & \left. \left. 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] + \right. \\
 & \left. m\left(-\frac{1}{2(3 + 2 m)}(2 + 2 m) \operatorname{AppellF1}\left[3 + 2 m, 1 + 2 m, 2, 4 + 2 m, \right. \right. \right. \\
 & \left. \left. \frac{1}{2}\left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right), 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{1}{4(3 + 2 m)} \right. \\
 & \left. (1 + 2 m)(2 + 2 m) \operatorname{AppellF1}\left[3 + 2 m, 2 + 2 m, 1, 4 + 2 m, \right. \right. \\
 & \left. \left. \frac{1}{2}\left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right), 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]\right)\right) / \\
 & \left(-2(1 + m) \operatorname{AppellF1}\left[1 + 2 m, 2 m, 1, 2 + 2 m, \frac{1}{2}\left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right), \right. \right. \\
 & \left. \left. 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \left(\operatorname{AppellF1}\left[2 + 2 m, 2 m, 2, 3 + 2 m, \right. \right. \right. \\
 & \left. \left. \frac{1}{2}\left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right), 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \right.
 \end{aligned}$$

$$m \operatorname{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2} \left(1 - \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), \right. \\ \left. 1 - \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \left(-1 + \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2\right]$$

**Problem 204: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(A + B \sin[e + fx]) (c + c \sin[e + fx])^m}{\sqrt{a - a \sin[e + fx]}} dx$$

Optimal (type 5, 118 leaves, 4 steps):

$$-\frac{2B \cos[e + fx] (c + c \sin[e + fx])^m}{f(1+2m)\sqrt{a - a \sin[e + fx]}} + \\ \left( (A+B) \cos[e + fx] \operatorname{Hypergeometric2F1}\left[1, \frac{1}{2} + m, \frac{3}{2} + m, \frac{1}{2} (1 + \sin[e + fx])\right] \right. \\ \left. (c + c \sin[e + fx])^m \right) / \left( f(1+2m)\sqrt{a - a \sin[e + fx]} \right)$$

Result (type 6, 7013 leaves):

$$-\left[ \sqrt{2} \left( \cos\left[\frac{1}{2}(e + fx)\right] - \sin\left[\frac{1}{2}(e + fx)\right] \right) \right. \\ \left. (c + c \sin[e + fx])^m \left( \frac{A \cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx\right)\right]^{2m}}{\cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + fx\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + fx\right)\right]} + \right. \right. \\ \left. \left. \frac{B \cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx\right)\right]^{2m} \sin[e + fx]}{\cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + fx\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + fx\right)\right]} \right) \right. \\ \left. \left( 2B \left( \cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx\right)\right] - \cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx\right)\right]^{-2m} \right) + \right. \right. \\ \left. \left( A(1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2} \left(1 - \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), \right. \right. \right. \right. \\ \left. \left. \left. 1 - \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cot\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(1 - \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right) \right) / \right. \\ \left. \left( -2(1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2} \left(1 - \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), \right. \right. \right. \right. \\ \left. \left. \left. 1 - \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \left( \operatorname{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right. \right. \right. \right. \\ \left. \left. \left. \frac{1}{2} \left(1 - \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \right. \\ \left. \left. \left. m \operatorname{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2} \left(1 - \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \right. \right. \right. \right. \right.$$



$$\begin{aligned}
 & \left( \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \\
 & \left( B(1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], \right. \\
 & \quad \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right) / \\
 & \left( -2(1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], \right. \\
 & \quad \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \left( \operatorname{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right. \right. \\
 & \quad \left. \left. \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \right. \\
 & \quad \left. m \operatorname{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], 1 - \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right) \right) / \\
 & \left( f(1+2m) \sqrt{a - a \sin[e + fx]} \left( -\frac{1}{1+2m} \sqrt{2} m \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^{-1+2m} \right. \right. \\
 & \quad \left. \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \left( 2B \left( \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] - \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^{-2m} \right) + \right. \right. \\
 & \quad \left( A(1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], 1 - \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right) \right) / \\
 & \left( -2(1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], \right. \\
 & \quad \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \left( \operatorname{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right. \right. \\
 & \quad \left. \left. \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \right. \\
 & \quad \left. m \operatorname{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], \right. \\
 & \quad \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right) + \\
 & \left( B(1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], 1 - \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right) / \\
 & \left( -2(1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], \right. \\
 & \quad \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \left( \operatorname{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right. \right. \\
 & \quad \left. \left. \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \right.
 \end{aligned}$$

$$\begin{aligned}
 & m \operatorname{AppellF1}\left[2+2 m, 1+2 m, 1, 3+2 m, \frac{1}{2}\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right),\right. \\
 & \quad \left.1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\left(-1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right]+ \\
 & \frac{1}{1+2 m} \sqrt{2} \operatorname{Cos}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^{2 m}\left(2 B\left(-\frac{1}{2} \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]-\right.\right. \\
 & \quad \left.\left.m \operatorname{Cos}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^{-1-2 m} \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)-\right. \\
 & \left.(A(1+m) \operatorname{AppellF1}\left[1+2 m, 2 m, 1, 2+2 m, \frac{1}{2}\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right), 1-\right.\right. \\
 & \quad \left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Csc}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right) / \\
 & \left(2\left(-2(1+m) \operatorname{AppellF1}\left[1+2 m, 2 m, 1, 2+2 m, \frac{1}{2}\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right),\right.\right.\right. \\
 & \quad \left.\left.1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+\left(\operatorname{AppellF1}\left[2+2 m, 2 m, 2, 3+2 m,\right.\right.\right. \\
 & \quad \left.\left.\frac{1}{2}\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right), 1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \right. \\
 & \quad \left. m \operatorname{AppellF1}\left[2+2 m, 1+2 m, 1, 3+2 m, \frac{1}{2}\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right),\right.\right. \\
 & \quad \left.\left.1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\left(-1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\right)- \\
 & \left.(B(1+m) \operatorname{AppellF1}\left[1+2 m, 2 m, 1, 2+2 m, \frac{1}{2}\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right),\right.\right. \\
 & \quad \left.\left.1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Csc}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right) / \\
 & \left(2\left(-2(1+m) \operatorname{AppellF1}\left[1+2 m, 2 m, 1, 2+2 m, \frac{1}{2}\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right),\right.\right.\right. \\
 & \quad \left.\left.1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+\left(\operatorname{AppellF1}\left[2+2 m, 2 m, 2, 3+2 m,\right.\right.\right. \\
 & \quad \left.\left.\frac{1}{2}\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right), 1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \right. \\
 & \quad \left. m \operatorname{AppellF1}\left[2+2 m, 1+2 m, 1, 3+2 m, \frac{1}{2}\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right),\right.\right. \\
 & \quad \left.\left.1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\left(-1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\right)- \\
 & \left.(A(1+m) \operatorname{AppellF1}\left[1+2 m, 2 m, 1, 2+2 m, \frac{1}{2}\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right),\right.\right. \\
 & \quad \left.\left.1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Cot}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right. \\
 & \quad \left.\operatorname{Csc}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) / \\
 & \left(2\left(-2(1+m) \operatorname{AppellF1}\left[1+2 m, 2 m, 1, 2+2 m, \frac{1}{2}\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right),\right.\right.\right. \\
 & \quad \left.\left.1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+\left(\operatorname{AppellF1}\left[2+2 m, 2 m, 2, 3+2 m,\right.\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \Bigg] + \\
 & m \operatorname{AppellF1} \left[ 2 + 2 m, 1 + 2 m, 1, 3 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), \right. \\
 & \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \left( -1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right] - \\
 & \left( B (1 + m) \operatorname{AppellF1} \left[ 1 + 2 m, 2 m, 1, 2 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), \right. \right. \\
 & \left. \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \right. \\
 & \left. \operatorname{Csc} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \right] / \\
 & \left( 2 \left( -2 (1 + m) \operatorname{AppellF1} \left[ 1 + 2 m, 2 m, 1, 2 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), \right. \right. \right. \\
 & \left. \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \left( \operatorname{AppellF1} \left[ 2 + 2 m, 2 m, 2, 3 + 2 m, \right. \right. \right. \\
 & \left. \left. \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \right. \\
 & \left. \left. m \operatorname{AppellF1} \left[ 2 + 2 m, 1 + 2 m, 1, 3 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), \right. \right. \right. \\
 & \left. \left. \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \left( -1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \right) \right) + \\
 & \left( A (1 + m) \cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \left( -\frac{1}{2 (2 + 2 m)} (1 + 2 m) \operatorname{AppellF1} \left[ 2 + 2 m, \right. \right. \right. \\
 & \left. \left. 2 m, 2, 3 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \\
 & \left. \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] - \frac{1}{2 (2 + 2 m)} \right. \\
 & \left. m (1 + 2 m) \operatorname{AppellF1} \left[ 2 + 2 m, 1 + 2 m, 1, 3 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), \right. \right. \\
 & \left. \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \right) \right. \\
 & \left. \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \right] / \left( -2 (1 + m) \operatorname{AppellF1} \left[ 1 + 2 m, 2 m, 1, 2 + 2 m, \right. \right. \\
 & \left. \left. \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \left( \operatorname{AppellF1} \left[ 2 + 2 m, \right. \right. \right. \\
 & \left. \left. 2 m, 2, 3 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \right. \\
 & \left. \left. m \operatorname{AppellF1} \left[ 2 + 2 m, 1 + 2 m, 1, 3 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), \right. \right. \right. \\
 & \left. \left. \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \left( -1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \right) \right) + \\
 & \left( B (1 + m) \cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \left( -\frac{1}{2 (2 + 2 m)} (1 + 2 m) \operatorname{AppellF1} \left[ 2 + 2 m, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2m, 2, 3+2m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \\
 & \sec \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right] - \frac{1}{2(2+2m)} \\
 & m(1+2m) \operatorname{AppellF1} \left[ 2+2m, 1+2m, 1, 3+2m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right), \right. \\
 & \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] \sec \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right] \\
 & \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right) \Big/ \left( -2(1+m) \operatorname{AppellF1} \left[ 1+2m, 2m, 1, 2+2m, \right. \right. \\
 & \left. \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] + \left( \operatorname{AppellF1} \left[ 2+2m, \right. \right. \\
 & \left. 2m, 2, 3+2m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] + \right. \\
 & \left. m \operatorname{AppellF1} \left[ 2+2m, 1+2m, 1, 3+2m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right), \right. \right. \\
 & \left. \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right) \left( -1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right) - \\
 & \left( A(1+m) \operatorname{AppellF1} \left[ 1+2m, 2m, 1, 2+2m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right), \right. \right. \\
 & \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] \cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right) \right. \\
 & \left. \left( \frac{1}{2} \left( \operatorname{AppellF1} \left[ 2+2m, 2m, 2, 3+2m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right), \right. \right. \right. \right. \\
 & \left. \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] + m \operatorname{AppellF1} \left[ 2+2m, 1+2m, 1, 3+2m, \right. \right. \right. \\
 & \left. \left. \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right) \\
 & \sec \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right] - 2(1+m) \\
 & \left( -\frac{1}{2(2+2m)} (1+2m) \operatorname{AppellF1} \left[ 2+2m, 2m, 2, 3+2m, \right. \right. \\
 & \left. \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right) \\
 & \sec \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right] - \frac{1}{2(2+2m)} m(1+2m) \\
 & \operatorname{AppellF1} \left[ 2+2m, 1+2m, 1, 3+2m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right), 1 - \right. \\
 & \left. \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] \sec \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right] \Big) + \\
 & \left( -1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right) \left( -\frac{1}{3+2m} (2+2m) \operatorname{AppellF1} \left[ 3+2m, 2m, \right. \right. \\
 & \left. 3, 4+2m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{1}{2(3+2m)} m(2+2m) \\
 & \text{AppellF1}\left[3+2m, 1+2m, 2, 4+2m, \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)^2\right], \\
 & 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] + \\
 & m\left(-\frac{1}{2(3+2m)}(2+2m) \text{AppellF1}\left[3+2m, 1+2m, 2, 4+2m, \right. \right. \\
 & \quad \left. \left. \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)^2\right], 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \\
 & \quad \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{1}{4(3+2m)} \\
 & \quad (1+2m)(2+2m) \text{AppellF1}\left[3+2m, 2+2m, 1, 4+2m, \right. \\
 & \quad \left. \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)^2\right], 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \\
 & \quad \left. \left. \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)\right) \Big/ \\
 & \left(-2(1+m) \text{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)^2\right], \right. \\
 & \quad \left. 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \left(\text{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right. \right. \\
 & \quad \left. \left. \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)^2\right], 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \right. \\
 & \quad \left. m \text{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)^2\right], \right. \\
 & \quad \left. 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \left(-1 + \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^2 - \right. \\
 & \left. \left(B(1+m) \text{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)^2\right], \right. \right. \\
 & \quad \left. 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \text{Cot}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^2\right) \\
 & \left(\frac{1}{2}\left(\text{AppellF1}\left[2+2m, 2m, 2, 3+2m, \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)^2\right], \right. \right. \\
 & \quad \left. 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + m \text{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \right. \\
 & \quad \left. \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)^2\right], 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right) \\
 & \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - 2(1+m) \\
 & \left(-\frac{1}{2(2+2m)}(1+2m) \text{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right. \right. \\
 & \quad \left. \left. \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)^2\right], 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)
 \end{aligned}$$

$$\begin{aligned}
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{1}{2(2+2m)} m(1+2m) \\
 & \operatorname{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2}\left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right), 1 - \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] \Bigg) + \\
 & \left(-1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right) \left(-\frac{1}{3+2m}(2+2m) \operatorname{AppellF1}\left[3+2m, 2m, \right. \right. \\
 & \quad \left. \left. 3, 4+2m, \frac{1}{2}\left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right), 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{1}{2(3+2m)} m(2+2m) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[3+2m, 1+2m, 2, 4+2m, \frac{1}{2}\left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right), \right. \right. \\
 & \quad \left. \left. 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] \right. + \\
 & \quad \left. m\left(-\frac{1}{2(3+2m)}(2+2m) \operatorname{AppellF1}\left[3+2m, 1+2m, 2, 4+2m, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{1}{2}\left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right), 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right. \\
 & \quad \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{1}{4(3+2m)} \right. \\
 & \quad \quad \left. (1+2m)(2+2m) \operatorname{AppellF1}\left[3+2m, 2+2m, 1, 4+2m, \right. \right. \\
 & \quad \quad \left. \left. \frac{1}{2}\left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right), 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right. \\
 & \quad \quad \left. \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)\right)\right) \Bigg) / \\
 & \left(-2(1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2}\left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right), \right. \right. \\
 & \quad \left. \left. 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \left(\operatorname{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{1}{2}\left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right), 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \right. \\
 & \quad \quad \left. m \operatorname{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2}\left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right), \right. \right. \\
 & \quad \quad \left. \left. 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right)\right) \left(-1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^2 \Bigg) \Bigg) \Bigg) \Bigg)
 \end{aligned}$$

**Problem 205: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (a + a \operatorname{Sin}[e + f x])^m (A + B \operatorname{Sin}[e + f x]) (c - c \operatorname{Sin}[e + f x])^{5/2} dx$$

Optimal (type 3, 275 leaves, 4 steps):

$$\frac{64 c^3 (B (5-2 m)-A (7+2 m)) \operatorname{Cos}[e+f x] (a+a \operatorname{Sin}[e+f x])^m}{f (5+2 m)(7+2 m)(3+8 m+4 m^2) \sqrt{c-c \operatorname{Sin}[e+f x]}} - \frac{(16 c^2 (B (5-2 m)-A (7+2 m)) \operatorname{Cos}[e+f x] (a+a \operatorname{Sin}[e+f x])^m \sqrt{c-c \operatorname{Sin}[e+f x]})}{(f (7+2 m)(15+16 m+4 m^2))} - \frac{(2 c (B (5-2 m)-A (7+2 m)) \operatorname{Cos}[e+f x] (a+a \operatorname{Sin}[e+f x])^m (c-c \operatorname{Sin}[e+f x])^{3/2})}{(f (5+2 m)(7+2 m))} - \frac{2 B \operatorname{Cos}[e+f x] (a+a \operatorname{Sin}[e+f x])^m (c-c \operatorname{Sin}[e+f x])^{5/2}}{f (7+2 m)}$$

Result (type 3, 667 leaves):

$$\frac{1}{f \left( \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] - \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] \right)^5} (a(1+\operatorname{Sin}[e+f x]))^m (c-c \operatorname{Sin}[e+f x])^{5/2} \left( \left( (2100 A - 1575 B + 1272 A m - 110 B m + 304 A m^2 - 68 B m^2 + 32 A m^3 - 8 B m^3) \left( \left( \left( \frac{1}{8} + \frac{i}{8} \right) \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] + \left( \frac{1}{8} - \frac{i}{8} \right) \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] \right) \right) / \left( (1+2 m)(3+2 m)(5+2 m)(7+2 m) \right) + \left( (2100 A - 1575 B + 1272 A m - 110 B m + 304 A m^2 - 68 B m^2 + 32 A m^3 - 8 B m^3) \left( \left( \left( \frac{1}{8} - \frac{i}{8} \right) \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] + \left( \frac{1}{8} + \frac{i}{8} \right) \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] \right) \right) / \left( (1+2 m)(3+2 m)(5+2 m)(7+2 m) \right) + \left( (350 A - 385 B + 184 A m - 104 B m + 24 A m^2 - 12 B m^2) \left( \left( \left( \frac{1}{8} - \frac{i}{8} \right) \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right] - \left( \frac{1}{8} + \frac{i}{8} \right) \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right] \right) \right) / \left( (3+2 m)(5+2 m)(7+2 m) \right) + \left( (350 A - 385 B + 184 A m - 104 B m + 24 A m^2 - 12 B m^2) \left( \left( \left( \frac{1}{8} + \frac{i}{8} \right) \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right] - \left( \frac{1}{8} - \frac{i}{8} \right) \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right] \right) \right) / \left( (3+2 m)(5+2 m)(7+2 m) \right) + \left( (14 A - 35 B + 4 A m - 6 B m) \left( \left( \left( -\frac{1}{8} + \frac{i}{8} \right) \operatorname{Cos}\left[\frac{5}{2}(e+f x)\right] - \left( \frac{1}{8} + \frac{i}{8} \right) \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right] \right) \right) / \left( (5+2 m)(7+2 m) \right) + \left( (14 A - 35 B + 4 A m - 6 B m) \left( \left( \left( -\frac{1}{8} - \frac{i}{8} \right) \operatorname{Cos}\left[\frac{5}{2}(e+f x)\right] - \left( \frac{1}{8} - \frac{i}{8} \right) \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right] \right) \right) / \left( (5+2 m)(7+2 m) \right) + \frac{\left( \frac{1}{8} - \frac{i}{8} \right) B \operatorname{Cos}\left[\frac{7}{2}(e+f x)\right] - \left( \frac{1}{8} + \frac{i}{8} \right) B \operatorname{Sin}\left[\frac{7}{2}(e+f x)\right]}{7+2 m} + \frac{\left( \frac{1}{8} + \frac{i}{8} \right) B \operatorname{Cos}\left[\frac{7}{2}(e+f x)\right] - \left( \frac{1}{8} - \frac{i}{8} \right) B \operatorname{Sin}\left[\frac{7}{2}(e+f x)\right]}{7+2 m} \right)$$

**Problem 208: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sin[e + f x])^m (A + B \sin[e + f x])}{\sqrt{c - c \sin[e + f x]}} dx$$

Optimal (type 5, 118 leaves, 4 steps):

$$\frac{2 B \cos[e + f x] (a + a \sin[e + f x])^m}{f (1 + 2 m) \sqrt{c - c \sin[e + f x]}} + \left( (A + B) \cos[e + f x] \operatorname{Hypergeometric2F1}\left[1, \frac{1}{2} + m, \frac{3}{2} + m, \frac{1}{2} (1 + \sin[e + f x])\right] \right) \frac{(a + a \sin[e + f x])^m}{(f (1 + 2 m) \sqrt{c - c \sin[e + f x]})}$$

Result (type 6, 7013 leaves):

$$\begin{aligned} & - \left( \left( \sqrt{2} \left( \cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right] \right) \right. \right. \\ & \left. \left. (a + a \sin[e + f x])^m \left( \frac{A \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^{2m}}{\cos\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + f x\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + f x\right)\right]} + \right. \right. \right. \\ & \left. \left. \frac{B \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^{2m} \sin[e + f x]}{\cos\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + f x\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + f x\right)\right]} \right) \right) \\ & \left( 2 B \left( \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right] - \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^{-2m} \right) + \right. \\ & \left( A (1 + m) \operatorname{AppellF1}\left[1 + 2 m, 2 m, 1, 2 + 2 m, \frac{1}{2} \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right), \right. \right. \\ & \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right) \right) \right) / \\ & \left( -2 (1 + m) \operatorname{AppellF1}\left[1 + 2 m, 2 m, 1, 2 + 2 m, \frac{1}{2} \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right), \right. \right. \\ & \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \left( \operatorname{AppellF1}\left[2 + 2 m, 2 m, 2, 3 + 2 m, \right. \right. \right. \\ & \left. \left. \frac{1}{2} \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right), 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \right. \right. \\ & \left. \left. m \operatorname{AppellF1}\left[2 + 2 m, 1 + 2 m, 1, 3 + 2 m, \frac{1}{2} \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right), 1 - \right. \right. \right. \\ & \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right) \right) + \\ & \left( B (1 + m) \operatorname{AppellF1}\left[1 + 2 m, 2 m, 1, 2 + 2 m, \frac{1}{2} \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right), \right. \right. \\ & \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right) \right) \right) / \\ & \left( -2 (1 + m) \operatorname{AppellF1}\left[1 + 2 m, 2 m, 1, 2 + 2 m, \frac{1}{2} \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right), \right. \right. \\ & \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \left( \operatorname{AppellF1}\left[2 + 2 m, 2 m, 2, 3 + 2 m, \right. \right. \right. \end{aligned}$$



$$\begin{aligned}
 & \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \Bigg) + \\
 & m \operatorname{AppellF1} \left[ 2 + 2 m, 1 + 2 m, 1, 3 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \right. \\
 & \quad \left. \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \left( -1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \Bigg) \Bigg) / \\
 & \left( f (1 + 2 m) \sqrt{c - c \sin [e + f x]} \left( -\frac{1}{1 + 2 m} \sqrt{2} m \cos \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{-1+2 m} \right. \right. \\
 & \quad \left. \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right] \left( 2 B \left( \cos \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right] - \cos \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{-2 m} \right) + \right. \right. \\
 & \quad \left. \left( A (1 + m) \operatorname{AppellF1} \left[ 1 + 2 m, 2 m, 1, 2 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \right. \right. \right. \\
 & \quad \quad \left. \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \Bigg) / \\
 & \quad \left( -2 (1 + m) \operatorname{AppellF1} \left[ 1 + 2 m, 2 m, 1, 2 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), \right. \right. \\
 & \quad \left. \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \left( \operatorname{AppellF1} \left[ 2 + 2 m, 2 m, 2, 3 + 2 m, \right. \right. \right. \\
 & \quad \quad \left. \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \right. \\
 & \quad \quad \left. m \operatorname{AppellF1} \left[ 2 + 2 m, 1 + 2 m, 1, 3 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), \right. \right. \\
 & \quad \quad \left. \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \left( -1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) + \\
 & \quad \left( B (1 + m) \operatorname{AppellF1} \left[ 1 + 2 m, 2 m, 1, 2 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \right. \right. \\
 & \quad \quad \left. \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \Bigg) / \\
 & \quad \left( -2 (1 + m) \operatorname{AppellF1} \left[ 1 + 2 m, 2 m, 1, 2 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), \right. \right. \\
 & \quad \left. \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \left( \operatorname{AppellF1} \left[ 2 + 2 m, 2 m, 2, 3 + 2 m, \right. \right. \right. \\
 & \quad \quad \left. \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \right. \\
 & \quad \quad \left. m \operatorname{AppellF1} \left[ 2 + 2 m, 1 + 2 m, 1, 3 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), \right. \right. \\
 & \quad \quad \left. \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \left( -1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) + \\
 & \quad \frac{1}{1 + 2 m} \sqrt{2} \cos \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{2 m} \left( 2 B \left( -\frac{1}{2} \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right] - \right. \right. \\
 & \quad \quad \left. m \cos \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{-1-2 m} \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right] \right) - \\
 & \quad \left( A (1 + m) \operatorname{AppellF1} \left[ 1 + 2 m, 2 m, 1, 2 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \text{Csc}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) / \\
 & \left(2\left(-2(1+m) \text{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right],\right. \right. \\
 & \quad \left.1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \left(\text{AppellF1}\left[2+2m, 2m, 2, 3+2m,\right. \right. \\
 & \quad \left.\left.\frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \\
 & \quad m \text{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], \\
 & \quad \left.1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \left(-1 + \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right) + \\
 & \left(A(1+m) \text{Cot}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(-\frac{1}{2(2+2m)}(1+2m) \text{AppellF1}\left[2+2m,\right. \right. \right. \\
 & \quad \left.2m, 2, 3+2m, \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
 & \quad \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{2(2+2m)} \\
 & \quad m(1+2m) \text{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], \\
 & \quad \left.1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \\
 & \left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) / \left(-2(1+m) \text{AppellF1}\left[1+2m, 2m, 1, 2+2m,\right. \right. \\
 & \quad \left.\frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \left(\text{AppellF1}\left[2+2m,\right. \right. \\
 & \quad \left.2m, 2, 3+2m, \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \\
 & \quad m \text{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], \\
 & \quad \left.1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \left(-1 + \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right) + \\
 & \left(B(1+m) \text{Cot}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(-\frac{1}{2(2+2m)}(1+2m) \text{AppellF1}\left[2+2m,\right. \right. \right. \\
 & \quad \left.2m, 2, 3+2m, \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
 & \quad \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{2(2+2m)} \\
 & \quad m(1+2m) \text{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2}\left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], \\
 & \quad \left.1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \\
 & \left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) / \left(-2(1+m) \text{AppellF1}\left[1+2m, 2m, 1, 2+2m,\right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 + \left( \text{AppellF1} \left[ 2 + 2 m, \right. \right. \\
 & \quad \left. \left. 2 m, 2, 3 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \right. \\
 & \quad \left. m \text{AppellF1} \left[ 2 + 2 m, 1 + 2 m, 1, 3 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), \right. \right. \\
 & \quad \left. \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \left( -1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) - \\
 & \left( A (1 + m) \text{AppellF1} \left[ 1 + 2 m, 2 m, 1, 2 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), \right. \right. \\
 & \quad \left. \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \\
 & \left( \frac{1}{2} \left( \text{AppellF1} \left[ 2 + 2 m, 2 m, 2, 3 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), \right. \right. \right. \\
 & \quad \left. \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + m \text{AppellF1} \left[ 2 + 2 m, 1 + 2 m, 1, 3 + 2 m, \right. \right. \\
 & \quad \left. \left. \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \\
 & \text{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] - 2 (1 + m) \\
 & \left( -\frac{1}{2 (2 + 2 m)} (1 + 2 m) \text{AppellF1} \left[ 2 + 2 m, 2 m, 2, 3 + 2 m, \right. \right. \\
 & \quad \left. \left. \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \\
 & \text{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] - \frac{1}{2 (2 + 2 m)} m (1 + 2 m) \\
 & \text{AppellF1} \left[ 2 + 2 m, 1 + 2 m, 1, 3 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \right. \\
 & \quad \left. \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \text{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] \right) + \\
 & \left( -1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \left( -\frac{1}{3 + 2 m} (2 + 2 m) \text{AppellF1} \left[ 3 + 2 m, 2 m, \right. \right. \\
 & \quad \left. \left. 3, 4 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \\
 & \text{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] - \frac{1}{2 (3 + 2 m)} m (2 + 2 m) \\
 & \text{AppellF1} \left[ 3 + 2 m, 1 + 2 m, 2, 4 + 2 m, \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), \right. \\
 & \quad \left. 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \text{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right] + \\
 & m \left( -\frac{1}{2 (3 + 2 m)} (2 + 2 m) \text{AppellF1} \left[ 3 + 2 m, 1 + 2 m, 2, 4 + 2 m, \right. \right. \\
 & \quad \left. \left. \frac{1}{2} \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right), 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{4(3+2m)} \right. \\
 & (1+2m)(2+2m) \operatorname{AppellF1}\left[3+2m, 2+2m, 1, 4+2m, \right. \\
 & \left. \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
 & \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right] \Big/ \\
 & \left(-2(1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], \right. \\
 & \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \left(\operatorname{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right. \right. \\
 & \left. \left. \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \left. m \operatorname{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), \right. \right. \\
 & \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2 - \right. \\
 & \left. \left(B(1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], \right. \right. \\
 & \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2\right) \right. \\
 & \left. \left(\frac{1}{2}\left(\operatorname{AppellF1}\left[2+2m, 2m, 2, 3+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], \right. \right. \right. \\
 & \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + m \operatorname{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \right. \right. \right. \\
 & \left. \left. \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \right. \\
 & \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - 2(1+m) \right. \\
 & \left. \left(-\frac{1}{2(2+2m)}(1+2m) \operatorname{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right. \right. \right. \\
 & \left. \left. \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \right. \\
 & \left. \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{2(2+2m)}m(1+2m) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) \right. \\
 & \left. \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \left(-\frac{1}{3+2m}(2+2m) \operatorname{AppellF1}\left[3+2m, 2m, \right. \right. \right. \\
 & \left. \left. 3, 4+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]-\frac{1}{2(3+2 m)} m(2+2 m) \\
& \operatorname{AppellF1}\left[3+2 m, 1+2 m, 2, 4+2 m, \frac{1}{2}\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right),\right. \\
& \left.1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]+ \\
& m\left(-\frac{1}{2(3+2 m)}(2+2 m) \operatorname{AppellF1}\left[3+2 m, 1+2 m, 2, 4+2 m,\right.\right. \\
& \left.\left.\frac{1}{2}\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right), 1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \right. \\
& \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]-\frac{1}{4(3+2 m)}\right. \\
& \left.(1+2 m)(2+2 m) \operatorname{AppellF1}\left[3+2 m, 2+2 m, 1, 4+2 m,\right.\right. \\
& \left.\left.\frac{1}{2}\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right), 1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \right. \\
& \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)\right) / \\
& \left(-2(1+m) \operatorname{AppellF1}\left[1+2 m, 2 m, 1, 2+2 m, \frac{1}{2}\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right),\right.\right. \\
& \left.1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+\left(\operatorname{AppellF1}\left[2+2 m, 2 m, 2, 3+2 m,\right.\right. \\
& \left.\left.\frac{1}{2}\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right), 1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \right. \\
& \left. m \operatorname{AppellF1}\left[2+2 m, 1+2 m, 1, 3+2 m, \frac{1}{2}\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right),\right.\right. \\
& \left.1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\left(-1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^2\right)
\end{aligned}$$

**Problem 209: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a+a \sin [e+f x])^m (A+B \sin [e+f x])}{(c-c \sin [e+f x])^{3/2}} dx$$

Optimal (type 5, 134 leaves, 4 steps):

$$\begin{aligned}
& \frac{(A+B) \cos [e+f x] (a+a \sin [e+f x])^m}{2 f (c-c \sin [e+f x])^{3/2}}+ \\
& \left(\frac{(A(1-2 m)-B(3+2 m)) \cos [e+f x] \operatorname{Hypergeometric2F1}\left[1, \frac{1}{2}+m, \frac{3}{2}+m, \frac{1}{2}(1+\sin [e+f x])\right]}{(a+a \sin [e+f x])^m}\right) / \left(4 c f(1+2 m) \sqrt{c-c \sin [e+f x]}\right)
\end{aligned}$$

Result (type 6, 14818 leaves):

$$\begin{aligned}
 & - \left( \left( \cos \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right] \right)^{-2m} \left( \cos \left[ \frac{1}{2} (e + f x) \right] - \sin \left[ \frac{1}{2} (e + f x) \right] \right)^3 \right. \\
 & \quad \left. (a + a \sin[e + f x])^m \left( \frac{A \cos \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{2m}}{\left( \cos \left[ \frac{\pi}{4} + \frac{1}{2} \left( e - \frac{\pi}{2} + f x \right) \right] - \sin \left[ \frac{\pi}{4} + \frac{1}{2} \left( e - \frac{\pi}{2} + f x \right) \right] \right)^3} + \right. \\
 & \quad \left. \frac{B \cos \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{2m} \sin[e + f x]}{\left( \cos \left[ \frac{\pi}{4} + \frac{1}{2} \left( e - \frac{\pi}{2} + f x \right) \right] - \sin \left[ \frac{\pi}{4} + \frac{1}{2} \left( e - \frac{\pi}{2} + f x \right) \right] \right)^3} \right) \left( \frac{1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{2m} \right. \\
 & \quad \left( - \left( \left( A \operatorname{AppellF1} \left[ 1, -2m, 2m, 2, \cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) / \right. \right. \\
 & \quad \left( -m \left( \operatorname{AppellF1} \left[ 2, 1 - 2m, 2m, 3, \cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \operatorname{AppellF1} \left[ 2, -2m, 1 + 2m, 3, \right. \right. \right. \\
 & \quad \left. \left. \left. \cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \operatorname{AppellF1} \left[ 1, -2m, 2m, 2, \right. \right. \right. \\
 & \quad \left. \left. \left. \cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) - \\
 & \quad \left( B \operatorname{AppellF1} \left[ 1, -2m, 2m, 2, \cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) / \\
 & \quad \left( -m \left( \operatorname{AppellF1} \left[ 2, 1 - 2m, 2m, 3, \cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ 2, -2m, 1 + 2m, 3, \cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) + \right. \\
 & \quad \left. \operatorname{AppellF1} \left[ 1, -2m, 2m, 2, \cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\cot \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \\
 & \quad \left. \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \\
 & \quad \left( A \operatorname{AppellF1} \left[ 1, -2m, 2m, 2, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \\
 & \quad \left. \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) / \\
 & \quad \left( \operatorname{AppellF1} \left[ 1, -2m, 2m, 2, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] - \right. \\
 & \quad \left. m \left( \operatorname{AppellF1} \left[ 2, 1 - 2m, 2m, 3, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ 2, -2m, 1 + 2m, 3, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \right) \\
 & \quad \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \left( B \operatorname{AppellF1} \left[ 1, -2m, 2m, 2, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) / \\
 & \quad \left( \operatorname{AppellF1} \left[ 1, -2m, 2m, 2, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] - \right.
 \end{aligned}$$

$$\begin{aligned}
 & m \left( \text{AppellF1}\left[2, 1-2m, 2m, 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \quad \text{AppellF1}\left[2, -2m, 1+2m, 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \\
 & \left(4A(1+m) \text{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right)\right) / \\
 & \left( (1+2m) \left(-2(1+m) \text{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \left(\text{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + m \right. \right. \\
 & \quad \quad \left. \left. \text{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right)\right) + \\
 & \left(12B(1+m) \text{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right)\right) / \\
 & \left( (1+2m) \left(-2(1+m) \text{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \left(\text{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + m \right. \right. \\
 & \quad \quad \left. \left. \text{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right)\right)\right) / \\
 & \left(8\sqrt{2} f (c - c \sin[e + fx])^{3/2} \left(\frac{1}{4\sqrt{2}} m \left(\frac{1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}\right)^{-1+2m} \right. \right. \\
 & \quad \left. \left. - \left(\left(\sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right)\right) / \right. \right. \\
 & \quad \left. \left. \left(2 \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2\right) - \frac{\sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]}{2 \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)} \right) \right) \right)
 \end{aligned}$$









$$\begin{aligned}
& -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \Bigg) \Bigg) / \\
& \left( \text{AppellF1}\left[1, -2m, 2m, 2, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \right. \\
& m \left( \text{AppellF1}\left[2, 1-2m, 2m, 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
& \quad \text{AppellF1}\left[2, -2m, 1+2m, 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Bigg) + \\
& \left( B \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left( -\frac{1}{2} m \text{AppellF1}\left[2, 1-2m, 2m, 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \right. \\
& \quad \left. \left. \frac{1}{2} m \text{AppellF1}\left[2, -2m, 1+2m, 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right) \Bigg) / \\
& \left( \text{AppellF1}\left[1, -2m, 2m, 2, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \right. \\
& m \left( \text{AppellF1}\left[2, 1-2m, 2m, 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
& \quad \text{AppellF1}\left[2, -2m, 1+2m, 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Bigg) + \\
& \left( A \text{AppellF1}\left[1, -2m, 2m, 2, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
& \left( -m \left( \frac{4}{3} m \text{AppellF1}\left[3, 1-2m, 1+2m, 4, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \csc\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \right. \right. \\
& \quad \left. \frac{1}{3} (1-2m) \text{AppellF1}\left[3, 2-2m, 2m, 4, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \csc\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \right. \right. \\
& \quad \left. \frac{1}{3} (1+2m) \text{AppellF1}\left[3, -2m, 2+2m, 4, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \csc\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \Bigg) + \\
& \frac{1}{2} \text{AppellF1}\left[1, -2m, 2m, 2, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
& \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \left( \frac{1}{2} m \text{AppellF1}\left[2, \right. \right. \\
& \quad \left. \left. 1-2m, 2m, 3, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right)
\end{aligned}$$

$$\begin{aligned}
& \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \operatorname{Csc}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \frac{1}{2} m \operatorname{AppellF1}\left[2, \right. \\
& \quad \left.-2m, 1+2m, 3, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
& \quad \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \operatorname{Csc}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Big) \Big/ \\
& \quad \left(-m \left(\operatorname{AppellF1}\left[2, 1-2m, 2m, 3, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1}\left[2, -2m, 1+2m, 3, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right] + \operatorname{AppellF1}\left[1, -2m, 2m, 2, \right. \right. \\
& \quad \left. \left. \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2 + \right. \\
& \quad \left. \left(\operatorname{B} \operatorname{AppellF1}\left[1, -2m, 2m, 2, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \right. \\
& \quad \left. \left(-m \left(\frac{4}{3} m \operatorname{AppellF1}\left[3, 1-2m, 1+2m, 4, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \operatorname{Csc}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \right. \right. \\
& \quad \left. \left. \frac{1}{3} (1-2m) \operatorname{AppellF1}\left[3, 2-2m, 2m, 4, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \operatorname{Csc}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \right. \right. \\
& \quad \left. \left. \frac{1}{3} (1+2m) \operatorname{AppellF1}\left[3, -2m, 2+2m, 4, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \operatorname{Csc}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2 + \right. \\
& \quad \left. \frac{1}{2} \operatorname{AppellF1}\left[1, -2m, 2m, 2, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \left(\frac{1}{2} m \operatorname{AppellF1}\left[2, \right. \right. \right. \\
& \quad \left. \left. 1-2m, 2m, 3, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
& \quad \left. \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \operatorname{Csc}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \frac{1}{2} m \operatorname{AppellF1}\left[2, \right. \right. \\
& \quad \left. \left.-2m, 1+2m, 3, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
& \quad \left. \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \operatorname{Csc}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Big) \Big/ \\
& \quad \left(-m \left(\operatorname{AppellF1}\left[2, 1-2m, 2m, 3, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1}\left[2, -2m, 1+2m, 3, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right] + \operatorname{AppellF1}\left[1, -2m, 2m, 2, \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \left( \text{Cot}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Cot}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \\
 & \left( \text{A AppellF1}\left[1, -2m, 2m, 2, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(-\frac{1}{2}m \text{AppellF1}\left[2, 1-2m, 2m, 3, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], \right. \\
 & \quad \left. -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \\
 & \quad \frac{1}{2}m \text{AppellF1}\left[2, -2m, 1+2m, 3, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], \\
 & \quad \left. -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \\
 & \quad \frac{1}{2}m \left( \text{AppellF1}\left[2, 1-2m, 2m, 3, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], \right. \\
 & \quad \left. -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + \text{AppellF1}\left[2, -2m, 1+2m, \right. \\
 & \quad \left. 3, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \right) \\
 & \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - m \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \\
 & \left(-\frac{4}{3}m \text{AppellF1}\left[3, 1-2m, 1+2m, 4, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], \right. \\
 & \quad \left. -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \\
 & \quad \frac{1}{3}(1-2m) \text{AppellF1}\left[3, 2-2m, 2m, 4, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], \\
 & \quad \left. -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \\
 & \quad \frac{1}{3}(1+2m) \text{AppellF1}\left[3, -2m, 2+2m, 4, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], -\text{Tan}\left[\frac{1}{4}\right. \\
 & \quad \left. \left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left. \right) \Big) / \\
 & \left( \text{AppellF1}\left[1, -2m, 2m, 2, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \right. \\
 & \quad m \left( \text{AppellF1}\left[2, 1-2m, 2m, 3, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], \right. \\
 & \quad \left. -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + \text{AppellF1}\left[2, -2m, 1+2m, 3, \text{Tan}\left[\frac{1}{4}\left(-e + \right. \right. \right. \\
 & \quad \left. \left. \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \right) \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \\
 & \left( \text{B AppellF1}\left[1, -2m, 2m, 2, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(-\frac{1}{2}m \text{AppellF1}\left[2, 1-2m, 2m, 3, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], \right. \\
 & \quad \left. -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] -
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{2} m \operatorname{AppellF1}\left[2, -2 m, 1+2 m, 3, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] - \\
 & \frac{1}{2} m \left( \operatorname{AppellF1}\left[2, 1-2 m, 2 m, 3, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] + \operatorname{AppellF1}\left[2, -2 m, 1+2 m, \right. \right. \\
 & \quad \left. \left. 3, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \right) \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] - m \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \\
 & \left( -\frac{4}{3} m \operatorname{AppellF1}\left[3, 1-2 m, 1+2 m, 4, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] + \right. \\
 & \quad \frac{1}{3} (1-2 m) \operatorname{AppellF1}\left[3, 2-2 m, 2 m, 4, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] - \right. \\
 & \quad \left. \frac{1}{3} (1+2 m) \operatorname{AppellF1}\left[3, -2 m, 2+2 m, 4, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\tan\left[\frac{1}{4}\right. \right. \right. \\
 & \quad \left. \left. \left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] \right) \Bigg) / \\
 & \left( \operatorname{AppellF1}\left[1, -2 m, 2 m, 2, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] - \right. \\
 & \quad \left. m \left( \operatorname{AppellF1}\left[2, 1-2 m, 2 m, 3, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] + \operatorname{AppellF1}\left[2, -2 m, 1+2 m, 3, \tan\left[\frac{1}{4}\left(-e+\right. \right. \right. \right. \\
 & \quad \left. \left. \left.\frac{\pi}{2}-f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 - \right. \\
 & \left. \left( 2 A (1+m) \operatorname{AppellF1}\left[1+2 m, 2 m, 1, 2+2 m, \frac{1}{2}-\frac{1}{2} \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. 1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Csc}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] \right) \Bigg) / \\
 & \left( (1+2 m) \left( -2 (1+m) \operatorname{AppellF1}\left[1+2 m, 2 m, 1, 2+2 m, \frac{1}{2}-\frac{1}{2} \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. 1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] + \left( \operatorname{AppellF1}\left[2+2 m, 2 m, 2, 3+2 m, \right. \right. \right. \right. \\
 & \quad \left. \left. \frac{1}{2}-\frac{1}{2} \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, 1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] + \right. \\
 & \quad \left. \left. m \operatorname{AppellF1}\left[2+2 m, 1+2 m, 1, 3+2 m, \frac{1}{2}-\frac{1}{2} \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. 1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \right) \left( -1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) \right) \Bigg) +
 \end{aligned}$$







$$\begin{aligned}
 & \left( 4 A (1+m) \operatorname{AppellF1}\left[1+2 m, 2 m, 1, 2+2 m, \frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right. \right. \\
 & \quad \left. \left. 1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Cot}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\left(-1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) \right. \\
 & \quad \left. \left(\frac{1}{2}\left(\operatorname{AppellF1}\left[2+2 m, 2 m, 2, 3+2 m, \frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. 1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+m \operatorname{AppellF1}\left[2+2 m, 1+2 m, 1, 3+2 m,\right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, 1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]-2(1+m) \right. \\
 & \quad \left. \left(-\frac{1}{2(2+2 m)}(1+2 m) \operatorname{AppellF1}\left[2+2 m, 2 m, 2, 3+2 m,\right. \right. \right. \\
 & \quad \quad \left. \left. \frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, 1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \right. \\
 & \quad \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]-\frac{1}{2(2+2 m)} m(1+2 m) \right. \\
 & \quad \quad \left. \operatorname{AppellF1}\left[2+2 m, 1+2 m, 1, 3+2 m, \frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, 1-\right. \right. \\
 & \quad \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right) \right. \\
 & \quad \left. \left(-1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\left(-\frac{1}{3+2 m}(2+2 m) \operatorname{AppellF1}\left[3+2 m,\right. \right. \right. \\
 & \quad \quad \left. \left. 2 m, 3, 4+2 m, \frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, 1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \right. \\
 & \quad \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]-\frac{1}{2(3+2 m)} \right. \\
 & \quad \quad \left. m(2+2 m) \operatorname{AppellF1}\left[3+2 m, 1+2 m, 2, 4+2 m, \frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right. \right. \\
 & \quad \quad \left. \left. 1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right) \right. \\
 & \quad \left. m\left(-\frac{1}{2(3+2 m)}(2+2 m) \operatorname{AppellF1}\left[3+2 m, 1+2 m, 2, 4+2 m,\right. \right. \right. \\
 & \quad \quad \left. \left. \frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, 1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \right. \\
 & \quad \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]-\frac{1}{4(3+2 m)} \right. \\
 & \quad \quad \left. (1+2 m)(2+2 m) \operatorname{AppellF1}\left[3+2 m, 2+2 m, 1, 4+2 m,\right. \right. \\
 & \quad \quad \left. \left. \frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, 1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \right. \\
 & \quad \quad \left. \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)\right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( (1+2m) \left( -2(1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], \right. \right. \\
 & \quad \left. \left. 1 - \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \left( \operatorname{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], 1 - \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \quad \left. m \operatorname{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], \right. \\
 & \quad \left. \left. 1 - \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \left( -1 + \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right)^2 - \\
 & \left( 12B(1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], \right. \\
 & \quad \left. 1 - \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Cot}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left( -1 + \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right)^2 \\
 & \left( \frac{1}{2} \left( \operatorname{AppellF1}\left[2+2m, 2m, 2, 3+2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], \right. \right. \\
 & \quad \left. \left. 1 - \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + m \operatorname{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \right. \right. \\
 & \quad \quad \left. \left. \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], 1 - \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) \\
 & \operatorname{Sec}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right] - 2(1+m) \\
 & \left( -\frac{1}{2(2+2m)} (1+2m) \operatorname{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right. \right. \\
 & \quad \left. \left. \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], 1 - \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \\
 & \operatorname{Sec}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{2(2+2m)} m(1+2m) \\
 & \operatorname{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], 1 - \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right] \right) + \\
 & \left( -1 + \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \left( -\frac{1}{3+2m} (2+2m) \operatorname{AppellF1}\left[3+2m, \right. \right. \\
 & \quad \left. \left. 2m, 3, 4+2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], 1 - \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \\
 & \operatorname{Sec}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{2(3+2m)} \\
 & m(2+2m) \operatorname{AppellF1}\left[3+2m, 1+2m, 2, 4+2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], \\
 & \quad \left. 1 - \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right] + \\
 & m \left( -\frac{1}{2(3+2m)} (2+2m) \operatorname{AppellF1}\left[3+2m, 1+2m, 2, 4+2m, \right. \right.
 \end{aligned}$$

$$\frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right]^2$$

$$\operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{1}{4(3+2m)}$$

$$(1+2m)(2+2m) \operatorname{AppellF1}\left[3+2m, 2+2m, 1, 4+2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right]$$

$$\operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)\right) /$$

$$\left((1+2m)\left(-2(1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \left(\operatorname{AppellF1}\left[2+2m, 2m, 2, 3+2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + m \operatorname{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right]\right)\right)\right)\right)$$

**Problem 210: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \operatorname{Sin}[e + f x])^m (A + B \operatorname{Sin}[e + f x])}{(c - c \operatorname{Sin}[e + f x])^{5/2}} dx$$

Optimal (type 5, 134 leaves, 4 steps):

$$\frac{(A + B) \operatorname{Cos}[e + f x] (a + a \operatorname{Sin}[e + f x])^m}{4 f (c - c \operatorname{Sin}[e + f x])^{5/2}} + \left( (A(3 - 2m) - B(5 + 2m)) \operatorname{Cos}[e + f x] \operatorname{Hypergeometric2F1}\left[2, \frac{1}{2} + m, \frac{3}{2} + m, \frac{1}{2} (1 + \operatorname{Sin}[e + f x])\right] (a + a \operatorname{Sin}[e + f x])^m \right) / \left( 16 c^2 f (1 + 2m) \sqrt{c - c \operatorname{Sin}[e + f x]} \right)$$

Result (type 6, 28451 leaves): Display of huge result suppressed!

**Problem 214: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int (a + a \operatorname{Sin}[e + f x])^m (A + B \operatorname{Sin}[e + f x]) (c - c \operatorname{Sin}[e + f x])^{-1-m} dx$$

Optimal (type 5, 163 leaves, 5 steps):

$$\frac{(A+B) \cos[e+fx] (a+a \sin[e+fx])^m (c-c \sin[e+fx])^{-1-m}}{f(1+2m)} - \frac{1}{f(1+2m)}$$

$$2^{\frac{1}{2}-m} B \cos[e+fx] \operatorname{Hypergeometric2F1}\left[\frac{1}{2}(1+2m), \frac{1}{2}(1+2m), \frac{1}{2}(3+2m), \frac{1}{2}(1+\sin[e+fx])\right]$$

$$(1-\sin[e+fx])^{\frac{1}{2}+m} (a+a \sin[e+fx])^m (c-c \sin[e+fx])^{-1-m}$$

Result (type 6, 6197 leaves):

$$-\left(\left(2^{-1-3m} \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{-2m} \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right.\right.$$

$$\left.\left(\cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right]\right)^{-2(-1-m)} (a+a \sin[e+fx])^m (c-c \sin[e+fx])^{-1-m}\right.$$

$$\left.\left(A \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \left(\cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] - \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]\right)^{-2-2m} +\right.$$

$$\left.\left.B \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \sin[e+fx]\right.\right.$$

$$\left.\left(\cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] - \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]\right)^{-2-2m}\right.$$

$$\left.\left(\frac{1}{1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}\right)^{2m} \left(\frac{\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]}{1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}\right)^{-2m}\right.$$

$$\left.\left(\left(8B(-3+2m) \operatorname{AppellF1}\left[\frac{1}{2}-m, -2m, 1, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right]^2,\right.\right.\right.$$

$$\left.\left.-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \left(1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{2m}\right)\right)/$$

$$\left(\left(-1+2m\right) \left(1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) \left(\left(-3+2m\right) \operatorname{AppellF1}\left[\frac{1}{2}-m, -2m,\right.\right.\right.$$

$$\left.\left.1, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) +\right.$$

$$\left.\left.2\left(2m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2m, 1, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right]^2,\right.\right.\right.$$

$$\left.\left.-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) + \operatorname{AppellF1}\left[\frac{3}{2}-m, -2m, 2, \frac{5}{2}-m,\right.\right.$$

$$\left.\left.\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\right) -$$

$$\frac{1}{-1+4m^2} (A+B) \left(\left(-1+2m\right) \operatorname{Hypergeometric2F1}\left[-\frac{1}{2}-m, -2m, \frac{1}{2}-m,\right.\right.$$

$$\left.\left.\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) + (1+2m) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}-m,\right.\right.$$

$$\left.\left.-2m, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\right)/$$

$$\begin{aligned} & \left( f \left( -2^{-3-3m} \operatorname{Csc} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \left( \frac{1}{1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{2m} \right. \right. \\ & \quad \left. \left. \left( \frac{\operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]}{1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{-2m} \right. \right. \\ & \quad \left( \left( 8 B (-3 + 2 m) \operatorname{AppellF1} \left[ \frac{1}{2} - m, -2 m, 1, \frac{3}{2} - m, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\ & \quad \quad \left. \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \left( 1 - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{2m} \right) \right) / \\ & \quad \left( (-1 + 2 m) \left( 1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \left( (-3 + 2 m) \operatorname{AppellF1} \left[ \frac{1}{2} - m, -2 m, \right. \right. \right. \\ & \quad \quad \left. \left. \left. 1, \frac{3}{2} - m, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \left( 2 m \operatorname{AppellF1} \left[ \right. \right. \right. \\ & \quad \quad \left. \left. \left. \frac{3}{2} - m, 1 - 2 m, 1, \frac{5}{2} - m, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) + \right. \\ & \quad \quad \left. \operatorname{AppellF1} \left[ \frac{3}{2} - m, -2 m, 2, \frac{5}{2} - m, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\ & \quad \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) - \frac{1}{-1 + 4 m^2} \\ & \quad (A + B) \left( (-1 + 2 m) \operatorname{Hypergeometric2F1} \left[ -\frac{1}{2} - m, -2 m, \frac{1}{2} - m, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) + \\ & \quad (1 + 2 m) \operatorname{Hypergeometric2F1} \left[ \frac{1}{2} - m, -2 m, \frac{3}{2} - \right. \\ & \quad \quad \left. m, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \left. \right) - \\ & \quad \left( 2^{-1-3m} m \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \left( \frac{1}{1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{1+2m} \right. \right. \\ & \quad \left. \left. \left( \frac{\operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]}{1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{-2m} \right. \right. \\ & \quad \left( \left( 8 B (-3 + 2 m) \operatorname{AppellF1} \left[ \frac{1}{2} - m, -2 m, 1, \frac{3}{2} - m, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\ & \quad \quad \left. \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \left( 1 - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{2m} \right) \right) / \\ & \quad \left( (-1 + 2 m) \left( 1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \left( (-3 + 2 m) \operatorname{AppellF1} \left[ \frac{1}{2} - m, -2 m, \right. \right. \right. \\ & \quad \quad \left. \left. \left. 1, \frac{3}{2} - m, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \left( 2 m \operatorname{AppellF1} \left[ \right. \right. \right. \\ & \quad \quad \left. \left. \left. \frac{3}{2} - m, 1 - 2 m, 1, \frac{5}{2} - m, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) + \right. \\ & \quad \quad \left. \operatorname{AppellF1} \left[ \frac{3}{2} - m, -2 m, 2, \frac{5}{2} - m, \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\ & \quad \quad \left. \left. - \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Tan} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \left. \right) \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) - \frac{1}{-1+4m^2} \\
 (A+B) & \left( (-1+2m) \text{Hypergeometric2F1}\left[-\frac{1}{2}-m, -2m, \frac{1}{2}-m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \left. (1+2m) \text{Hypergeometric2F1}\left[\frac{1}{2}-m, -2m, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) - \\
 2^{-3m} m \cot & \left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left( \frac{1}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{2m} \\
 & \left( \frac{\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{-1-2m} \\
 & \left( -\frac{\sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{2\left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2} + \frac{\sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{4\left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)} \right) \\
 & \left( \left( 8B(-3+2m) \text{AppellF1}\left[\frac{1}{2}-m, -2m, 1, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{2m} \right) \right) / \\
 & \left( (-1+2m) \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \left( (-3+2m) \text{AppellF1}\left[\frac{1}{2}-m, -2m, \right. \right. \right. \\
 & \left. \left. \left. \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left( 2m \text{AppellF1}\left[\frac{3}{2}-m, 1-2m, 1, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \text{AppellF1}\left[\frac{3}{2}-m, -2m, 2, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) - \frac{1}{-1+4m^2} \\
 (A+B) & \left( (-1+2m) \text{Hypergeometric2F1}\left[-\frac{1}{2}-m, -2m, \frac{1}{2}-m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \left. (1+2m) \text{Hypergeometric2F1}\left[\frac{1}{2}-m, -2m, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + \\
 2^{-1-3m} m \cot & \left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left( \frac{1}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{2m} \\
 & \left( \frac{\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{-2m}
 \end{aligned}$$





$$\begin{aligned}
 & \left( (-1+2m) \left( 1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right) \left( (-3+2m) \operatorname{AppellF1} \left[ \frac{1}{2} - m, -2m, \right. \right. \right. \\
 & \quad \left. \left. \left. 1, \frac{3}{2} - m, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] + 2 \left( 2m \operatorname{AppellF1} \left[ \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{3}{2} - m, 1 - 2m, 1, \frac{5}{2} - m, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right) + \right. \\
 & \quad \left. \operatorname{AppellF1} \left[ \frac{3}{2} - m, -2m, 2, \frac{5}{2} - m, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right) \right) - \\
 & \left( 8Bm(-3+2m) \operatorname{AppellF1} \left[ \frac{1}{2} - m, -2m, 1, \frac{3}{2} - m, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right. \\
 & \quad \left. \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^3 \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right)^{-1+2m} \right) / \\
 & \left( (-1+2m) \left( 1 + \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right) \left( (-3+2m) \operatorname{AppellF1} \left[ \frac{1}{2} - m, -2m, 1, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{3}{2} - m, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] + 2 \left( 2m \operatorname{AppellF1} \left[ \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{3}{2} - m, 1 - 2m, 1, \frac{5}{2} - m, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right) + \right. \\
 & \quad \left. \operatorname{AppellF1} \left[ \frac{3}{2} - m, -2m, 2, \frac{5}{2} - m, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right) \right) - \\
 & \left( 8B(-3+2m) \operatorname{AppellF1} \left[ \frac{1}{2} - m, -2m, 1, \frac{3}{2} - m, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \left( 1 - \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right)^{2m} \right. \\
 & \quad \left. \left( \left( 2m \operatorname{AppellF1} \left[ \frac{3}{2} - m, 1 - 2m, 1, \frac{5}{2} - m, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] + \operatorname{AppellF1} \left[ \frac{3}{2} - m, -2m, 2, \frac{5}{2} - m, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right) \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right) \\
 & \quad \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right] + (-3+2m) \left( -\frac{1}{\frac{3}{2}-m} \left( \frac{1}{2}-m \right) m \operatorname{AppellF1} \left[ \frac{3}{2} - m, \right. \right. \\
 & \quad \left. \left. 1 - 2m, 1, \frac{5}{2} - m, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right) \\
 & \quad \operatorname{Sec} \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right] - \frac{1}{2 \left( \frac{3}{2}-m \right)} \left( \frac{1}{2}-m \right) \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \left. \left. \left. \frac{3}{2} - m, -2m, 1, \frac{5}{2} - m, \tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( \frac{3}{2} - m, -2m, 2, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right. \\
 & \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) + 2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \\
 & \left( -\frac{1}{\frac{5}{2} - m} \left(\frac{3}{2} - m\right) m \operatorname{AppellF1}\left[\frac{5}{2} - m, 1 - 2m, 2, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \\
 & \quad \frac{1}{\frac{5}{2} - m} \left(\frac{3}{2} - m\right) \operatorname{AppellF1}\left[\frac{5}{2} - m, -2m, 3, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \right. \\
 & \quad \left. 2m \left( -\frac{1}{2\left(\frac{5}{2} - m\right)} \left(\frac{3}{2} - m\right) \operatorname{AppellF1}\left[\frac{5}{2} - m, 1 - 2m, 2, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \right. \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{1}{2\left(\frac{5}{2} - m\right)} (1 - 2m) \left(\frac{3}{2} - m\right) \operatorname{AppellF1}\left[\frac{5}{2} - m, \right. \right. \\
 & \quad \left. \left. 2 - 2m, 1, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right)\right)\right)\right) / \\
 & \left( (-1 + 2m) \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \left( (-3 + 2m) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, \right. \right. \right. \right. \\
 & \quad \left. \left. 1, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \quad \left. 2 \left( 2m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 1, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 2, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \right. \right. \right. \right. \\
 & \quad \quad \quad \left. \left. \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^2 \right) - \\
 & \frac{1}{-1 + 4m^2} (A + B) \left( \frac{1}{2} (1 + 2m) \operatorname{Hypergeometric2F1}\left[\frac{1}{2} - m, -2m, \frac{3}{2} - m, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \right. \\
 & \quad \left. \frac{1}{2} \left(-\frac{1}{2} - m\right) (-1 + 2m) \operatorname{Csc}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right. \\
 & \quad \left. \left( -\operatorname{Hypergeometric2F1}\left[-\frac{1}{2} - m, -2m, \frac{1}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned} & \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right)^{2m} + \frac{1}{2}\left(\frac{1}{2} - m\right)(1 + 2m) \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \\ & \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left(-\operatorname{Hypergeometric2F1}\left[\frac{1}{2} - m, -2m, \frac{3}{2} - m, \right. \right. \\ & \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right)^{2m}\right) \right) \right) \end{aligned}$$

**Problem 215: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int (a + a \sin[e + fx])^m (A + B \sin[e + fx]) (c - c \sin[e + fx])^{-m} dx$$

Optimal (type 5, 158 leaves, 5 steps):

$$\begin{aligned} & \frac{1}{f(1+2m)} 2^{\frac{1}{2}-m} c (A+2Bm) \cos[e+fx] \\ & \operatorname{Hypergeometric2F1}\left[\frac{1}{2}(1+2m), \frac{1}{2}(1+2m), \frac{1}{2}(3+2m), \frac{1}{2}(1+\sin[e+fx])\right] \\ & (1-\sin[e+fx])^{\frac{1}{2}+m} (a+a\sin[e+fx])^m (c-c\sin[e+fx])^{-1-m} - \\ & \frac{B \cos[e+fx] (a+a\sin[e+fx])^m (c-c\sin[e+fx])^{-m}}{f} \end{aligned}$$

Result (type 6, 15390 leaves):

$$\begin{aligned} & - \left( \left( 2^{2-3m} (-3+2m) \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \right)^{-2m} \right. \\ & \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^{2m} (a+a\sin[e+fx])^m (c-c\sin[e+fx])^{-m} \\ & \left( A \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \right)^{2m} \left( \cos\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + fx\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + fx\right)\right] \right)^{-2m} + \\ & B \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^{2m} \sin[e+fx] \\ & \left( \cos\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + fx\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + fx\right)\right] \right)^{-2m} \\ & \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left( \frac{\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{-2m} \left( \frac{1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{2m} \\ & - \left( \left( \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 1, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \right. \\ & \left. \left. \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2 \right) / \left( (-3+2m) \right. \right. \\ & \left. \left. \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 1, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right) + \end{aligned}$$



$$\begin{aligned}
 & 3 \times 2^{1-3m} (-3+2m) \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \\
 & \left(\frac{\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}\right)^{-2m} \left(\frac{1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}\right)^{2m} \\
 & \left(-\left(\operatorname{AppellF1}\left[\frac{1}{2}-m, -2m, 1, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-\right.\right.\right.\right. \right. \\
 & \quad \left.\left.\left.\left. fx\right)\right]^2\right]\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^2\right)/\left((-3+2m) \operatorname{AppellF1}\left[\frac{1}{2}-m, \right.\right.\right. \right. \\
 & \quad \left.\left.\left. -2m, 1, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right)+ \right. \\
 & \quad \left. 2\left(2m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2m, 1, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right.\right.\right. \right. \\
 & \quad \left.\left.\left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]+\operatorname{AppellF1}\left[\frac{3}{2}-m, -2m, 2, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\right.\right.\right. \right. \right. \\
 & \quad \left.\left.\left. \frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)- \\
 & \left(\operatorname{B AppellF1}\left[\frac{1}{2}-m, -2m, 1, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right.\right. \right. \\
 & \quad \left.\left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^2\right)/\left((-3+2m) \operatorname{AppellF1}\left[\right.\right. \right. \\
 & \quad \left.\left.\left. \frac{1}{2}-m, -2m, 1, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right)+2 \right. \\
 & \quad \left. \left(2m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2m, 1, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right.\right.\right. \right. \\
 & \quad \left.\left.\left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]+\operatorname{AppellF1}\left[\frac{3}{2}-m, -2m, 2, \frac{5}{2}-m, \operatorname{Tan}\left[\right.\right.\right. \right. \\
 & \quad \left.\left.\left. \frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)+ \\
 & \left(8 \operatorname{B AppellF1}\left[\frac{1}{2}-m, -2m, 2, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right.\right. \right. \\
 & \quad \left.\left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\right)/ \\
 & \left(\left(-3+2m\right) \operatorname{AppellF1}\left[\frac{1}{2}-m, -2m, 2, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right.\right. \right. \\
 & \quad \left.\left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right)+4\left(m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2m, 2, \frac{5}{2}-m, \right.\right. \right. \\
 & \quad \left.\left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]+\operatorname{AppellF1}\left[\frac{3}{2}-m, \right.\right. \right. \\
 & \quad \left.\left. -2m, 3, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \\
 & \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2-\left(8 \operatorname{B AppellF1}\left[\frac{1}{2}-m, -2m, 3, \frac{3}{2}-m, \right.\right. \right. \\
 & \quad \left.\left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right)/\left(\left(-3+2m\right) \operatorname{AppellF1}\left[\right.\right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Big] + 2 \\
 & \left( 2m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 3, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 3 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 4, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Big) + \\
 & \frac{1}{(-1 + 2m) \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^3} 2^{-3m} (-3 + 2m) \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \\
 & \left( \frac{\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{-2m} \\
 & \left( \frac{1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{2m} \\
 & \left( - \left( \left( \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 1, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2 \right) \right) / \\
 & \quad \left( (-3 + 2m) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 1, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left( 2m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 1, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 2, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) - \\
 & \quad \left( \operatorname{B AppellF1}\left[\frac{1}{2} - m, -2m, 1, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right)^2 \\
 & \quad \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2 \Big) / \left( (-3 + 2m) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, \right. \right. \\
 & \quad \left. \left. 1, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \quad \left. 2 \left( 2m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 1, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 2, \frac{5}{2} - m, \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + \\
 & \quad \left( 8 \operatorname{B AppellF1}\left[\frac{1}{2} - m, -2m, 2, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\left/\left((-3+2 m) \operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m, 2, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+4\left(m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2 m, 2, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+\operatorname{AppellF1}\left[\frac{3}{2}-m,-2 m, 3, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)-\left(8 B \operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m, 3, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\left/\left((-3+2 m) \operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m, 3, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+2\left(2 m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2 m, 3, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+3 \operatorname{AppellF1}\left[\frac{3}{2}-m,-2 m, 4, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\right)\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)-\frac{1}{(-1+2 m)\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^3} 2^{3-3 m} m(-3+2 m) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\left(\frac{\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}\right)^{-1-2 m}\left(\frac{1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}\right)^{2 m}\left(-\frac{\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{2\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^2}+\frac{\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{4\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)}\right)\left(-\left(\left(\operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m, 1, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\left/\left((-3+2 m) \operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m, 1, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+2\left(2 m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2 m, 1, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & \text{AppellF1}\left[\frac{3}{2}-m, -2m, 2, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \Bigg) - \\
 & \left( \text{B AppellF1}\left[\frac{1}{2}-m, -2m, 1, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\
 & \quad \left. \left(1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^2 \right) \Bigg) / \left( (-3+2m) \text{AppellF1}\left[\frac{1}{2}-m, -2m, \right. \right. \\
 & \quad \left. \left. 1, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\
 & \quad \left. 2\left(2m \text{AppellF1}\left[\frac{3}{2}-m, 1-2m, 1, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \text{AppellF1}\left[\frac{3}{2}-m, -2m, 2, \frac{5}{2}-m, \right. \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) + \\
 & \left( 8 \text{B AppellF1}\left[\frac{1}{2}-m, -2m, 2, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \left(1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) \right) \Bigg) / \left( (-3+2m) \text{AppellF1}\left[ \right. \right. \\
 & \quad \left. \left. \frac{1}{2}-m, -2m, 2, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\
 & \quad \left. 4\left(m \text{AppellF1}\left[\frac{3}{2}-m, 1-2m, 2, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \text{AppellF1}\left[\frac{3}{2}-m, -2m, 3, \frac{5}{2}-m, \right. \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) - \\
 & \left( 8 \text{B AppellF1}\left[\frac{1}{2}-m, -2m, 3, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \Bigg) / \left( (-3+2m) \text{AppellF1}\left[\frac{1}{2}-m, -2m, 3, \frac{3}{2}-m, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 2\left(2m \text{AppellF1}\left[\frac{3}{2}-m, \right. \right. \right. \\
 & \quad \quad \left. \left. 1-2m, 3, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\
 & \quad \quad \left. 3 \text{AppellF1}\left[\frac{3}{2}-m, -2m, 4, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \Bigg) + \\
 & \frac{1}{(-1+2m) \left(1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^3} 2^{3-3m} m (-3+2m) \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \\
 & \left( \frac{\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]}{1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2} \right)^{-2m}
 \end{aligned}$$



$$\begin{aligned}
 & \left( \frac{1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{-1+2m} \\
 & \left( - \left( \left( \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right)^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right) / \right. \\
 & \quad \left. \left( 2 \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2 \right) - \frac{\sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]}{2 \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)} \right) \right) \\
 & \left( - \left( \left( \text{AppellF1}\left[\frac{1}{2} - m, -2m, 1, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2 \right) / \right. \right. \\
 & \quad \left( (-3 + 2m) \text{AppellF1}\left[\frac{1}{2} - m, -2m, 1, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left( 2m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 1, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. \text{AppellF1}\left[\frac{3}{2} - m, -2m, 2, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) - \right. \\
 & \quad \left( \text{B AppellF1}\left[\frac{1}{2} - m, -2m, 1, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right)^2 \\
 & \quad \left( 1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^2 \right) / \left( (-3 + 2m) \text{AppellF1}\left[\frac{1}{2} - m, -2m, \right. \right. \\
 & \quad \left. \left. 1, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \quad \left. 2 \left( 2m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 1, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \text{AppellF1}\left[\frac{3}{2} - m, -2m, 2, \frac{5}{2} - m, \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + \\
 & \quad \left( 8 \text{B AppellF1}\left[\frac{1}{2} - m, -2m, 2, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right) / \left( (-3 + 2m) \text{AppellF1}\left[\right. \right. \\
 & \quad \left. \left. \frac{1}{2} - m, -2m, 2, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \quad \left. 4 \left( m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 2, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \text{AppellF1}\left[\frac{3}{2} - m, -2m, 3, \frac{5}{2} - m, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \\
 & \left( 8 \text{B AppellF1}\left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) / \left( (-3 + 2m) \text{AppellF1}\left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left( 2m \text{AppellF1}\left[\frac{3}{2} - m, \right. \right. \right. \\
 & \left. \left. \left. 1 - 2m, 3, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \left. \left. 3 \text{AppellF1}\left[\frac{3}{2} - m, -2m, 4, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + \\
 & \frac{1}{(-1 + 2m) \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^3} 2^{2-3m} (-3 + 2m) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \\
 & \left( \frac{\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{-2m} \\
 & \left( \frac{1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{2m} \\
 & \left( - \left( \left( \text{A AppellF1}\left[\frac{1}{2} - m, -2m, 1, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right. \right. \right. \\
 & \left. \left. \left. \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right) \right) / \left( (-3 + 2m) \text{AppellF1}\left[\frac{1}{2} - m, -2m, 1, \frac{3}{2} - m, \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left( 2m \text{AppellF1}\left[\frac{3}{2} - m, \right. \right. \right. \right. \\
 & \left. \left. \left. 1 - 2m, 1, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \left. \left. \left. \text{AppellF1}\left[\frac{3}{2} - m, -2m, 2, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) - \\
 & \left( \text{B AppellF1}\left[\frac{1}{2} - m, -2m, 1, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right)^2 \\
 & \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right) / \\
 & \left( (-3 + 2m) \text{AppellF1}\left[\frac{1}{2} - m, -2m, 1, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left( 2m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 1, \right. \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
& -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 2, \frac{5}{2} - m, \right. \\
& \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \\
& \left(4 B \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 2, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) / \\
& \left( (-3 + 2m) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 2, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 4\left(m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 2, \right. \right. \right. \\
& \left. \left. \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
& \left. \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 3, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \\
& \left(8 B \left(-\frac{1}{\frac{3}{2} - m}\left(\frac{1}{2} - m\right) m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 2, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \\
& \left. \frac{1}{\frac{3}{2} - m}\left(\frac{1}{2} - m\right) \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 3, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) \\
& \left. \left. \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right) / \left((-3 + 2m) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, \right. \right. \right. \\
& \left. \left. 2, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
& \left. 4\left(m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 2, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 3, \frac{5}{2} - m, \right. \right. \\
& \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) - \\
& \left(8 B \left(-\frac{1}{\frac{3}{2} - m}\left(\frac{1}{2} - m\right) m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 3, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \\
& \left. \frac{1}{2\left(\frac{3}{2} - m\right)} 3\left(\frac{1}{2} - m\right) \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 4, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right)
\end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right)\right)\right) / \\
 & \left( (-3+2m) \operatorname{AppellF1}\left[\frac{1}{2}-m, -2m, 3, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right], \right. \\
 & \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 2\left( 2m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2m, 3, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right], -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\
 & \quad \left. 3 \operatorname{AppellF1}\left[\frac{3}{2}-m, -2m, 4, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right], \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) + \\
 & \left( A \operatorname{AppellF1}\left[\frac{1}{2}-m, -2m, 1, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right], -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \\
 & \left( 1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right)^2 \left( \left( 2m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2m, 1, \frac{5}{2}-m, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right], -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}-m, \right. \right. \\
 & \quad \left. \left. -2m, 2, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right], -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + (-3+2m) \\
 & \left( -\frac{1}{\frac{3}{2}-m} \left(\frac{1}{2}-m\right) m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2m, 1, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right], \right. \\
 & \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \right. \\
 & \quad \left. \frac{1}{2\left(\frac{3}{2}-m\right)} \left(\frac{1}{2}-m\right) \operatorname{AppellF1}\left[\frac{3}{2}-m, -2m, 2, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right], \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right)\right) + \\
 & 2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \left( -\frac{1}{\frac{5}{2}-m} \left(\frac{3}{2}-m\right) m \operatorname{AppellF1}\left[\frac{5}{2}-m, 1-2m, \right. \right. \\
 & \quad \left. \left. 2, \frac{7}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right], -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \frac{1}{\frac{5}{2}-m} \\
 & \left( \frac{3}{2}-m \right) \operatorname{AppellF1}\left[\frac{5}{2}-m, -2m, 3, \frac{7}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right],
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] + \\
 & 2 m\left(-\frac{1}{2\left(\frac{5}{2}-m\right)}\left(\frac{3}{2}-m\right) \operatorname{AppellF1}\left[\frac{5}{2}-m, 1-2 m, 2, \frac{7}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-\right.\right.\right.\right. \\
 & \quad \left.\left.\left.\left.f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right. \right. \\
 & \quad \left.\left.+\frac{1}{2\left(\frac{5}{2}-m\right)}(1-2 m)\left(\frac{3}{2}-m\right) \operatorname{AppellF1}\left[\frac{5}{2}-m, 2-2 m, 1, \frac{7}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right. \right. \\
 & \quad \left.\left.\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)\right)\right) / \\
 & \left(\left(-3+2 m\right) \operatorname{AppellF1}\left[\frac{1}{2}-m, -2 m, 1, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right. \\
 & \quad \left.+\left(2 m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2 m, 1, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right. \right. \\
 & \quad \left.+\operatorname{AppellF1}\left[\frac{3}{2}-m, -2 m, 2, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) + \\
 & \left(\operatorname{B AppellF1}\left[\frac{1}{2}-m, -2 m, 1, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right) \\
 & \left(\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^2\left(\left(2 m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2 m, 1, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right. \right. \right. \\
 & \quad \left.+\operatorname{AppellF1}\left[\frac{3}{2}-m, -2 m, 2, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right) \right) \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]+(-3+2 m) \\
 & \left(-\frac{1}{\frac{3}{2}-m}\left(\frac{1}{2}-m\right) m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2 m, 1, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right. \\
 & \quad \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]-\frac{1}{2\left(\frac{3}{2}-m\right)}\left(\frac{1}{2}-m\right) \operatorname{AppellF1}\left[\frac{3}{2}-m, -2 m, 2, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right)
 \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \Bigg) + \\
 & 2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \left( -\frac{1}{\frac{5}{2}-m} \left(\frac{3}{2}-m\right) m \operatorname{AppellF1}\left[\frac{5}{2}-m, 1-2m, \right. \right. \\
 & \quad \left. \left. 2, \frac{7}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right] \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \frac{1}{\frac{5}{2}-m} \right. \\
 & \quad \left. \left(\frac{3}{2}-m\right) \operatorname{AppellF1}\left[\frac{5}{2}-m, -2m, 3, \frac{7}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right] \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) + \\
 & \quad 2m \left( -\frac{1}{2\left(\frac{5}{2}-m\right)} \left(\frac{3}{2}-m\right) \operatorname{AppellF1}\left[\frac{5}{2}-m, 1-2m, 2, \frac{7}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}- \right. \right. \right. \right. \\
 & \quad \left. \left. \left. fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right] \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[ \right. \right. \\
 & \quad \left. \left. \frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + \frac{1}{2\left(\frac{5}{2}-m\right)} (1-2m) \left(\frac{3}{2}-m\right) \operatorname{AppellF1}\left[\frac{5}{2}-m, \right. \right. \\
 & \quad \left. \left. 2-2m, 1, \frac{7}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right] \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \right) \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \left( (-3+2m) \operatorname{AppellF1}\left[\frac{1}{2}-m, -2m, 1, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right] + 2 \left( 2m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2m, 1, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right] \right) + \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{3}{2}-m, -2m, 2, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right] \right) \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right)^2 - \\
 & \left( 8B \operatorname{AppellF1}\left[\frac{1}{2}-m, -2m, 2, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right] \left( 1 + \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \right) \\
 & \left( 2 \left( m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2m, 2, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \operatorname{AppellF1}\left[\frac{3}{2}-m,-2 m, 3,\right. \\
 & \left.\frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]+(-3+2 m) \\
 & \left(-\frac{1}{\frac{3}{2}-m}\left(\frac{1}{2}-m\right) m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2 m, 2, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]-\right. \\
 & \left.\frac{1}{\frac{3}{2}-m}\left(\frac{1}{2}-m\right) \operatorname{AppellF1}\left[\frac{3}{2}-m,-2 m, 3, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)+ \\
 & 4 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\left(-\frac{1}{\frac{5}{2}-m}\left(\frac{3}{2}-m\right) m \operatorname{AppellF1}\left[\frac{5}{2}-m, 1-2 m,\right.\right. \\
 & \left.\left.3, \frac{7}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \right. \\
 & \left.\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]-\frac{1}{2\left(\frac{5}{2}-m\right)}\right. \\
 & \left.3\left(\frac{3}{2}-m\right) \operatorname{AppellF1}\left[\frac{5}{2}-m,-2 m, 4, \frac{7}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]+ \right. \\
 & \left. m\left(-\frac{1}{\frac{5}{2}-m}\left(\frac{3}{2}-m\right) \operatorname{AppellF1}\left[\frac{5}{2}-m, 1-2 m, 3, \frac{7}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \right. \\
 & \left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]+\frac{1}{2\left(\frac{5}{2}-m\right)}(1-2 m)\left(\frac{3}{2}-m\right) \operatorname{AppellF1}\left[\frac{5}{2}-m,\right.\right. \\
 & \left.\left.2-2 m, 2, \frac{7}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \right. \\
 & \left.\left.\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)\right)\right) / \\
 & \left((-3+2 m) \operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m, 2, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+4\left(m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2 m, 2,\right.\right. \right. \\
 & \left.\left.\frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \right.
 \end{aligned}$$



$$\begin{aligned}
 & \text{AppellF1}\left[\frac{3}{2}-m, -2m, 3, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 + \\
 & \left(8B \text{AppellF1}\left[\frac{1}{2}-m, -2m, 3, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \left(2m \text{AppellF1}\left[\frac{3}{2}-m, 1-2m, 3, \frac{5}{2}-m, \right. \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 3 \text{AppellF1}\left[\frac{3}{2}-m, \right. \right. \\
 & \quad \quad \left. \left. -2m, 4, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + (-3+2m) \right. \\
 & \quad \left. \left(-\frac{1}{\frac{3}{2}-m}\left(\frac{1}{2}-m\right) m \text{AppellF1}\left[\frac{3}{2}-m, 1-2m, 3, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \right. \right. \\
 & \quad \quad \left. \frac{1}{2\left(\frac{3}{2}-m\right)} 3\left(\frac{1}{2}-m\right) \text{AppellF1}\left[\frac{3}{2}-m, -2m, 4, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right) \right) + \\
 & 2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \left(2m \left(-\frac{1}{2\left(\frac{5}{2}-m\right)} 3\left(\frac{3}{2}-m\right) \text{AppellF1}\left[\frac{5}{2}-m, \right. \right. \right. \\
 & \quad \left. \left. 1-2m, 4, \frac{7}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + \right. \\
 & \quad \left. \frac{1}{2\left(\frac{5}{2}-m\right)} (1-2m) \left(\frac{3}{2}-m\right) \text{AppellF1}\left[\frac{5}{2}-m, 2-2m, 3, \frac{7}{2}-m, \right. \right. \\
 & \quad \quad \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right) + 3 \\
 & \left(-\frac{1}{\frac{5}{2}-m}\left(\frac{3}{2}-m\right) m \text{AppellF1}\left[\frac{5}{2}-m, 1-2m, 4, \frac{7}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right)
 \end{aligned}$$



$$\frac{1}{3 f (1+2 m)} 2^{\frac{5}{2}-m} c^3 (3 A-2 B (1-m)) \operatorname{Cos}[e+f x]$$

$$\operatorname{Hypergeometric2F1}\left[\frac{1}{2}(-3+2 m), \frac{1}{2}(1+2 m), \frac{1}{2}(3+2 m), \frac{1}{2}(1+\operatorname{Sin}[e+f x])\right]$$

$$(1-\operatorname{Sin}[e+f x])^{\frac{1}{2}+m} (a+a \operatorname{Sin}[e+f x])^m (c-c \operatorname{Sin}[e+f x])^{-1-m} -$$

$$\frac{B \operatorname{Cos}[e+f x] (a+a \operatorname{Sin}[e+f x])^m (c-c \operatorname{Sin}[e+f x])^{2-m}}{3 f}$$

Result (type 6, 37 061 leaves): Display of huge result suppressed!

### Problem 232: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c+d x]^5 (a+a \operatorname{Sin}[c+d x])^3 (A-A \operatorname{Sin}[c+d x]) dx$$

Optimal (type 3, 86 leaves, 10 steps):

$$\frac{5 a^3 A \operatorname{ArcTanh}[\operatorname{Cos}[c+d x]]}{8 d} - \frac{2 a^3 A \operatorname{Cot}[c+d x]^3}{3 d} -$$

$$\frac{3 a^3 A \operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]}{8 d} - \frac{a^3 A \operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]^3}{4 d}$$

Result (type 3, 210 leaves):

$$a^3 A \left( \frac{\operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{3 d} - \frac{3 \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{32 d} - \frac{\operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{12 d} - \right.$$

$$\frac{\operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^4}{64 d} + \frac{5 \operatorname{Log}[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]]}{8 d} - \frac{5 \operatorname{Log}[\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]]}{8 d} + \frac{3 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2}{32 d} +$$

$$\left. \frac{\operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^4}{64 d} - \frac{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{3 d} + \frac{\operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{12 d} \right)$$

### Problem 233: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c+d x]^6 (a+a \operatorname{Sin}[c+d x])^3 (A-A \operatorname{Sin}[c+d x]) dx$$

Optimal (type 3, 105 leaves, 12 steps):

$$\frac{a^3 A \operatorname{ArcTanh}[\operatorname{Cos}[c+d x]]}{4 d} - \frac{2 a^3 A \operatorname{Cot}[c+d x]^3}{3 d} - \frac{a^3 A \operatorname{Cot}[c+d x]^5}{5 d} +$$

$$\frac{a^3 A \operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]}{4 d} - \frac{a^3 A \operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]^3}{2 d}$$

Result (type 3, 268 leaves):

$$a^3 A \left( \frac{7 \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{30d} + \frac{\operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{16d} - \frac{19 \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{480d} - \frac{\operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{32d} - \frac{\operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{160d} + \frac{\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right]}{4d} - \frac{\operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{4d} - \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{16d} + \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4}{32d} - \frac{7 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{30d} + \frac{19 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{480d} + \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{160d} \right)$$

**Problem 234: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Csc}[c+dx]^7 (a+a \operatorname{Sin}[c+dx])^3 (A-A \operatorname{Sin}[c+dx]) dx$$

Optimal (type 3, 130 leaves, 12 steps):

$$\frac{3 a^3 A \operatorname{ArcTanh}\left[\operatorname{Cos}[c+dx]\right]}{16 d} - \frac{2 a^3 A \operatorname{Cot}[c+dx]^3}{3 d} - \frac{2 a^3 A \operatorname{Cot}[c+dx]^5}{5 d} + \frac{3 a^3 A \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]}{16 d} - \frac{5 a^3 A \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^3}{24 d} - \frac{a^3 A \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^5}{6 d}$$

Result (type 3, 306 leaves):

$$a^3 A \left( \frac{2 \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{15d} + \frac{3 \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{64d} + \frac{\operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{240d} - \frac{\operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{64d} - \frac{\operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{80d} - \frac{\operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^6}{384d} + \frac{3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right]}{16d} - \frac{3 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{16d} - \frac{3 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{64d} + \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4}{64d} + \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^6}{384d} - \frac{2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{15d} - \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{240d} + \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{80d} \right)$$

**Problem 236: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sin}[c+dx]^3 (A-A \operatorname{Sin}[c+dx])}{(a+a \operatorname{Sin}[c+dx])^3} dx$$

Optimal (type 3, 103 leaves, 9 steps):

$$\frac{4 A x}{a^3} + \frac{A \cos [c+d x]}{a^3 d} + \frac{2 A \cos [c+d x]}{5 a^3 d (1+\sin [c+d x])^3} -$$

$$\frac{31 A \cos [c+d x]}{15 a^3 d (1+\sin [c+d x])^2} + \frac{104 A \cos [c+d x]}{15 a^3 d (1+\sin [c+d x])}$$

Result (type 3, 228 leaves):

$$\frac{1}{20 a^3 d \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{1}{2} (c+d x) \right] + \sin \left[ \frac{1}{2} (c+d x) \right] \right)^5}$$

$$A \left( -1200 d x \cos \left[ \frac{d x}{2} \right] + 1665 \cos \left[ c + \frac{d x}{2} \right] - 1675 \cos \left[ c + \frac{3 d x}{2} \right] + 600 d x \cos \left[ 2 c + \frac{3 d x}{2} \right] + \right.$$

$$120 d x \cos \left[ 2 c + \frac{5 d x}{2} \right] + 75 \cos \left[ 3 c + \frac{5 d x}{2} \right] + 15 \cos \left[ 3 c + \frac{7 d x}{2} \right] + 2495 \sin \left[ \frac{d x}{2} \right] -$$

$$1200 d x \sin \left[ c + \frac{d x}{2} \right] - 600 d x \sin \left[ c + \frac{3 d x}{2} \right] + 405 \sin \left[ 2 c + \frac{3 d x}{2} \right] -$$

$$\left. 491 \sin \left[ 2 c + \frac{5 d x}{2} \right] + 120 d x \sin \left[ 3 c + \frac{5 d x}{2} \right] + 15 \sin \left[ 4 c + \frac{7 d x}{2} \right] \right)$$

**Problem 237: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sin [c+d x]^2 (A-A \sin [c+d x])}{(a+a \sin [c+d x])^3} dx$$

Optimal (type 3, 89 leaves, 8 steps):

$$-\frac{A x}{a^3} - \frac{2 A \cos [c+d x]}{5 a^3 d (1+\sin [c+d x])^3} + \frac{7 A \cos [c+d x]}{5 a^3 d (1+\sin [c+d x])^2} - \frac{13 A \cos [c+d x]}{5 a^3 d (1+\sin [c+d x])}$$

Result (type 3, 189 leaves):

$$\left( A \left( -50 d x \cos \left[ \frac{d x}{2} \right] + 110 \cos \left[ c + \frac{d x}{2} \right] - 90 \cos \left[ c + \frac{3 d x}{2} \right] + 25 d x \cos \left[ 2 c + \frac{3 d x}{2} \right] + \right.$$

$$5 d x \cos \left[ 2 c + \frac{5 d x}{2} \right] + 150 \sin \left[ \frac{d x}{2} \right] - 50 d x \sin \left[ c + \frac{d x}{2} \right] - 25 d x \sin \left[ c + \frac{3 d x}{2} \right] +$$

$$\left. 40 \sin \left[ 2 c + \frac{3 d x}{2} \right] - 26 \sin \left[ 2 c + \frac{5 d x}{2} \right] + 5 d x \sin \left[ 3 c + \frac{5 d x}{2} \right] \right) /$$

$$\left( 20 a^3 d \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{1}{2} (c+d x) \right] + \sin \left[ \frac{1}{2} (c+d x) \right] \right)^5 \right)$$

**Problem 240: Result more than twice size of optimal antiderivative.**

$$\int \frac{\csc [c+d x] (A-A \sin [c+d x])}{(a+a \sin [c+d x])^3} dx$$

Optimal (type 3, 98 leaves, 9 steps):

$$-\frac{A \operatorname{ArcTanh}[\operatorname{Cos}[c+d x]]}{a^3 d} + \frac{2 A \operatorname{Cos}[c+d x]}{5 a^3 d (1+\operatorname{Sin}[c+d x])^3} + \frac{3 A \operatorname{Cos}[c+d x]}{5 a^3 d (1+\operatorname{Sin}[c+d x])^2} + \frac{8 A \operatorname{Cos}[c+d x]}{5 a^3 d (1+\operatorname{Sin}[c+d x])}$$

Result (type 3, 313 leaves):

$$\left( \left( \left( \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right) \left( 2 \operatorname{Cos}\left[\frac{c}{2}\right] - 2 \operatorname{Sin}\left[\frac{c}{2}\right] + 3 \operatorname{Cos}\left[\frac{c}{2}\right] \left( \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right)^2 - 3 \operatorname{Sin}\left[\frac{c}{2}\right] \left( \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right)^2 - 5 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]\right] \left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right)^4 + 5 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] \left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right)^4 \right) + 2 \operatorname{Sin}\left[\frac{d x}{2}\right] (-17 + 4 \operatorname{Cos}[2(c+d x)] - 19 \operatorname{Sin}[c+d x]) \right) (A - A \operatorname{Sin}[c+d x]) \Big/ \left( 5 a^3 d \left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right)^2 \left( \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right)^5 \right)$$

**Problem 241: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Csc}[c+d x]^2 (A - A \operatorname{Sin}[c+d x])}{(a + a \operatorname{Sin}[c+d x])^3} dx$$

Optimal (type 3, 113 leaves, 15 steps):

$$\frac{4 A \operatorname{ArcTanh}[\operatorname{Cos}[c+d x]]}{a^3 d} - \frac{A \operatorname{Cot}[c+d x]}{a^3 d} - \frac{2 A \operatorname{Cot}[c+d x]}{5 a^3 d (1+\operatorname{Csc}[c+d x])^3} + \frac{31 A \operatorname{Cot}[c+d x]}{15 a^3 d (1+\operatorname{Csc}[c+d x])^2} - \frac{104 A \operatorname{Cot}[c+d x]}{15 a^3 d (1+\operatorname{Csc}[c+d x])}$$

Result (type 3, 252 leaves):

$$\frac{1}{a^3} A \left( -\frac{\text{Cot}\left[\frac{1}{2}(c+dx)\right]}{2d} + \frac{4 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c+dx)\right]\right]}{d} - \frac{4 \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{d} + \frac{4 \text{Sin}\left[\frac{1}{2}(c+dx)\right]}{5d \left(\text{Cos}\left[\frac{1}{2}(c+dx)\right] + \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} - \frac{2}{5d \left(\text{Cos}\left[\frac{1}{2}(c+dx)\right] + \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4} + \frac{38 \text{Sin}\left[\frac{1}{2}(c+dx)\right]}{15d \left(\text{Cos}\left[\frac{1}{2}(c+dx)\right] + \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^3} - \frac{19}{15d \left(\text{Cos}\left[\frac{1}{2}(c+dx)\right] + \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2} + \frac{158 \text{Sin}\left[\frac{1}{2}(c+dx)\right]}{15d \left(\text{Cos}\left[\frac{1}{2}(c+dx)\right] + \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)} + \frac{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}{2d} \right)$$

**Problem 242: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Csc}[c+dx]^3 (A - A \text{Sin}[c+dx])}{(a + a \text{Sin}[c+dx])^3} dx$$

Optimal (type 3, 138 leaves, 13 steps):

$$-\frac{19 A \text{ArcTanh}\left[\text{Cos}[c+dx]\right]}{2 a^3 d} + \frac{4 A \text{Cot}[c+dx]}{a^3 d} - \frac{A \text{Cot}[c+dx] \text{Csc}[c+dx]}{2 a^3 d} + \frac{2 A \text{Cos}[c+dx]}{5 a^3 d (1 + \text{Sin}[c+dx])^3} + \frac{29 A \text{Cos}[c+dx]}{15 a^3 d (1 + \text{Sin}[c+dx])^2} + \frac{164 A \text{Cos}[c+dx]}{15 a^3 d (1 + \text{Sin}[c+dx])}$$

Result (type 3, 290 leaves):

$$\frac{1}{a^3} A \left( \frac{2 \text{Cot}\left[\frac{1}{2}(c+dx)\right]}{d} - \frac{\text{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{8d} - \frac{19 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c+dx)\right]\right]}{2d} + \frac{19 \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{2d} + \frac{\text{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{8d} - \frac{4 \text{Sin}\left[\frac{1}{2}(c+dx)\right]}{5d \left(\text{Cos}\left[\frac{1}{2}(c+dx)\right] + \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} + \frac{2}{5d \left(\text{Cos}\left[\frac{1}{2}(c+dx)\right] + \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4} - \frac{58 \text{Sin}\left[\frac{1}{2}(c+dx)\right]}{15d \left(\text{Cos}\left[\frac{1}{2}(c+dx)\right] + \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^3} + \frac{29}{15d \left(\text{Cos}\left[\frac{1}{2}(c+dx)\right] + \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2} - \frac{328 \text{Sin}\left[\frac{1}{2}(c+dx)\right]}{15d \left(\text{Cos}\left[\frac{1}{2}(c+dx)\right] + \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)} - \frac{2 \text{Tan}\left[\frac{1}{2}(c+dx)\right]}{d} \right)$$

**Problem 243: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Csc}[c + d x]^4 (A - A \text{Sin}[c + d x])}{(a + a \text{Sin}[c + d x])^3} dx$$

Optimal (type 3, 153 leaves, 15 steps):

$$\frac{18 A \text{ArcTanh}[\text{Cos}[c + d x]]}{a^3 d} - \frac{10 A \text{Cot}[c + d x]}{a^3 d} - \frac{A \text{Cot}[c + d x]^3}{3 a^3 d} + \frac{2 A \text{Cot}[c + d x] \text{Csc}[c + d x]}{a^3 d} - \frac{2 A \text{Cos}[c + d x]}{5 a^3 d (1 + \text{Sin}[c + d x])^3} - \frac{13 A \text{Cos}[c + d x]}{5 a^3 d (1 + \text{Sin}[c + d x])^2} - \frac{93 A \text{Cos}[c + d x]}{5 a^3 d (1 + \text{Sin}[c + d x])}$$

Result (type 3, 348 leaves):

$$\frac{1}{a^3} A \left( -\frac{29 \text{Cot}\left[\frac{1}{2}(c + d x)\right]}{6 d} + \frac{\text{Csc}\left[\frac{1}{2}(c + d x)\right]^2}{2 d} - \frac{\text{Cot}\left[\frac{1}{2}(c + d x)\right] \text{Csc}\left[\frac{1}{2}(c + d x)\right]^2}{24 d} + \frac{18 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right]\right]}{d} - \frac{18 \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c + d x)\right]\right]}{d} - \frac{\text{Sec}\left[\frac{1}{2}(c + d x)\right]^2}{2 d} + \frac{4 \text{Sin}\left[\frac{1}{2}(c + d x)\right]}{5 d \left(\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^5} - \frac{2}{5 d \left(\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4} + \frac{26 \text{Sin}\left[\frac{1}{2}(c + d x)\right]}{5 d \left(\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^3} - \frac{13}{5 d \left(\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} + \frac{186 \text{Sin}\left[\frac{1}{2}(c + d x)\right]}{5 d \left(\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right)} + \left. \frac{29 \text{Tan}\left[\frac{1}{2}(c + d x)\right]}{6 d} + \frac{\text{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \text{Tan}\left[\frac{1}{2}(c + d x)\right]}{24 d} \right)$$

**Problem 248: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(a + a \text{Sin}[e + f x]) (A + B \text{Sin}[e + f x])}{c + d \text{Sin}[e + f x]} dx$$

Optimal (type 3, 98 leaves, 6 steps):

$$-\frac{a (B c - (A + B) d) x}{d^2} + \frac{2 a (c - d) (B c - A d) \text{ArcTan}\left[\frac{d + c \text{Tan}\left[\frac{1}{2}(e + f x)\right]}{\sqrt{c^2 - d^2}}\right]}{d^2 \sqrt{c^2 - d^2} f} - \frac{a B \text{Cos}[e + f x]}{d f}$$

Result (type 3, 196 leaves):



$$\left( a \left( A d x + B (-c + d) x - \frac{B d \cos[e] \cos[fx]}{f} + \right. \right. \\ \left. \left. \left( 2 (c - d) (B c - A d) \operatorname{ArcTan} \left[ \frac{\sec\left[\frac{fx}{2}\right] (\cos[e] - i \sin[e]) (d \cos\left[e + \frac{fx}{2}\right] + c \sin\left[\frac{fx}{2}\right])}{\sqrt{c^2 - d^2} \sqrt{(\cos[e] - i \sin[e])^2}} \right] \right. \right. \right. \\ \left. \left. \left. (\cos[e] - i \sin[e]) \right) \right) / \left( \sqrt{c^2 - d^2} f \sqrt{(\cos[e] - i \sin[e])^2} + \frac{B d \sin[e] \sin[fx]}{f} \right) \right) \\ \left. \left. (1 + \sin[e + fx]) \right) \right) / \left( d^2 \left( \cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right] \right)^2 \right)$$

**Problem 249: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(a + a \sin[e + fx]) (A + B \sin[e + fx])}{(c + d \sin[e + fx])^2} dx$$

Optimal (type 3, 124 leaves, 6 steps):

$$\frac{a B x}{d^2} + \frac{2 a ((A + B) (c - d) d^2 - B c (c^2 - d^2)) \operatorname{ArcTan} \left[ \frac{d + c \tan\left[\frac{1}{2}(e + fx)\right]}{\sqrt{c^2 - d^2}} \right]}{d^2 (c^2 - d^2)^{3/2} f} + \frac{a (B c - A d) \cos[e + fx]}{d (c + d) f (c + d \sin[e + fx])}$$

Result (type 3, 217 leaves):

$$\left( a (1 + \sin[e + fx]) \left( B x + \right. \right. \\ \left. \left. \left( 2 (A d^2 - B (c^2 + c d - d^2)) \operatorname{ArcTan} \left[ \frac{\sec\left[\frac{fx}{2}\right] (\cos[e] - i \sin[e]) (d \cos\left[e + \frac{fx}{2}\right] + c \sin\left[\frac{fx}{2}\right])}{\sqrt{c^2 - d^2} \sqrt{(\cos[e] - i \sin[e])^2}} \right] \right. \right. \right. \\ \left. \left. \left. (\cos[e] - i \sin[e]) \right) \right) / \left( (c + d) \sqrt{c^2 - d^2} f \sqrt{(\cos[e] - i \sin[e])^2} + \right. \right. \\ \left. \left. \frac{(-B c + A d) \csc[e] (c \cos[e] + d \sin[fx])}{(c + d) f (c + d \sin[e + fx])} \right) \right) \right) / \left( d^2 \left( \cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right] \right)^2 \right)$$

**Problem 250: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(a + a \sin[e + fx]) (A + B \sin[e + fx])}{(c + d \sin[e + fx])^3} dx$$

Optimal (type 3, 176 leaves, 7 steps):

$$\frac{a (2 A c + B c - A d - 2 B d) \operatorname{ArcTan}\left[\frac{d+c \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]}{\sqrt{c^2-d^2}}\right]}{(c+d)\left(c^2-d^2\right)^{3 / 2} f} +$$

$$\frac{a(B c-A d) \operatorname{Cos}[e+f x]}{2 d(c+d) f(c+d \operatorname{Sin}[e+f x])^2} - \frac{a(A(c-2 d) d+B\left(c^2+2 c d-2 d^2\right)) \operatorname{Cos}[e+f x]}{2(c-d) d(c+d)^2 f(c+d \operatorname{Sin}[e+f x])}$$

Result (type 3, 345 leaves):

$$\left( a(1 + \operatorname{Sin}[e + f x]) \right.$$

$$\left. \left( \left( 4(2 A c + B c - A d - 2 B d) \operatorname{ArcTan}\left[\frac{\operatorname{Sec}\left[\frac{f x}{2}\right](\operatorname{Cos}[e] - i \operatorname{Sin}[e])\left(d \operatorname{Cos}\left[e + \frac{f x}{2}\right] + c \operatorname{Sin}\left[\frac{f x}{2}\right]\right)}{\sqrt{c^2 - d^2} \sqrt{(\operatorname{Cos}[e] - i \operatorname{Sin}[e])^2}}\right]} \right. \right.$$

$$\left. \left. (\operatorname{Cos}[e] - i \operatorname{Sin}[e]) \right) / \left( \sqrt{c^2 - d^2} \sqrt{(\operatorname{Cos}[e] - i \operatorname{Sin}[e])^2} \right) + \right.$$

$$\left. \left( (2 c^2 + d^2)(A(c - 2 d) d + B(c^2 + 2 c d - 2 d^2)) \operatorname{Cot}[e] + \right. \right.$$

$$\left. \left. d \operatorname{Csc}[e](-d(A(c - 2 d) d + B(c^2 + 2 c d - 2 d^2)) \operatorname{Cos}[e + 2 f x] + \right. \right.$$

$$\left. \left. (B c(2 c^2 + 6 c d - 5 d^2) - A d(-4 c^2 + 6 c d + d^2)) \operatorname{Sin}[f x] + (A d^2(-2 c + d) + \right. \right.$$

$$\left. \left. B c(2 c^2 + 2 c d - 3 d^2)) \operatorname{Sin}[2 e + f x] \right) / \left( d^2(c + d \operatorname{Sin}[e + f x])^2 \right) \right) /$$

$$\left( 4(c - d)(c + d)^2 f \left( \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] + \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] \right)^2 \right)$$

**Problem 264: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \operatorname{Sin}[e + f x])^3 (A + B \operatorname{Sin}[e + f x])}{(c + d \operatorname{Sin}[e + f x])^3} dx$$

Optimal (type 3, 305 leaves, 8 steps):

$$-\frac{a^3(3 B c - A d - 3 B d) x}{d^4} - \left( a^3(c - d)(A d(2 c^2 + 6 c d + 7 d^2) - 3 B(2 c^3 + 4 c^2 d + c d^2 - 2 d^3)) \right.$$

$$\left. \operatorname{ArcTan}\left[\frac{d + c \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}{\sqrt{c^2 - d^2}}\right] \right) / \left( d^4(c + d)^2 \sqrt{c^2 - d^2} f \right) -$$

$$\frac{a^3(3 B c(2 c + 3 d) - A d(2 c + 5 d)) \operatorname{Cos}[e + f x]}{2 d^3(c + d)^2 f} + \frac{a(B c - A d) \operatorname{Cos}[e + f x](a + a \operatorname{Sin}[e + f x])^2}{2 d(c + d) f(c + d \operatorname{Sin}[e + f x])^2} -$$

$$\left( (A d(c + 4 d) - B(3 c^2 + 4 c d - 2 d^2)) \operatorname{Cos}[e + f x](a^3 + a^3 \operatorname{Sin}[e + f x]) \right) /$$

$$\left( 2 d^2(c + d)^2 f(c + d \operatorname{Sin}[e + f x]) \right)$$

Result (type 3, 830 leaves):

$$\frac{1}{4 d^4 (c+d)^2 f \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right)^6}$$

$$a^3 (1 + \sin[e+f x])^3 \left( \frac{1}{\sqrt{c^2-d^2}} 4(c-d) (-A d (2 c^2+6 c d+7 d^2) + 3 B (2 c^3+4 c^2 d+c d^2-2 d^3)) \right.$$

$$\left. \text{ArcTan} \left[ \frac{d+c \tan \left[ \frac{1}{2} (e+f x) \right]}{\sqrt{c^2-d^2}} \right] + \frac{1}{(c+d \sin[e+f x])^2} \right.$$

$$\left. \left( -12 B c^5 e+4 A c^4 d e-12 B c^4 d e+8 A c^3 d^2 e+6 B c^3 d^2 e+6 A c^2 d^3 e+6 B c^2 d^3 e+4 A c d^4 e+ \right. \right.$$

$$6 B c d^4 e+2 A d^5 e+6 B d^5 e-12 B c^5 f x+4 A c^4 d f x-12 B c^4 d f x+8 A c^3 d^2 f x+$$

$$6 B c^3 d^2 f x+6 A c^2 d^3 f x+6 B c^2 d^3 f x+4 A c d^4 f x+6 B c d^4 f x+2 A d^5 f x+6 B d^5 f x-$$

$$d(2 A d(-2 c^3-4 c^2 d+5 c d^2+d^3)+B(12 c^4+12 c^3 d-9 c^2 d^2+4 c d^3+d^4)) \cos[e+f x]-$$

$$2 d^2(c+d)^2(-3 B c+A d+3 B d)(e+f x) \cos[2(e+f x)]+$$

$$B c^2 d^3 \cos[3(e+f x)]+2 B c d^4 \cos[3(e+f x)]+B d^5 \cos[3(e+f x)]-$$

$$24 B c^4 d e \sin[e+f x]+8 A c^3 d^2 e \sin[e+f x]-24 B c^3 d^2 e \sin[e+f x]+$$

$$16 A c^2 d^3 e \sin[e+f x]+24 B c^2 d^3 e \sin[e+f x]+8 A c d^4 e \sin[e+f x]+$$

$$24 B c d^4 e \sin[e+f x]-24 B c^4 d f x \sin[e+f x]+8 A c^3 d^2 f x \sin[e+f x]-$$

$$24 B c^3 d^2 f x \sin[e+f x]+16 A c^2 d^3 f x \sin[e+f x]+24 B c^2 d^3 f x \sin[e+f x]+$$

$$8 A c d^4 f x \sin[e+f x]+24 B c d^4 f x \sin[e+f x]-9 B c^3 d^2 \sin[2(e+f x)]+$$

$$3 A c^2 d^3 \sin[2(e+f x)]-9 B c^2 d^3 \sin[2(e+f x)]+3 A c d^4 \sin[2(e+f x)]+$$

$$\left. \left. 4 B c d^4 \sin[2(e+f x)]-6 A d^5 \sin[2(e+f x)]-2 B d^5 \sin[2(e+f x)] \right) \right)$$

**Problem 265: Result more than twice size of optimal antiderivative.**

$$\int \frac{(A+B \sin[e+f x])(c+d \sin[e+f x])^3}{a+a \sin[e+f x]} dx$$

Optimal (type 3, 220 leaves, 3 steps):

$$\frac{(3 A d(2 c^2-2 c d+d^2)+B(2 c^3-6 c^2 d+9 c d^2-3 d^3)) x}{2 a} +$$

$$\frac{2 d(3 A(c^2-3 c d+d^2)-B(7 c^2-9 c d+4 d^2)) \cos[e+f x]}{3 a f} +$$

$$\frac{d^2(6 A c-11 B c-9 A d+9 B d) \cos[e+f x] \sin[e+f x]}{6 a f} +$$

$$\frac{(3 A-4 B) d \cos[e+f x](c+d \sin[e+f x])^2}{3 a f} - \frac{(A-B) \cos[e+f x](c+d \sin[e+f x])^3}{f(a+a \sin[e+f x])}$$

Result (type 3, 788 leaves):

$$\frac{1}{24 a f (1 + \sin[e + f x])} \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right) \left( 3 (4 A d (6 c^2 (e + f x) - 3 c d (1 + 2 e + 2 f x) + d^2 (1 + 3 e + 3 f x)) + B (8 c^3 (e + f x) - 12 c^2 d (1 + 2 e + 2 f x) + 12 c d^2 (1 + 3 e + 3 f x) - d^3 (7 + 12 e + 12 f x))) \cos\left[\frac{1}{2}(e + f x)\right] + 9 d (A d (-4 c + d) + B (-4 c^2 + 3 c d - 2 d^2)) \cos\left[\frac{3}{2}(e + f x)\right] + 9 B c d^2 \cos\left[\frac{5}{2}(e + f x)\right] + 3 A d^3 \cos\left[\frac{5}{2}(e + f x)\right] - 2 B d^3 \cos\left[\frac{5}{2}(e + f x)\right] + B d^3 \cos\left[\frac{7}{2}(e + f x)\right] + 48 A c^3 \sin\left[\frac{1}{2}(e + f x)\right] - 48 B c^3 \sin\left[\frac{1}{2}(e + f x)\right] - 144 A c^2 d \sin\left[\frac{1}{2}(e + f x)\right] + 180 B c^2 d \sin\left[\frac{1}{2}(e + f x)\right] + 180 A c d^2 \sin\left[\frac{1}{2}(e + f x)\right] - 180 B c d^2 \sin\left[\frac{1}{2}(e + f x)\right] - 60 A d^3 \sin\left[\frac{1}{2}(e + f x)\right] + 69 B d^3 \sin\left[\frac{1}{2}(e + f x)\right] + 24 B c^3 e \sin\left[\frac{1}{2}(e + f x)\right] + 72 A c^2 d e \sin\left[\frac{1}{2}(e + f x)\right] - 72 B c^2 d e \sin\left[\frac{1}{2}(e + f x)\right] - 72 A c d^2 e \sin\left[\frac{1}{2}(e + f x)\right] + 108 B c d^2 e \sin\left[\frac{1}{2}(e + f x)\right] + 36 A d^3 e \sin\left[\frac{1}{2}(e + f x)\right] - 36 B d^3 e \sin\left[\frac{1}{2}(e + f x)\right] + 24 B c^3 f x \sin\left[\frac{1}{2}(e + f x)\right] + 72 A c^2 d f x \sin\left[\frac{1}{2}(e + f x)\right] - 72 B c^2 d f x \sin\left[\frac{1}{2}(e + f x)\right] - 72 A c d^2 f x \sin\left[\frac{1}{2}(e + f x)\right] + 108 B c d^2 f x \sin\left[\frac{1}{2}(e + f x)\right] + 36 A d^3 f x \sin\left[\frac{1}{2}(e + f x)\right] - 36 B d^3 f x \sin\left[\frac{1}{2}(e + f x)\right] - 36 B c^2 d \sin\left[\frac{3}{2}(e + f x)\right] - 36 A c d^2 \sin\left[\frac{3}{2}(e + f x)\right] + 27 B c d^2 \sin\left[\frac{3}{2}(e + f x)\right] + 9 A d^3 \sin\left[\frac{3}{2}(e + f x)\right] - 18 B d^3 \sin\left[\frac{3}{2}(e + f x)\right] - 9 B c d^2 \sin\left[\frac{5}{2}(e + f x)\right] - 3 A d^3 \sin\left[\frac{5}{2}(e + f x)\right] + 2 B d^3 \sin\left[\frac{5}{2}(e + f x)\right] + B d^3 \sin\left[\frac{7}{2}(e + f x)\right] \right)$$

**Problem 268: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sin[e + f x]}{a + a \sin[e + f x]} dx$$

Optimal (type 3, 35 leaves, 2 steps):

$$\frac{B x - (A - B) \cos[e + f x]}{a f (a + a \sin[e + f x])}$$

Result (type 3, 79 leaves):

$$\left( \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right) \left( B (e + f x) \cos\left[\frac{1}{2}(e + f x)\right] + (2 A + B (-2 + e + f x)) \sin\left[\frac{1}{2}(e + f x)\right] \right) \right) / (a f (1 + \sin[e + f x]))$$

### Problem 272: Result more than twice size of optimal antiderivative.

$$\int \frac{(A + B \sin[e + f x]) (c + d \sin[e + f x])^3}{(a + a \sin[e + f x])^2} dx$$

Optimal (type 3, 228 leaves, 3 steps):

$$\begin{aligned} & \frac{d (2 A (3 c - 2 d) d + B (6 c^2 - 12 c d + 7 d^2)) x}{2 a^2} + \\ & \frac{2 d (A (c^2 + 6 c d - 5 d^2) + B (2 c^2 - 15 c d + 8 d^2)) \cos[e + f x]}{3 a^2 f} + \\ & \frac{d^2 (B (4 c - 21 d) + 2 A (c + 6 d)) \cos[e + f x] \sin[e + f x]}{6 a^2 f} - \\ & \frac{(2 B (c - 4 d) + A (c + 5 d)) \cos[e + f x] (c + d \sin[e + f x])^2}{3 a^2 f (1 + \sin[e + f x])} - \\ & \frac{(A - B) \cos[e + f x] (c + d \sin[e + f x])^3}{3 f (a + a \sin[e + f x])^2} \end{aligned}$$

Result (type 3, 1032 leaves):

$$\begin{aligned}
& \frac{1}{48 f (a + a \sin [e + f x])^2} \\
& \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) \left( 48 B c^3 \cos \left[ \frac{1}{2} (e + f x) \right] + 144 A c^2 d \cos \left[ \frac{1}{2} (e + f x) \right] - \right. \\
& \quad 288 B c^2 d \cos \left[ \frac{1}{2} (e + f x) \right] - 288 A c d^2 \cos \left[ \frac{1}{2} (e + f x) \right] + 360 B c d^2 \cos \left[ \frac{1}{2} (e + f x) \right] + \\
& \quad 120 A d^3 \cos \left[ \frac{1}{2} (e + f x) \right] - 147 B d^3 \cos \left[ \frac{1}{2} (e + f x) \right] + 216 B c^2 d (e + f x) \cos \left[ \frac{1}{2} (e + f x) \right] + \\
& \quad 216 A c d^2 (e + f x) \cos \left[ \frac{1}{2} (e + f x) \right] - 432 B c d^2 (e + f x) \cos \left[ \frac{1}{2} (e + f x) \right] - \\
& \quad 144 A d^3 (e + f x) \cos \left[ \frac{1}{2} (e + f x) \right] + 252 B d^3 (e + f x) \cos \left[ \frac{1}{2} (e + f x) \right] - \\
& \quad 16 A c^3 \cos \left[ \frac{3}{2} (e + f x) \right] - 32 B c^3 \cos \left[ \frac{3}{2} (e + f x) \right] - 96 A c^2 d \cos \left[ \frac{3}{2} (e + f x) \right] + \\
& \quad 240 B c^2 d \cos \left[ \frac{3}{2} (e + f x) \right] + 240 A c d^2 \cos \left[ \frac{3}{2} (e + f x) \right] - 492 B c d^2 \cos \left[ \frac{3}{2} (e + f x) \right] - \\
& \quad 164 A d^3 \cos \left[ \frac{3}{2} (e + f x) \right] + 239 B d^3 \cos \left[ \frac{3}{2} (e + f x) \right] - 72 B c^2 d (e + f x) \cos \left[ \frac{3}{2} (e + f x) \right] - \\
& \quad 72 A c d^2 (e + f x) \cos \left[ \frac{3}{2} (e + f x) \right] + 144 B c d^2 (e + f x) \cos \left[ \frac{3}{2} (e + f x) \right] + \\
& \quad 48 A d^3 (e + f x) \cos \left[ \frac{3}{2} (e + f x) \right] - 84 B d^3 (e + f x) \cos \left[ \frac{3}{2} (e + f x) \right] + \\
& \quad 36 B c d^2 \cos \left[ \frac{5}{2} (e + f x) \right] + 12 A d^3 \cos \left[ \frac{5}{2} (e + f x) \right] - 15 B d^3 \cos \left[ \frac{5}{2} (e + f x) \right] + \\
& \quad 3 B d^3 \cos \left[ \frac{7}{2} (e + f x) \right] + 48 A c^3 \sin \left[ \frac{1}{2} (e + f x) \right] + 48 B c^3 \sin \left[ \frac{1}{2} (e + f x) \right] + \\
& \quad 144 A c^2 d \sin \left[ \frac{1}{2} (e + f x) \right] - 432 B c^2 d \sin \left[ \frac{1}{2} (e + f x) \right] - 432 A c d^2 \sin \left[ \frac{1}{2} (e + f x) \right] + \\
& \quad 792 B c d^2 \sin \left[ \frac{1}{2} (e + f x) \right] + 264 A d^3 \sin \left[ \frac{1}{2} (e + f x) \right] - 381 B d^3 \sin \left[ \frac{1}{2} (e + f x) \right] + \\
& \quad 216 B c^2 d (e + f x) \sin \left[ \frac{1}{2} (e + f x) \right] + 216 A c d^2 (e + f x) \sin \left[ \frac{1}{2} (e + f x) \right] - \\
& \quad 432 B c d^2 (e + f x) \sin \left[ \frac{1}{2} (e + f x) \right] - 144 A d^3 (e + f x) \sin \left[ \frac{1}{2} (e + f x) \right] + \\
& \quad 252 B d^3 (e + f x) \sin \left[ \frac{1}{2} (e + f x) \right] - 108 B c d^2 \sin \left[ \frac{3}{2} (e + f x) \right] - \\
& \quad 36 A d^3 \sin \left[ \frac{3}{2} (e + f x) \right] + 63 B d^3 \sin \left[ \frac{3}{2} (e + f x) \right] + 72 B c^2 d (e + f x) \sin \left[ \frac{3}{2} (e + f x) \right] + \\
& \quad 72 A c d^2 (e + f x) \sin \left[ \frac{3}{2} (e + f x) \right] - 144 B c d^2 (e + f x) \sin \left[ \frac{3}{2} (e + f x) \right] - \\
& \quad 48 A d^3 (e + f x) \sin \left[ \frac{3}{2} (e + f x) \right] + 84 B d^3 (e + f x) \sin \left[ \frac{3}{2} (e + f x) \right] - 36 B c d^2 \sin \left[ \frac{5}{2} (e + f x) \right] - \\
& \quad \left. 12 A d^3 \sin \left[ \frac{5}{2} (e + f x) \right] + 15 B d^3 \sin \left[ \frac{5}{2} (e + f x) \right] + 3 B d^3 \sin \left[ \frac{7}{2} (e + f x) \right] \right)
\end{aligned}$$

**Problem 273: Result more than twice size of optimal antiderivative.**

$$\int \frac{(A + B \sin[e + f x]) (c + d \sin[e + f x])^2}{(a + a \sin[e + f x])^2} dx$$

Optimal (type 3, 132 leaves, 5 steps):

$$\frac{d (2 B (c - d) + A d) x}{a^2} + \frac{(A - 4 B) d^2 \cos[e + f x]}{3 a^2 f} - \frac{(c - d) (2 B (c - 3 d) + A (c + 3 d)) \cos[e + f x]}{3 a^2 f (1 + \sin[e + f x])} - \frac{(A - B) \cos[e + f x] (c + d \sin[e + f x])^2}{3 f (a + a \sin[e + f x])^2}$$

Result (type 3, 338 leaves):

$$\frac{1}{12 a^2 f (1 + \sin[e + f x])^2} \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right) \left( 6 (A d (4 c + d (-4 + 3 e + 3 f x)) + B (2 c^2 + d^2 (5 - 6 e - 6 f x) + 2 c d (-4 + 3 e + 3 f x))) \right. \\ \left. \cos\left[\frac{1}{2}(e + f x)\right] - (B (8 c^2 + d^2 (41 - 12 e - 12 f x) + 4 c d (-10 + 3 e + 3 f x)) + 2 A (2 c^2 + 8 c d + d^2 (-10 + 3 e + 3 f x))) \cos\left[\frac{3}{2}(e + f x)\right] + 3 B d^2 \cos\left[\frac{5}{2}(e + f x)\right] + \right. \\ \left. 6 (2 A c^2 + 2 B c^2 + 4 A c d - 12 B c d - 6 A d^2 + 9 B d^2 + 8 B c d e + 4 A d^2 e - 8 B d^2 e + 8 B c d f x + 4 A d^2 f x - 8 B d^2 f x - 2 d (-2 B c (e + f x) - A d (e + f x) + 2 B d (1 + e + f x))) \cos[e + f x] - \right. \\ \left. B d^2 \cos[2(e + f x)] \right) \sin\left[\frac{1}{2}(e + f x)\right]$$

**Problem 274: Result more than twice size of optimal antiderivative.**

$$\int \frac{(A + B \sin[e + f x]) (c + d \sin[e + f x])}{(a + a \sin[e + f x])^2} dx$$

Optimal (type 3, 85 leaves, 4 steps):

$$\frac{B d x}{a^2} - \frac{(A c + 2 B c + 2 A d - 5 B d) \cos[e + f x]}{3 a^2 f (1 + \sin[e + f x])} - \frac{(A - B) (c - d) \cos[e + f x]}{3 f (a + a \sin[e + f x])^2}$$

Result (type 3, 180 leaves):

$$\left( \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right) \left( 2 (A - B) (c - d) \sin\left[\frac{1}{2}(e + f x)\right] - (A - B) (c - d) \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right) \right) + \right. \\ \left. 2 (A c + 2 B c + 2 A d - 5 B d) \sin\left[\frac{1}{2}(e + f x)\right] \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right)^2 + \right. \\ \left. 3 B d (e + f x) \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right)^3 \right) / \left( 3 a^2 f (1 + \sin[e + f x])^2 \right)$$

**Problem 278: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sin[e + f x]}{(a + a \sin[e + f x])^2 (c + d \sin[e + f x])^3} dx$$

Optimal (type 3, 386 leaves, 8 steps):

$$\left( d (A d (12 c^2 + 16 c d + 7 d^2) - B (6 c^3 + 12 c^2 d + 13 c d^2 + 4 d^3)) \operatorname{ArcTan}\left[\frac{d + c \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}{\sqrt{c^2 - d^2}}\right] \right) /$$

$$\left( a^2 (c - d)^4 (c + d)^2 \sqrt{c^2 - d^2} f \right) -$$

$$\frac{d (A (2 c^2 - 16 c d - 21 d^2) + B (4 c^2 + 19 c d + 12 d^2)) \operatorname{Cos}[e + f x]}{6 a^2 (c - d)^3 (c + d) f (c + d \sin[e + f x])^2} -$$

$$\frac{(A c + 2 B c - 8 A d + 5 B d) \operatorname{Cos}[e + f x]}{3 a^2 (c - d)^2 f (1 + \sin[e + f x]) (c + d \sin[e + f x])^2} -$$

$$\frac{(A - B) \operatorname{Cos}[e + f x]}{3 (c - d) f (a + a \sin[e + f x])^2 (c + d \sin[e + f x])^2} -$$

$$\frac{(d (A (2 c^3 - 16 c^2 d - 59 c d^2 - 32 d^3) + B (4 c^3 + 37 c^2 d + 44 c d^2 + 20 d^3)) \operatorname{Cos}[e + f x]) /}{(6 a^2 (c - d)^4 (c + d)^2 f (c + d \sin[e + f x]))}$$

Result (type 3, 1522 leaves):

$$- \left( \left( d (6 B c^3 - 12 A c^2 d + 12 B c^2 d - 16 A c d^2 + 13 B c d^2 - 7 A d^3 + 4 B d^3) \right. \right.$$

$$\left. \operatorname{ArcTan}\left[\frac{\operatorname{Sec}\left[\frac{1}{2}(e + f x)\right] \left(d \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] + c \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]\right)}{\sqrt{c^2 - d^2}}\right] \right)$$

$$\left( \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] + \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] \right)^4 \right) /$$

$$\left( (c - d)^4 (c + d)^2 \sqrt{c^2 - d^2} f (a + a \sin[e + f x])^2 \right) +$$

$$\frac{1}{48 (c - d)^4 (c + d)^2 f (a + a \sin[e + f x])^2 (c + d \sin[e + f x])^2}$$

$$\left( \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] + \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] \right)$$

$$\left( 48 B c^5 \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] - 96 A c^4 d \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] + 240 B c^4 d \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] - \right.$$

$$524 A c^3 d^2 \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] + 536 B c^3 d^2 \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] -$$

$$\left. 776 A c^2 d^3 \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] + 701 B c^2 d^3 \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] - 487 A c d^4 \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] + \right.$$



$$\begin{aligned}
 & 400 B c d^4 \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] - 112 A d^5 \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] + 70 B d^5 \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] - \\
 & 16 A c^5 \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right] - 32 B c^5 \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right] + 80 A c^4 d \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right] - \\
 & 224 B c^4 d \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right] + 536 A c^3 d^2 \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right] - 728 B c^3 d^2 \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right] + \\
 & 1028 A c^2 d^3 \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right] - 893 B c^2 d^3 \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right] + 695 A c d^4 \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right] - \\
 & 482 B c d^4 \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right] + 134 A d^5 \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right] - 98 B d^5 \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right] + \\
 & 24 B c^3 d^2 \operatorname{Cos}\left[\frac{5}{2}(e+f x)\right] - 12 A c^2 d^3 \operatorname{Cos}\left[\frac{5}{2}(e+f x)\right] + 21 B c^2 d^3 \operatorname{Cos}\left[\frac{5}{2}(e+f x)\right] - \\
 & 15 A c d^4 \operatorname{Cos}\left[\frac{5}{2}(e+f x)\right] - 18 B c d^4 \operatorname{Cos}\left[\frac{5}{2}(e+f x)\right] + 6 A d^5 \operatorname{Cos}\left[\frac{5}{2}(e+f x)\right] - \\
 & 6 B d^5 \operatorname{Cos}\left[\frac{5}{2}(e+f x)\right] + 4 A c^3 d^2 \operatorname{Cos}\left[\frac{7}{2}(e+f x)\right] + 8 B c^3 d^2 \operatorname{Cos}\left[\frac{7}{2}(e+f x)\right] - \\
 & 32 A c^2 d^3 \operatorname{Cos}\left[\frac{7}{2}(e+f x)\right] + 59 B c^2 d^3 \operatorname{Cos}\left[\frac{7}{2}(e+f x)\right] - 97 A c d^4 \operatorname{Cos}\left[\frac{7}{2}(e+f x)\right] + \\
 & 76 B c d^4 \operatorname{Cos}\left[\frac{7}{2}(e+f x)\right] - 52 A d^5 \operatorname{Cos}\left[\frac{7}{2}(e+f x)\right] + 34 B d^5 \operatorname{Cos}\left[\frac{7}{2}(e+f x)\right] + \\
 & 48 A c^5 \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] + 48 B c^5 \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] - 224 A c^4 d \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] + \\
 & 416 B c^4 d \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] - 872 A c^3 d^2 \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] + 992 B c^3 d^2 \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] - \\
 & 1144 A c^2 d^3 \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] + 967 B c^2 d^3 \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] - 685 A c d^4 \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] + \\
 & 496 B c d^4 \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] - 168 A d^5 \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] + 126 B d^5 \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] + \\
 & 48 B c^4 d \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right] - 132 A c^3 d^2 \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right] + 96 B c^3 d^2 \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right] - \\
 & 204 A c^2 d^3 \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right] + 207 B c^2 d^3 \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right] - 165 A c d^4 \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right] + \\
 & 174 B c d^4 \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right] - 66 A d^5 \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right] + 42 B d^5 \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right] - \\
 & 16 A c^4 d \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right] - 32 B c^4 d \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right] + 116 A c^3 d^2 \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right] - \\
 & 224 B c^3 d^2 \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right] + 412 A c^2 d^3 \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right] - 409 B c^2 d^3 \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right] + \\
 & 403 A c d^4 \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right] - 286 B c d^4 \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right] + 114 A d^5 \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right] - \\
 & 78 B d^5 \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right] + 15 B c^2 d^3 \operatorname{Sin}\left[\frac{7}{2}(e+f x)\right] - 21 A c d^4 \operatorname{Sin}\left[\frac{7}{2}(e+f x)\right] + \\
 & 12 B c d^4 \operatorname{Sin}\left[\frac{7}{2}(e+f x)\right] - 12 A d^5 \operatorname{Sin}\left[\frac{7}{2}(e+f x)\right] + 6 B d^5 \operatorname{Sin}\left[\frac{7}{2}(e+f x)\right]
 \end{aligned}$$

**Problem 280: Result more than twice size of optimal antiderivative.**

$$\int \frac{(A + B \sin[e + f x]) (c + d \sin[e + f x])^2}{(a + a \sin[e + f x])^3} dx$$

Optimal (type 3, 164 leaves, 5 steps):

$$\frac{B d^2 x}{a^3} - \frac{(c - d) (B (3 c - 7 d) + 2 A (c + d)) \cos[e + f x]}{15 a f (a + a \sin[e + f x])^2} - \frac{(B (3 c^2 + 14 c d - 29 d^2) + 2 A (c^2 + 3 c d + 2 d^2)) \cos[e + f x]}{15 f (a^3 + a^3 \sin[e + f x])} - \frac{(A - B) \cos[e + f x] (c + d \sin[e + f x])^2}{5 f (a + a \sin[e + f x])^3}$$

Result (type 3, 514 leaves):

$$\frac{1}{60 a^3 f (1 + \sin[e + f x])^3} \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right) \left( 30 (2 A d (c + d) + B (c^2 + 4 c d + d^2 (-9 + 5 e + 5 f x))) \cos\left[\frac{1}{2}(e + f x)\right] - 5 (4 A (c^2 + 3 c d + 2 d^2) + B (6 c^2 + 16 c d + d^2 (-46 + 15 e + 15 f x))) \cos\left[\frac{3}{2}(e + f x)\right] - 15 B d^2 e \cos\left[\frac{5}{2}(e + f x)\right] - 15 B d^2 f x \cos\left[\frac{5}{2}(e + f x)\right] + 40 A c^2 \sin\left[\frac{1}{2}(e + f x)\right] + 30 B c^2 \sin\left[\frac{1}{2}(e + f x)\right] + 60 A c d \sin\left[\frac{1}{2}(e + f x)\right] + 160 B c d \sin\left[\frac{1}{2}(e + f x)\right] + 80 A d^2 \sin\left[\frac{1}{2}(e + f x)\right] - 370 B d^2 \sin\left[\frac{1}{2}(e + f x)\right] + 150 B d^2 e \sin\left[\frac{1}{2}(e + f x)\right] + 150 B d^2 f x \sin\left[\frac{1}{2}(e + f x)\right] + 60 B c d \sin\left[\frac{3}{2}(e + f x)\right] + 30 A d^2 \sin\left[\frac{3}{2}(e + f x)\right] - 90 B d^2 \sin\left[\frac{3}{2}(e + f x)\right] + 75 B d^2 e \sin\left[\frac{3}{2}(e + f x)\right] + 75 B d^2 f x \sin\left[\frac{3}{2}(e + f x)\right] - 4 A c^2 \sin\left[\frac{5}{2}(e + f x)\right] - 6 B c^2 \sin\left[\frac{5}{2}(e + f x)\right] - 12 A c d \sin\left[\frac{5}{2}(e + f x)\right] - 28 B c d \sin\left[\frac{5}{2}(e + f x)\right] - 14 A d^2 \sin\left[\frac{5}{2}(e + f x)\right] + 64 B d^2 \sin\left[\frac{5}{2}(e + f x)\right] - 15 B d^2 e \sin\left[\frac{5}{2}(e + f x)\right] - 15 B d^2 f x \sin\left[\frac{5}{2}(e + f x)\right] \right)$$

**Problem 283: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sin[e + f x]}{(a + a \sin[e + f x])^3 (c + d \sin[e + f x])} dx$$

Optimal (type 3, 229 leaves, 7 steps):

$$\frac{2 d^2 (B c - A d) \operatorname{ArcTan}\left[\frac{d+c \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]}{\sqrt{c^2-d^2}}\right]}{a^3 (c-d)^3 \sqrt{c^2-d^2} f} - \frac{(A-B) \operatorname{Cos}[e+f x]}{5 (c-d) f (a+a \operatorname{Sin}[e+f x])^3} - \frac{(2 A c+3 B c-7 A d+2 B d) \operatorname{Cos}[e+f x]}{15 a (c-d)^2 f (a+a \operatorname{Sin}[e+f x])^2} - \frac{(B(3 c^2-16 c d-2 d^2)+A(2 c^2-9 c d+22 d^2)) \operatorname{Cos}[e+f x]}{15 (c-d)^3 f (a^3+a^3 \operatorname{Sin}[e+f x])}$$

Result (type 3, 502 leaves):

$$\frac{1}{30 a^3 (c-d)^3 f (1+\operatorname{Sin}[e+f x])^3} \left( \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] + \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] \right) \left( 15 B c^2 \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] - 15 A c d \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] - 75 B c d \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] + 75 A d^2 \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] - 10 A c^2 \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right] - 15 B c^2 \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right] + 45 A c d \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right] + 65 B c d \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right] - 95 A d^2 \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right] + 10 B d^2 \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right] + 20 A c^2 \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] + 15 B c^2 \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] - 75 A c d \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] - 85 B c d \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] + 145 A d^2 \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] - 20 B d^2 \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] - \frac{1}{\sqrt{c^2-d^2}} 60 d^2 (-B c + A d) \operatorname{ArcTan}\left[\frac{d+c \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]}{\sqrt{c^2-d^2}}\right] \left( \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] + \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] \right)^5 - 15 B c d \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right] + 15 A d^2 \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right] - 2 A c^2 \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right] - 3 B c^2 \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right] + 9 A c d \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right] + 16 B c d \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right] - 22 A d^2 \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right] + 2 B d^2 \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right] \right)$$

**Problem 284: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Sin}[e + f x]}{(a + a \operatorname{Sin}[e + f x])^3 (c + d \operatorname{Sin}[e + f x])^2} dx$$

Optimal (type 3, 381 leaves, 8 steps):

$$\frac{2 d^2 (A d (4 c+3 d)-B(3 c^2+3 c d+d^2)) \operatorname{ArcTan}\left[\frac{d+c \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]}{\sqrt{c^2-d^2}}\right]}{a^3(c-d)^4(c+d) \sqrt{c^2-d^2} f} - \frac{(d(B(3 c^3-23 c^2 d-63 c d^2-22 d^3)+A(2 c^3-12 c^2 d+43 c d^2+72 d^3)) \operatorname{Cos}[e+f x]) / (15 a^3(c-d)^4(c+d) f(c+d \operatorname{Sin}[e+f x])) - \frac{(A-B) \operatorname{Cos}[e+f x]}{5(c-d) f(a+a \operatorname{Sin}[e+f x])^3(c+d \operatorname{Sin}[e+f x])} - \frac{(2 A c+3 B c-9 A d+4 B d) \operatorname{Cos}[e+f x]}{15 a(c-d)^2 f(a+a \operatorname{Sin}[e+f x])^2(c+d \operatorname{Sin}[e+f x])} - \frac{(B(3 c^2-23 c d-15 d^2)+A(2 c^2-12 c d+45 d^2)) \operatorname{Cos}[e+f x]}{15(c-d)^3 f(a^3+a^3 \operatorname{Sin}[e+f x])(c+d \operatorname{Sin}[e+f x])}}$$

Result (type 3, 1253 leaves):

$$\left(2 d^2(3 B c^2-4 A c d+3 B c d-3 A d^2+B d^2) \operatorname{ArcTan}\left[\frac{\operatorname{Sec}\left[\frac{1}{2}(e+f x)\right](d \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right]+c \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right])}{\sqrt{c^2-d^2}}\right] \left(\operatorname{Cos}\left[\frac{1}{2}(e+f x)\right]+\operatorname{Sin}\left[\frac{1}{2}(e+f x)\right]\right)^6\right) / \left((c-d)^4(c+d) \sqrt{c^2-d^2} f(a+a \operatorname{Sin}[e+f x])^3\right) + \frac{1}{120(c-d)^4(c+d) f(a+a \operatorname{Sin}[e+f x])^3(c+d \operatorname{Sin}[e+f x])} \left(\operatorname{Cos}\left[\frac{1}{2}(e+f x)\right]+\operatorname{Sin}\left[\frac{1}{2}(e+f x)\right]\right) \left(60 B c^4 \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right]-80 A c^3 d \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right]-390 B c^3 d \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right]+540 A c^2 d^2 \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right]-1090 B c^2 d^2 \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right]+1430 A c d^3 \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right]-885 B c d^3 \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right]+735 A d^4 \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right]-320 B d^4 \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right]-40 A c^4 \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right]-60 B c^4 \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right]+196 A c^3 d \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right]+304 B c^3 d \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right]-476 A c^2 d^2 \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right]+1076 B c^2 d^2 \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right]-1546 A c d^3 \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right]+1181 B c d^3 \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right]-969 A d^4 \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right]+334 B d^4 \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right]+60 B c^2 d^2 \operatorname{Cos}\left[\frac{5}{2}(e+f x)\right]-90 A c d^3 \operatorname{Cos}\left[\frac{5}{2}(e+f x)\right]+15 B c d^3 \operatorname{Cos}\left[\frac{5}{2}(e+f x)\right]-15 A d^4 \operatorname{Cos}\left[\frac{5}{2}(e+f x)\right]+30 B d^4 \operatorname{Cos}\left[\frac{5}{2}(e+f x)\right]+4 A c^3 d \operatorname{Cos}\left[\frac{7}{2}(e+f x)\right]+6 B c^3 d \operatorname{Cos}\left[\frac{7}{2}(e+f x)\right]-24 A c^2 d^2 \operatorname{Cos}\left[\frac{7}{2}(e+f x)\right]-46 B c^2 d^2 \operatorname{Cos}\left[\frac{7}{2}(e+f x)\right]+$$

$$\begin{aligned}
 & 86 A c d^3 \cos\left[\frac{7}{2}(e+fx)\right] - 111 B c d^3 \cos\left[\frac{7}{2}(e+fx)\right] + 129 A d^4 \cos\left[\frac{7}{2}(e+fx)\right] - \\
 & 44 B d^4 \cos\left[\frac{7}{2}(e+fx)\right] + 80 A c^4 \sin\left[\frac{1}{2}(e+fx)\right] + 60 B c^4 \sin\left[\frac{1}{2}(e+fx)\right] - \\
 & 340 A c^3 d \sin\left[\frac{1}{2}(e+fx)\right] - 440 B c^3 d \sin\left[\frac{1}{2}(e+fx)\right] + 820 A c^2 d^2 \sin\left[\frac{1}{2}(e+fx)\right] - \\
 & 1520 B c^2 d^2 \sin\left[\frac{1}{2}(e+fx)\right] + 2140 A c d^3 \sin\left[\frac{1}{2}(e+fx)\right] - 1435 B c d^3 \sin\left[\frac{1}{2}(e+fx)\right] + \\
 & 975 A d^4 \sin\left[\frac{1}{2}(e+fx)\right] - 340 B d^4 \sin\left[\frac{1}{2}(e+fx)\right] - 90 B c^3 d \sin\left[\frac{3}{2}(e+fx)\right] + \\
 & 120 A c^2 d^2 \sin\left[\frac{3}{2}(e+fx)\right] - 390 B c^2 d^2 \sin\left[\frac{3}{2}(e+fx)\right] + 540 A c d^3 \sin\left[\frac{3}{2}(e+fx)\right] - \\
 & 315 B c d^3 \sin\left[\frac{3}{2}(e+fx)\right] + 285 A d^4 \sin\left[\frac{3}{2}(e+fx)\right] - 150 B d^4 \sin\left[\frac{3}{2}(e+fx)\right] - \\
 & 8 A c^4 \sin\left[\frac{5}{2}(e+fx)\right] - 12 B c^4 \sin\left[\frac{5}{2}(e+fx)\right] + 28 A c^3 d \sin\left[\frac{5}{2}(e+fx)\right] + \\
 & 62 B c^3 d \sin\left[\frac{5}{2}(e+fx)\right] - 52 A c^2 d^2 \sin\left[\frac{5}{2}(e+fx)\right] + 362 B c^2 d^2 \sin\left[\frac{5}{2}(e+fx)\right] - \\
 & 568 A c d^3 \sin\left[\frac{5}{2}(e+fx)\right] + 553 B c d^3 \sin\left[\frac{5}{2}(e+fx)\right] - 555 A d^4 \sin\left[\frac{5}{2}(e+fx)\right] + \\
 & 190 B d^4 \sin\left[\frac{5}{2}(e+fx)\right] - 15 B c d^3 \sin\left[\frac{7}{2}(e+fx)\right] + 15 A d^4 \sin\left[\frac{7}{2}(e+fx)\right]
 \end{aligned}$$

**Problem 290: Result is not expressed in closed-form.**

$$\int \frac{\sqrt{a+a \sin[e+fx]} (A+B \sin[e+fx])}{c+d \sin[e+fx]} dx$$

Optimal (type 3, 100 leaves, 3 steps):

$$\frac{2 \sqrt{a} (B c - A d) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{d} \cos[e+fx]}{\sqrt{c+d} \sqrt{a+a \sin[e+fx]}}\right]}{d^{3/2} \sqrt{c+d} f} - \frac{2 a B \cos[e+fx]}{d f \sqrt{a+a \sin[e+fx]}}$$

Result (type 7, 903 leaves):

$$\begin{aligned}
 & \frac{1}{d^{3/2} \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)} \left( \frac{1}{2} + \frac{i}{2} \right) \left( -\frac{(2-2i) B \sqrt{d} \cos\left[\frac{fx}{2}\right] \left( \cos\left[\frac{e}{2}\right] - \sin\left[\frac{e}{2}\right] \right)}{f} + \right. \\
 & \frac{1}{\sqrt{c+d} \left( \cos[e] + i(-1+\sin[e]) \right) \sqrt{\cos[e] - i \sin[e]}} (-Bc + Ad) \left( \cos\left[\frac{e}{2}\right] + i \sin\left[\frac{e}{2}\right] \right) \\
 & \left( (-1+i) \times \cos[e] + \frac{1}{4f} \text{RootSum}\left[-d + 2ic e^{ie} \#1^2 + d e^{2ie} \#1^4\right] \&, \frac{1}{d - ic e^{ie} \#1^2} \right. \\
 & \left( (1+i) d \sqrt{e^{-ie}} fx - (2-2i) d \sqrt{e^{-ie}} \text{Log}\left[e^{\frac{ifx}{2}} - \#1\right] - i \sqrt{d} \sqrt{c+d} fx \#1 + \right. \\
 & 2 \sqrt{d} \sqrt{c+d} \text{Log}\left[e^{\frac{ifx}{2}} - \#1\right] \#1 + \frac{(1-i) c fx \#1^2}{\sqrt{e^{-ie}}} + \frac{(2+2i) c \text{Log}\left[e^{\frac{ifx}{2}} - \#1\right] \#1^2}{\sqrt{e^{-ie}}} - \\
 & \left. \left. \sqrt{d} \sqrt{c+d} e^{ie} fx \#1^3 - 2i \sqrt{d} \sqrt{c+d} e^{ie} \text{Log}\left[e^{\frac{ifx}{2}} - \#1\right] \#1^3 \right) \& \right) \\
 & \left. \left( \cos[e] + i(-1+\sin[e]) \right) \sqrt{\cos[e] - i \sin[e]} + (1+i) \times \sin[e] \right) + \\
 & \frac{1}{\sqrt{c+d} \left( \cos[e] + i(-1+\sin[e]) \right) \sqrt{\cos[e] - i \sin[e]}} \\
 & (-Bc + Ad) \left( \cos\left[\frac{e}{2}\right] + i \sin\left[\frac{e}{2}\right] \right) \\
 & \left( (1-i) \times \cos[e] - (1+i) \times \sin[e] + \frac{1}{4f} \text{RootSum}\left[-d + 2ic e^{ie} \#1^2 + d e^{2ie} \#1^4\right] \&, \right. \\
 & \frac{1}{d - ic e^{ie} \#1^2} \left( (1-i) d \sqrt{e^{-ie}} fx + (2+2i) d \sqrt{e^{-ie}} \text{Log}\left[e^{\frac{ifx}{2}} - \#1\right] + \right. \\
 & \left. \sqrt{d} \sqrt{c+d} fx \#1 + 2i \sqrt{d} \sqrt{c+d} \text{Log}\left[e^{\frac{ifx}{2}} - \#1\right] \#1 - \frac{(1+i) c fx \#1^2}{\sqrt{e^{-ie}}} + \right. \\
 & \left. \frac{(2-2i) c \text{Log}\left[e^{\frac{ifx}{2}} - \#1\right] \#1^2}{\sqrt{e^{-ie}}} - i \sqrt{d} \sqrt{c+d} e^{ie} fx \#1^3 + 2 \sqrt{d} \sqrt{c+d} e^{ie} \right. \\
 & \left. \left. \text{Log}\left[e^{\frac{ifx}{2}} - \#1\right] \#1^3 \right) \& \sqrt{\cos[e] - i \sin[e]} (-1 - i \cos[e] + \sin[e]) \right) + \\
 & \left. \frac{(2-2i) B \sqrt{d} \left( \cos\left[\frac{e}{2}\right] + \sin\left[\frac{e}{2}\right] \right) \sin\left[\frac{fx}{2}\right]}{f} \right) \sqrt{a(1+\sin[e+fx])}
 \end{aligned}$$

Problem 291: Result is not expressed in closed-form.

$$\int \frac{\sqrt{a + a \sin[e + f x]} (A + B \sin[e + f x])}{(c + d \sin[e + f x])^2} dx$$

Optimal (type 3, 126 leaves, 3 steps):

$$-\frac{\sqrt{a} (A d + B (c + 2 d)) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{d} \cos[e + f x]}{\sqrt{c+d} \sqrt{a+a \sin[e+f x]}}\right]}{d^{3/2} (c+d)^{3/2} f} + \frac{a (B c - A d) \cos[e + f x]}{d (c+d) f \sqrt{a + a \sin[e + f x]} (c + d \sin[e + f x])}$$

Result (type 7, 901 leaves):

$$\begin{aligned}
 & \frac{1}{d^{3/2} \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)} \\
 & \left( \frac{1}{4} + \frac{i}{4} \right) \sqrt{a(1+\sin[e+fx])} \left( \frac{1}{(c+d)^{3/2} (\cos[e] + i(-1+\sin[e])) \sqrt{\cos[e] - i\sin[e]}} \right. \\
 & (Ad+B(c+2d)) \left( \cos\left[\frac{e}{2}\right] + i\sin\left[\frac{e}{2}\right] \right) \\
 & \left( (-1+i) \times \cos[e] + \frac{1}{4f} \text{RootSum}[-d+2ic e^{ie} \#1^2 + d e^{2ie} \#1^4] \&, \frac{1}{d-i c e^{ie} \#1^2} \right. \\
 & \left( (1+i) d \sqrt{e^{-ie}} fx - (2-2i) d \sqrt{e^{-ie}} \text{Log}\left[e^{\frac{ifx}{2}} - \#1\right] - i \sqrt{d} \sqrt{c+d} fx \#1 + \right. \\
 & 2 \sqrt{d} \sqrt{c+d} \text{Log}\left[e^{\frac{ifx}{2}} - \#1\right] \#1 + \frac{(1-i) c fx \#1^2}{\sqrt{e^{-ie}}} + \frac{(2+2i) c \text{Log}\left[e^{\frac{ifx}{2}} - \#1\right] \#1^2}{\sqrt{e^{-ie}}} - \\
 & \left. \left. \sqrt{d} \sqrt{c+d} e^{ie} fx \#1^3 - 2i \sqrt{d} \sqrt{c+d} e^{ie} \text{Log}\left[e^{\frac{ifx}{2}} - \#1\right] \#1^3 \right) \& \right) \\
 & \left. \left( \cos[e] + i(-1+\sin[e]) \right) \sqrt{\cos[e] - i\sin[e]} + (1+i) \times \sin[e] \right) + \\
 & \frac{1}{(c+d)^{3/2} (\cos[e] + i(-1+\sin[e])) \sqrt{\cos[e] - i\sin[e]}} \\
 & (Ad+B(c+2d)) \left( \cos\left[\frac{e}{2}\right] + i\sin\left[\frac{e}{2}\right] \right) \\
 & \left( (1-i) \times \cos[e] - (1+i) \times \sin[e] + \frac{1}{4f} \text{RootSum}[-d+2ic e^{ie} \#1^2 + d e^{2ie} \#1^4] \&, \right. \\
 & \frac{1}{d-i c e^{ie} \#1^2} \left( (1-i) d \sqrt{e^{-ie}} fx + (2+2i) d \sqrt{e^{-ie}} \text{Log}\left[e^{\frac{ifx}{2}} - \#1\right] + \right. \\
 & \left. \sqrt{d} \sqrt{c+d} fx \#1 + 2i \sqrt{d} \sqrt{c+d} \text{Log}\left[e^{\frac{ifx}{2}} - \#1\right] \#1 - \frac{(1+i) c fx \#1^2}{\sqrt{e^{-ie}}} + \right. \\
 & \left. \frac{(2-2i) c \text{Log}\left[e^{\frac{ifx}{2}} - \#1\right] \#1^2}{\sqrt{e^{-ie}}} - i \sqrt{d} \sqrt{c+d} e^{ie} fx \#1^3 + 2 \sqrt{d} \sqrt{c+d} e^{ie} \right. \\
 & \left. \left. \text{Log}\left[e^{\frac{ifx}{2}} - \#1\right] \#1^3 \right) \& \right) \sqrt{\cos[e] - i\sin[e]} (-1-i \cos[e] + \sin[e]) \left. \right) - \\
 & \frac{(2-2i) \sqrt{d} (-Bc+Ad) \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)}{(c+d) f (c+d \sin[e+fx])}
 \end{aligned}$$



### Problem 292: Result is not expressed in closed-form.

$$\int \frac{\sqrt{a + a \sin[e + f x]} (A + B \sin[e + f x])}{(c + d \sin[e + f x])^3} dx$$

Optimal (type 3, 192 leaves, 4 steps):

$$\frac{\sqrt{a} (3 A d + B (c + 4 d)) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{d} \cos[e + f x]}{\sqrt{c+d} \sqrt{a+a \sin[e+f x]}}\right]}{4 d^{3/2} (c+d)^{5/2} f} + \frac{a (B c - A d) \cos[e + f x]}{2 d (c+d) f \sqrt{a+a \sin[e+f x]} (c+d \sin[e+f x])^2} - \frac{a (3 A d + B (c + 4 d)) \cos[e + f x]}{4 d (c+d)^2 f \sqrt{a+a \sin[e+f x]} (c+d \sin[e+f x])}$$

Result (type 7, 967 leaves):

$$\frac{1}{d^{3/2} \left( \cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right)} \left( \frac{1}{16} + \frac{i}{16} \right) \sqrt{a (1 + \sin[e + f x])} \left( \frac{1}{(c+d)^{5/2} (\cos[e] + i(-1 + \sin[e])) \sqrt{\cos[e] - i \sin[e]}} \right. \\ \left. (3 A d + B (c + 4 d)) \left( \cos\left[\frac{e}{2}\right] + i \sin\left[\frac{e}{2}\right] \right) \left( (-1 + i) \times \cos[e] + \frac{1}{4 f} \operatorname{RootSum}\left[-d + 2 i c e^{i e} \#1^2 + d e^{2 i e} \#1^4 \&, \frac{1}{d - i c e^{i e} \#1^2} \right. \right. \right. \\ \left. \left. \left( (1 + i) d \sqrt{e^{-i e}} f x - (2 - 2 i) d \sqrt{e^{-i e}} \operatorname{Log}\left[e^{\frac{i f x}{2}} - \#1\right] - i \sqrt{d} \sqrt{c+d} f x \#1 + \right. \right. \right. \\ \left. \left. \left. 2 \sqrt{d} \sqrt{c+d} \operatorname{Log}\left[e^{\frac{i f x}{2}} - \#1\right] \#1 + \frac{(1 - i) c f x \#1^2}{\sqrt{e^{-i e}}} + \frac{(2 + 2 i) c \operatorname{Log}\left[e^{\frac{i f x}{2}} - \#1\right] \#1^2}{\sqrt{e^{-i e}}} - \right. \right. \right. \\ \left. \left. \left. \sqrt{d} \sqrt{c+d} e^{i e} f x \#1^3 - 2 i \sqrt{d} \sqrt{c+d} e^{i e} \operatorname{Log}\left[e^{\frac{i f x}{2}} - \#1\right] \#1^3 \right) \& \right) \\ \left. (\cos[e] + i(-1 + \sin[e])) \sqrt{\cos[e] - i \sin[e]} + (1 + i) \times \sin[e] \right) + \frac{1}{(c+d)^{5/2} (\cos[e] + i(-1 + \sin[e])) \sqrt{\cos[e] - i \sin[e]}} \\ (3 A d + B (c + 4 d)) \left( \cos\left[\frac{e}{2}\right] + i \sin\left[\frac{e}{2}\right] \right)$$

$$\left( (1-i) x \cos[e] - (1+i) x \sin[e] + \frac{1}{4f} \text{RootSum}[-d + 2i c e^{ie} \#1^2 + d e^{2ie} \#1^4 \&, \right.$$

$$\frac{1}{d-i c e^{ie} \#1^2} \left( (1-i) d \sqrt{e^{-ie}} f x + (2+2i) d \sqrt{e^{-ie}} \text{Log}\left[e^{\frac{ifx}{2}} - \#1\right] + \right.$$

$$\sqrt{d} \sqrt{c+d} f x \#1 + 2i \sqrt{d} \sqrt{c+d} \text{Log}\left[e^{\frac{ifx}{2}} - \#1\right] \#1 - \frac{(1+i) c f x \#1^2}{\sqrt{e^{-ie}}} +$$

$$\frac{(2-2i) c \text{Log}\left[e^{\frac{ifx}{2}} - \#1\right] \#1^2}{\sqrt{e^{-ie}}} - i \sqrt{d} \sqrt{c+d} e^{ie} f x \#1^3 + 2 \sqrt{d} \sqrt{c+d} e^{ie}$$

$$\left. \text{Log}\left[e^{\frac{ifx}{2}} - \#1\right] \#1^3 \right) \& \sqrt{\cos[e] - i \sin[e]} (-1 - i \cos[e] + \sin[e]) \left. \right) -$$

$$\frac{(4-4i) \sqrt{d} (-Bc + Ad) \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)}{(c+d) f (c+d \sin[e+fx])^2} -$$

$$\left( (2-2i) \sqrt{d} (3Ad + B(c+4d)) \left( \cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right) \right) /$$

$$\left( (c+d)^2 f (c+d \sin[e+fx]) \right)$$

**Problem 293: Result more than twice size of optimal antiderivative.**

$$\int (a + a \sin[e + fx])^{3/2} (A + B \sin[e + fx]) (c + d \sin[e + fx])^3 dx$$

Optimal (type 3, 374 leaves, 6 steps):

$$\frac{(4a^2(c+d)(15c^2+10cd+7d^2)(11A(c-17d)d-3B(c^2-9cd+56d^2))\cos[e+fx])}{(3465d^2f\sqrt{a+a\sin[e+fx]})} + \frac{1}{3465df}$$

$$+ \frac{8a(5c-d)(c+d)(11A(c-17d)d-3B(c^2-9cd+56d^2))\cos[e+fx]\sqrt{a+a\sin[e+fx]}}{1155f} +$$

$$\frac{1}{1155f} 4(c+d)(11A(c-17d)d-3B(c^2-9cd+56d^2))\cos[e+fx](a+a\sin[e+fx])^{3/2} +$$

$$\frac{(2a^2(11A(c-17d)d-3B(c^2-9cd+56d^2))\cos[e+fx](c+d\sin[e+fx])^3)}{(693d^2f\sqrt{a+a\sin[e+fx]})} + \frac{2a^2(3B(c-4d)-11Ad)\cos[e+fx](c+d\sin[e+fx])^4}{99d^2f\sqrt{a+a\sin[e+fx]}}$$

$$- \frac{2aB\cos[e+fx]\sqrt{a+a\sin[e+fx]}(c+d\sin[e+fx])^4}{11df}$$

Result (type 3, 1101 leaves):

1

$$\begin{aligned}
 & 55440 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^3 \\
 & \left( a \left( 1 + \sin [e + f x] \right) \right)^{3/2} \left( -166320 A c^3 \cos \left[ \frac{1}{2} (e + f x) \right] - 110880 B c^3 \cos \left[ \frac{1}{2} (e + f x) \right] - \right. \\
 & \quad 332640 A c^2 d \cos \left[ \frac{1}{2} (e + f x) \right] - 291060 B c^2 d \cos \left[ \frac{1}{2} (e + f x) \right] - \\
 & \quad 291060 A c d^2 \cos \left[ \frac{1}{2} (e + f x) \right] - 249480 B c d^2 \cos \left[ \frac{1}{2} (e + f x) \right] - 83160 A d^3 \cos \left[ \frac{1}{2} (e + f x) \right] - \\
 & \quad 76230 B d^3 \cos \left[ \frac{1}{2} (e + f x) \right] - 18480 A c^3 \cos \left[ \frac{3}{2} (e + f x) \right] - 27720 B c^3 \cos \left[ \frac{3}{2} (e + f x) \right] - \\
 & \quad 83160 A c^2 d \cos \left[ \frac{3}{2} (e + f x) \right] - 69300 B c^2 d \cos \left[ \frac{3}{2} (e + f x) \right] - 69300 A c d^2 \cos \left[ \frac{3}{2} (e + f x) \right] - \\
 & \quad 69300 B c d^2 \cos \left[ \frac{3}{2} (e + f x) \right] - 23100 A d^3 \cos \left[ \frac{3}{2} (e + f x) \right] - 20790 B d^3 \cos \left[ \frac{3}{2} (e + f x) \right] + \\
 & \quad 5544 B c^3 \cos \left[ \frac{5}{2} (e + f x) \right] + 16632 A c^2 d \cos \left[ \frac{5}{2} (e + f x) \right] + 24948 B c^2 d \cos \left[ \frac{5}{2} (e + f x) \right] + \\
 & \quad 24948 A c d^2 \cos \left[ \frac{5}{2} (e + f x) \right] + 24948 B c d^2 \cos \left[ \frac{5}{2} (e + f x) \right] + 8316 A d^3 \cos \left[ \frac{5}{2} (e + f x) \right] + \\
 & \quad 9009 B d^3 \cos \left[ \frac{5}{2} (e + f x) \right] + 5940 B c^2 d \cos \left[ \frac{7}{2} (e + f x) \right] + 5940 A c d^2 \cos \left[ \frac{7}{2} (e + f x) \right] + \\
 & \quad 8910 B c d^2 \cos \left[ \frac{7}{2} (e + f x) \right] + 2970 A d^3 \cos \left[ \frac{7}{2} (e + f x) \right] + 3465 B d^3 \cos \left[ \frac{7}{2} (e + f x) \right] - \\
 & \quad 2310 B c d^2 \cos \left[ \frac{9}{2} (e + f x) \right] - 770 A d^3 \cos \left[ \frac{9}{2} (e + f x) \right] - 1155 B d^3 \cos \left[ \frac{9}{2} (e + f x) \right] - \\
 & \quad 315 B d^3 \cos \left[ \frac{11}{2} (e + f x) \right] + 166320 A c^3 \sin \left[ \frac{1}{2} (e + f x) \right] + 110880 B c^3 \sin \left[ \frac{1}{2} (e + f x) \right] + \\
 & \quad 332640 A c^2 d \sin \left[ \frac{1}{2} (e + f x) \right] + 291060 B c^2 d \sin \left[ \frac{1}{2} (e + f x) \right] + 291060 A c d^2 \sin \left[ \frac{1}{2} (e + f x) \right] + \\
 & \quad 249480 B c d^2 \sin \left[ \frac{1}{2} (e + f x) \right] + 83160 A d^3 \sin \left[ \frac{1}{2} (e + f x) \right] + 76230 B d^3 \sin \left[ \frac{1}{2} (e + f x) \right] - \\
 & \quad 18480 A c^3 \sin \left[ \frac{3}{2} (e + f x) \right] - 27720 B c^3 \sin \left[ \frac{3}{2} (e + f x) \right] - 83160 A c^2 d \sin \left[ \frac{3}{2} (e + f x) \right] - \\
 & \quad 69300 B c^2 d \sin \left[ \frac{3}{2} (e + f x) \right] - 69300 A c d^2 \sin \left[ \frac{3}{2} (e + f x) \right] - 69300 B c d^2 \sin \left[ \frac{3}{2} (e + f x) \right] - \\
 & \quad 23100 A d^3 \sin \left[ \frac{3}{2} (e + f x) \right] - 20790 B d^3 \sin \left[ \frac{3}{2} (e + f x) \right] - 5544 B c^3 \sin \left[ \frac{5}{2} (e + f x) \right] - \\
 & \quad 16632 A c^2 d \sin \left[ \frac{5}{2} (e + f x) \right] - 24948 B c^2 d \sin \left[ \frac{5}{2} (e + f x) \right] - 24948 A c d^2 \sin \left[ \frac{5}{2} (e + f x) \right] - \\
 & \quad 24948 B c d^2 \sin \left[ \frac{5}{2} (e + f x) \right] - 8316 A d^3 \sin \left[ \frac{5}{2} (e + f x) \right] - 9009 B d^3 \sin \left[ \frac{5}{2} (e + f x) \right] + \\
 & \quad 5940 B c^2 d \sin \left[ \frac{7}{2} (e + f x) \right] + 5940 A c d^2 \sin \left[ \frac{7}{2} (e + f x) \right] + 8910 B c d^2 \sin \left[ \frac{7}{2} (e + f x) \right] + \\
 & \quad 2970 A d^3 \sin \left[ \frac{7}{2} (e + f x) \right] + 3465 B d^3 \sin \left[ \frac{7}{2} (e + f x) \right] + 2310 B c d^2 \sin \left[ \frac{9}{2} (e + f x) \right] + \\
 & \quad \left. 770 A d^3 \sin \left[ \frac{9}{2} (e + f x) \right] + 1155 B d^3 \sin \left[ \frac{9}{2} (e + f x) \right] - 315 B d^3 \sin \left[ \frac{11}{2} (e + f x) \right] \right)
 \end{aligned}$$

**Problem 297: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sin[e + f x])^{3/2} (A + B \sin[e + f x])}{c + d \sin[e + f x]} dx$$

Optimal (type 3, 153 leaves, 4 steps):

$$\frac{2 a^{3/2} (c - d) (B c - A d) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{d} \cos[e + f x]}{\sqrt{c+d} \sqrt{a+a \sin[e + f x]}}\right]}{d^{5/2} \sqrt{c+d} f} + \frac{2 a^2 (3 B c - 3 A d - 4 B d) \cos[e + f x]}{3 d^2 f \sqrt{a+a \sin[e + f x]}} - \frac{2 a B \cos[e + f x] \sqrt{a+a \sin[e + f x]}}{3 d f}$$

Result (type 3, 356 leaves):

$$\frac{1}{6 d^{5/2} f \left( \cos\left[\frac{1}{2} (e + f x)\right] + \sin\left[\frac{1}{2} (e + f x)\right] \right)^3} \left( (a (1 + \sin[e + f x]))^{3/2} \left( -6 \sqrt{d} (-2 B c + 2 A d + 3 B d) \cos\left[\frac{1}{2} (e + f x)\right] - 2 B d^{3/2} \cos\left[\frac{3}{2} (e + f x)\right] \right) - \frac{1}{\sqrt{c+d}} 3 (c - d) (B c - A d) \left( e + f x - 2 \operatorname{Log}\left[\operatorname{Sec}\left[\frac{1}{4} (e + f x)\right]^2\right] + 2 \operatorname{Log}\left[-\operatorname{Sec}\left[\frac{1}{4} (e + f x)\right]^2\right] \right) \left( c + d + \sqrt{d} \sqrt{c+d} \cos\left[\frac{1}{2} (e + f x)\right] - \sqrt{d} \sqrt{c+d} \sin\left[\frac{1}{2} (e + f x)\right] \right) \right) + \frac{1}{\sqrt{c+d}} 3 (c - d) (B c - A d) \left( e + f x - 2 \operatorname{Log}\left[\operatorname{Sec}\left[\frac{1}{4} (e + f x)\right]^2\right] + 2 \operatorname{Log}\left[ (c + d) \operatorname{Sec}\left[\frac{1}{4} (e + f x)\right]^2 + \sqrt{d} \sqrt{c+d} \left( -1 + 2 \operatorname{Tan}\left[\frac{1}{4} (e + f x)\right] + \operatorname{Tan}\left[\frac{1}{4} (e + f x)\right]^2 \right) \right] \right) + 6 \sqrt{d} (-2 B c + 2 A d + 3 B d) \sin\left[\frac{1}{2} (e + f x)\right] - 2 B d^{3/2} \sin\left[\frac{3}{2} (e + f x)\right] \right)$$

**Problem 300: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (a + a \sin[e + f x])^{5/2} (A + B \sin[e + f x]) (c + d \sin[e + f x])^3 dx$$

Optimal (type 3, 534 leaves, 7 steps):

$$\begin{aligned}
 & - \left( (4 a^3 (c+d) (15 c^2 + 10 c d + 7 d^2) \right. \\
 & \quad \left. (13 A d (3 c^2 - 38 c d + 355 d^2) - B (15 c^3 - 150 c^2 d + 799 c d^2 - 4184 d^3)) \cos [e+f x] \right) / \\
 & \quad \left( 45 045 d^3 f \sqrt{a+a \sin [e+f x]} \right) - \frac{1}{45 045 d^2 f} 8 a^2 (5 c-d) (c+d) \\
 & \quad \left( 13 A d (3 c^2 - 38 c d + 355 d^2) - B (15 c^3 - 150 c^2 d + 799 c d^2 - 4184 d^3) \right) \\
 & \quad \cos [e+f x] \sqrt{a+a \sin [e+f x]} - \frac{1}{15 015 d f} \\
 & 4 a (c+d) (13 A d (3 c^2 - 38 c d + 355 d^2) - B (15 c^3 - 150 c^2 d + 799 c d^2 - 4184 d^3)) \\
 & \quad \cos [e+f x] (a+a \sin [e+f x])^{3/2} - \\
 & \quad \left( 2 a^3 (13 A d (3 c^2 - 38 c d + 355 d^2) - B (15 c^3 - 150 c^2 d + 799 c d^2 - 4184 d^3)) \right. \\
 & \quad \left. \cos [e+f x] (c+d \sin [e+f x])^3 \right) / \left( 9009 d^3 f \sqrt{a+a \sin [e+f x]} \right) - \\
 & \quad \left( 2 a^3 (15 B c^2 - 39 A c d - 75 B c d + 299 A d^2 + 280 B d^2) \cos [e+f x] (c+d \sin [e+f x])^4 \right) / \\
 & \quad \left( 1287 d^3 f \sqrt{a+a \sin [e+f x]} \right) + \frac{1}{143 d^2 f} \\
 & 2 a^2 (5 B c - 13 A d - 16 B d) \cos [e+f x] \sqrt{a+a \sin [e+f x]} (c+d \sin [e+f x])^4 - \\
 & \quad \frac{2 a B \cos [e+f x] (a+a \sin [e+f x])^{3/2} (c+d \sin [e+f x])^4}{13 d f}
 \end{aligned}$$

Result (type 3, 1565 leaves):

$$\begin{aligned}
 & \frac{B d^3 \cos \left[ \frac{13}{2} (e+f x) \right] (a (1 + \sin [e+f x]))^{5/2}}{416 f \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right)^5} + \\
 & \quad \left( (40 A c^3 + 30 B c^3 + 90 A c^2 d + 78 B c^2 d + 78 A c d^2 + 69 B c d^2 + 23 A d^3 + 21 B d^3) \right. \\
 & \quad \left. \left( \left( -\frac{1}{16} - \frac{i}{16} \right) \cos \left[ \frac{1}{2} (e+f x) \right] + \left( \frac{1}{16} - \frac{i}{16} \right) \sin \left[ \frac{1}{2} (e+f x) \right] \right) (a (1 + \sin [e+f x]))^{5/2} \right) / \\
 & \quad \left( f \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right)^5 \right) + \\
 & \quad \left( (40 A c^3 + 30 B c^3 + 90 A c^2 d + 78 B c^2 d + 78 A c d^2 + 69 B c d^2 + 23 A d^3 + 21 B d^3) \right. \\
 & \quad \left. \left( \left( -\frac{1}{16} + \frac{i}{16} \right) \cos \left[ \frac{1}{2} (e+f x) \right] + \left( \frac{1}{16} + \frac{i}{16} \right) \sin \left[ \frac{1}{2} (e+f x) \right] \right) (a (1 + \sin [e+f x]))^{5/2} \right) / \\
 & \quad \left( f \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right)^5 \right) + \\
 & \quad \left( (80 A c^3 + 88 B c^3 + 264 A c^2 d + 240 B c^2 d + 240 A c d^2 + 228 B c d^2 + 76 A d^3 + 71 B d^3) \right. \\
 & \quad \left. (a (1 + \sin [e+f x]))^{5/2} \left( \left( -\frac{1}{192} + \frac{i}{192} \right) \cos \left[ \frac{3}{2} (e+f x) \right] - \left( \frac{1}{192} + \frac{i}{192} \right) \sin \left[ \frac{3}{2} (e+f x) \right] \right) \right) / \\
 & \quad \left( f \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right)^5 \right) + \\
 & \quad \left( (80 A c^3 + 88 B c^3 + 264 A c^2 d + 240 B c^2 d + 240 A c d^2 + 228 B c d^2 + 76 A d^3 + 71 B d^3) \right. \\
 & \quad \left. (a (1 + \sin [e+f x]))^{5/2} \left( \left( -\frac{1}{192} - \frac{i}{192} \right) \cos \left[ \frac{3}{2} (e+f x) \right] - \left( \frac{1}{192} - \frac{i}{192} \right) \sin \left[ \frac{3}{2} (e+f x) \right] \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
& \left( f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^5 + \\
& \left( (16 A c^3 + 40 B c^3 + 120 A c^2 d + 144 B c^2 d + 144 A c d^2 + 150 B c d^2 + 50 A d^3 + 51 B d^3) \right. \\
& \quad \left. (a (1 + \sin[e + f x]))^{5/2} \left( \left( \frac{1}{320} - \frac{i}{320} \right) \cos \left[ \frac{5}{2} (e + f x) \right] - \left( \frac{1}{320} + \frac{i}{320} \right) \sin \left[ \frac{5}{2} (e + f x) \right] \right) \right) / \\
& \left( f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^5 + \\
& \left( (16 A c^3 + 40 B c^3 + 120 A c^2 d + 144 B c^2 d + 144 A c d^2 + 150 B c d^2 + 50 A d^3 + 51 B d^3) \right. \\
& \quad \left. (a (1 + \sin[e + f x]))^{5/2} \left( \left( \frac{1}{320} + \frac{i}{320} \right) \cos \left[ \frac{5}{2} (e + f x) \right] - \left( \frac{1}{320} - \frac{i}{320} \right) \sin \left[ \frac{5}{2} (e + f x) \right] \right) \right) / \\
& \left( f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^5 + \\
& \left( (4 B c^3 + 12 A c^2 d + 30 B c^2 d + 30 A c d^2 + 39 B c d^2 + 13 A d^3 + 15 B d^3) (a (1 + \sin[e + f x]))^{5/2} \right. \\
& \quad \left. \left( \left( \frac{1}{224} + \frac{i}{224} \right) \cos \left[ \frac{7}{2} (e + f x) \right] + \left( \frac{1}{224} - \frac{i}{224} \right) \sin \left[ \frac{7}{2} (e + f x) \right] \right) \right) / \\
& \left( f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^5 + \\
& \left( (4 B c^3 + 12 A c^2 d + 30 B c^2 d + 30 A c d^2 + 39 B c d^2 + 13 A d^3 + 15 B d^3) (a (1 + \sin[e + f x]))^{5/2} \right. \\
& \quad \left. \left( \left( \frac{1}{224} - \frac{i}{224} \right) \cos \left[ \frac{7}{2} (e + f x) \right] + \left( \frac{1}{224} + \frac{i}{224} \right) \sin \left[ \frac{7}{2} (e + f x) \right] \right) \right) / \\
& \left( f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^5 + \\
& \left( (6 B c^2 + 6 A c d + 15 B c d + 5 A d^2 + 7 B d^2) (a (1 + \sin[e + f x]))^{5/2} \right. \\
& \quad \left. \left( \left( -\frac{1}{288} - \frac{i}{288} \right) d \cos \left[ \frac{9}{2} (e + f x) \right] + \left( \frac{1}{288} - \frac{i}{288} \right) d \sin \left[ \frac{9}{2} (e + f x) \right] \right) \right) / \\
& \left( f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^5 + \\
& \left( (6 B c^2 + 6 A c d + 15 B c d + 5 A d^2 + 7 B d^2) (a (1 + \sin[e + f x]))^{5/2} \right. \\
& \quad \left. \left( \left( -\frac{1}{288} + \frac{i}{288} \right) d \cos \left[ \frac{9}{2} (e + f x) \right] + \left( \frac{1}{288} + \frac{i}{288} \right) d \sin \left[ \frac{9}{2} (e + f x) \right] \right) \right) / \\
& \left( f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^5 + \left( (6 B c + 2 A d + 5 B d) (a (1 + \sin[e + f x]))^{5/2} \right. \\
& \quad \left. \left( \left( -\frac{1}{704} + \frac{i}{704} \right) d^2 \cos \left[ \frac{11}{2} (e + f x) \right] - \left( \frac{1}{704} + \frac{i}{704} \right) d^2 \sin \left[ \frac{11}{2} (e + f x) \right] \right) \right) / \\
& \left( f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^5 + \left( (6 B c + 2 A d + 5 B d) (a (1 + \sin[e + f x]))^{5/2} \right. \\
& \quad \left. \left( \left( -\frac{1}{704} - \frac{i}{704} \right) d^2 \cos \left[ \frac{11}{2} (e + f x) \right] - \left( \frac{1}{704} - \frac{i}{704} \right) d^2 \sin \left[ \frac{11}{2} (e + f x) \right] \right) \right) /
\end{aligned}$$

$$\left( f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right)^5 - \frac{B d^3 (a (1 + \sin [e + f x]))^{5/2} \sin \left[ \frac{13}{2} (e + f x) \right]}{416 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^5}$$

**Problem 301: Result more than twice size of optimal antiderivative.**

$$\int (a + a \sin [e + f x])^{5/2} (A + B \sin [e + f x]) (c + d \sin [e + f x])^2 dx$$

Optimal (type 3, 429 leaves, 6 steps):

$$\begin{aligned} & - \left( (2 a^3 (15 c^2 + 10 c d + 7 d^2) (11 A d (c^2 - 10 c d + 73 d^2) - B (5 c^3 - 40 c^2 d + 169 c d^2 - 710 d^3)) \right. \\ & \quad \left. \cos [e + f x] \right) / \left( 3465 d^3 f \sqrt{a + a \sin [e + f x]} \right) - \frac{1}{3465 d^2 f} \\ & 4 a^2 (5 c - d) (11 A d (c^2 - 10 c d + 73 d^2) - B (5 c^3 - 40 c^2 d + 169 c d^2 - 710 d^3)) \\ & \quad \cos [e + f x] \sqrt{a + a \sin [e + f x]} - \frac{1}{1155 d f} \\ & 2 a (11 A d (c^2 - 10 c d + 73 d^2) - B (5 c^3 - 40 c^2 d + 169 c d^2 - 710 d^3)) \\ & \quad \cos [e + f x] (a + a \sin [e + f x])^{3/2} + \\ & \left( 2 a^3 (11 A (3 c - 19 d) d - B (15 c^2 - 65 c d + 194 d^2)) \cos [e + f x] (c + d \sin [e + f x])^3 \right) / \\ & \quad \left( 693 d^3 f \sqrt{a + a \sin [e + f x]} \right) + \frac{1}{99 d^2 f} \\ & 2 a^2 (5 B c - 11 A d - 14 B d) \cos [e + f x] \sqrt{a + a \sin [e + f x]} (c + d \sin [e + f x])^3 - \\ & \frac{2 a B \cos [e + f x] (a + a \sin [e + f x])^{3/2} (c + d \sin [e + f x])^3}{11 d f} \end{aligned}$$

Result (type 3, 891 leaves):

$$\frac{1}{55440 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^5} \left( a \left( 1 + \sin [e + f x] \right) \right)^{5/2} \left( -277200 A c^2 \cos \left[ \frac{1}{2} (e + f x) \right] - 207900 B c^2 \cos \left[ \frac{1}{2} (e + f x) \right] - 415800 A c d \cos \left[ \frac{1}{2} (e + f x) \right] - 360360 B c d \cos \left[ \frac{1}{2} (e + f x) \right] - 180180 A d^2 \cos \left[ \frac{1}{2} (e + f x) \right] - 159390 B d^2 \cos \left[ \frac{1}{2} (e + f x) \right] - 46200 A c^2 \cos \left[ \frac{3}{2} (e + f x) \right] - 50820 B c^2 \cos \left[ \frac{3}{2} (e + f x) \right] - 101640 A c d \cos \left[ \frac{3}{2} (e + f x) \right] - 92400 B c d \cos \left[ \frac{3}{2} (e + f x) \right] - 46200 A d^2 \cos \left[ \frac{3}{2} (e + f x) \right] - 43890 B d^2 \cos \left[ \frac{3}{2} (e + f x) \right] + 5544 A c^2 \cos \left[ \frac{5}{2} (e + f x) \right] + 13860 B c^2 \cos \left[ \frac{5}{2} (e + f x) \right] + 27720 A c d \cos \left[ \frac{5}{2} (e + f x) \right] + 33264 B c d \cos \left[ \frac{5}{2} (e + f x) \right] + 16632 A d^2 \cos \left[ \frac{5}{2} (e + f x) \right] + 17325 B d^2 \cos \left[ \frac{5}{2} (e + f x) \right] + 1980 B c^2 \cos \left[ \frac{7}{2} (e + f x) \right] + 3960 A c d \cos \left[ \frac{7}{2} (e + f x) \right] + 9900 B c d \cos \left[ \frac{7}{2} (e + f x) \right] + 4950 A d^2 \cos \left[ \frac{7}{2} (e + f x) \right] + 6435 B d^2 \cos \left[ \frac{7}{2} (e + f x) \right] - 1540 B c d \cos \left[ \frac{9}{2} (e + f x) \right] - 770 A d^2 \cos \left[ \frac{9}{2} (e + f x) \right] - 1925 B d^2 \cos \left[ \frac{9}{2} (e + f x) \right] - 315 B d^2 \cos \left[ \frac{11}{2} (e + f x) \right] + 277200 A c^2 \sin \left[ \frac{1}{2} (e + f x) \right] + 207900 B c^2 \sin \left[ \frac{1}{2} (e + f x) \right] + 415800 A c d \sin \left[ \frac{1}{2} (e + f x) \right] + 360360 B c d \sin \left[ \frac{1}{2} (e + f x) \right] + 180180 A d^2 \sin \left[ \frac{1}{2} (e + f x) \right] + 159390 B d^2 \sin \left[ \frac{1}{2} (e + f x) \right] - 46200 A c^2 \sin \left[ \frac{3}{2} (e + f x) \right] - 50820 B c^2 \sin \left[ \frac{3}{2} (e + f x) \right] - 101640 A c d \sin \left[ \frac{3}{2} (e + f x) \right] - 92400 B c d \sin \left[ \frac{3}{2} (e + f x) \right] - 46200 A d^2 \sin \left[ \frac{3}{2} (e + f x) \right] - 43890 B d^2 \sin \left[ \frac{3}{2} (e + f x) \right] - 5544 A c^2 \sin \left[ \frac{5}{2} (e + f x) \right] - 13860 B c^2 \sin \left[ \frac{5}{2} (e + f x) \right] - 27720 A c d \sin \left[ \frac{5}{2} (e + f x) \right] - 33264 B c d \sin \left[ \frac{5}{2} (e + f x) \right] - 16632 A d^2 \sin \left[ \frac{5}{2} (e + f x) \right] - 17325 B d^2 \sin \left[ \frac{5}{2} (e + f x) \right] + 1980 B c^2 \sin \left[ \frac{7}{2} (e + f x) \right] + 3960 A c d \sin \left[ \frac{7}{2} (e + f x) \right] + 9900 B c d \sin \left[ \frac{7}{2} (e + f x) \right] + 4950 A d^2 \sin \left[ \frac{7}{2} (e + f x) \right] + 6435 B d^2 \sin \left[ \frac{7}{2} (e + f x) \right] + 1540 B c d \sin \left[ \frac{9}{2} (e + f x) \right] + 770 A d^2 \sin \left[ \frac{9}{2} (e + f x) \right] + 1925 B d^2 \sin \left[ \frac{9}{2} (e + f x) \right] - 315 B d^2 \sin \left[ \frac{11}{2} (e + f x) \right] \right)$$

**Problem 302: Result more than twice size of optimal antiderivative.**

$$\int (a + a \sin [e + f x])^{5/2} (A + B \sin [e + f x]) (c + d \sin [e + f x]) dx$$

Optimal (type 3, 212 leaves, 6 steps):



$$\begin{aligned}
 & - \frac{64 a^3 (21 A c + 15 B c + 15 A d + 13 B d) \operatorname{Cos}[e + f x]}{315 f \sqrt{a + a \operatorname{Sin}[e + f x]}} - \\
 & \frac{16 a^2 (21 A c + 15 B c + 15 A d + 13 B d) \operatorname{Cos}[e + f x] \sqrt{a + a \operatorname{Sin}[e + f x]}}{315 f} - \\
 & \frac{2 a (21 A c + 15 B c + 15 A d + 13 B d) \operatorname{Cos}[e + f x] (a + a \operatorname{Sin}[e + f x])^{3/2}}{105 f} - \\
 & \frac{2 (9 B c + 9 A d - 2 B d) \operatorname{Cos}[e + f x] (a + a \operatorname{Sin}[e + f x])^{5/2}}{63 f} - \frac{2 B d \operatorname{Cos}[e + f x] (a + a \operatorname{Sin}[e + f x])^{7/2}}{9 a f}
 \end{aligned}$$

Result (type 3, 673 leaves):

$$\begin{aligned}
& - \left( \left( (20 A c + 15 B c + 15 A d + 13 B d) \cos \left[ \frac{1}{2} (e + f x) \right] (a (1 + \sin [e + f x]))^{5/2} \right) / \right. \\
& \quad \left. \left( 4 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^5 \right) \right) - \\
& \left( (10 A c + 11 B c + 11 A d + 10 B d) \cos \left[ \frac{3}{2} (e + f x) \right] (a (1 + \sin [e + f x]))^{5/2} \right) / \\
& \quad \left( 12 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^5 \right) + \\
& \frac{(2 A c + 5 B c + 5 A d + 6 B d) \cos \left[ \frac{5}{2} (e + f x) \right] (a (1 + \sin [e + f x]))^{5/2}}{20 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^5} + \\
& \frac{(2 B c + 2 A d + 5 B d) \cos \left[ \frac{7}{2} (e + f x) \right] (a (1 + \sin [e + f x]))^{5/2}}{56 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^5} - \\
& \frac{B d \cos \left[ \frac{9}{2} (e + f x) \right] (a (1 + \sin [e + f x]))^{5/2}}{72 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^5} + \\
& \left( (20 A c + 15 B c + 15 A d + 13 B d) \sin \left[ \frac{1}{2} (e + f x) \right] (a (1 + \sin [e + f x]))^{5/2} \right) / \\
& \quad \left( 4 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^5 \right) - \\
& \left( (10 A c + 11 B c + 11 A d + 10 B d) (a (1 + \sin [e + f x]))^{5/2} \sin \left[ \frac{3}{2} (e + f x) \right] \right) / \\
& \quad \left( 12 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^5 \right) - \\
& \frac{(2 A c + 5 B c + 5 A d + 6 B d) (a (1 + \sin [e + f x]))^{5/2} \sin \left[ \frac{5}{2} (e + f x) \right]}{20 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^5} + \\
& \frac{(2 B c + 2 A d + 5 B d) (a (1 + \sin [e + f x]))^{5/2} \sin \left[ \frac{7}{2} (e + f x) \right]}{56 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^5} + \\
& \frac{B d (a (1 + \sin [e + f x]))^{5/2} \sin \left[ \frac{9}{2} (e + f x) \right]}{72 f \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^5}
\end{aligned}$$

**Problem 304: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sin [e + f x])^{5/2} (A + B \sin [e + f x])}{c + d \sin [e + f x]} dx$$

Optimal (type 3, 218 leaves, 5 steps):

$$\frac{2 a^{5/2} (c-d)^2 (B c-A d) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{d} \cos [e+f x]}{\sqrt{c+d} \sqrt{a+a \sin [e+f x]}}\right]}{d^{7/2} \sqrt{c+d} f} +$$

$$\frac{2 a^3 (5 A (3 c-7 d) d-B (15 c^2-35 c d+32 d^2)) \cos [e+f x]}{15 d^3 f \sqrt{a+a \sin [e+f x]}} +$$

$$\frac{2 a^2 (5 B c-5 A d-8 B d) \cos [e+f x] \sqrt{a+a \sin [e+f x]}}{15 d^2 f} - \frac{2 a B \cos [e+f x] (a+a \sin [e+f x])^{3/2}}{5 d f}$$

Result (type 3, 450 leaves):

$$\frac{1}{30 d^{7/2} f \left( \cos \left[ \frac{1}{2} (e+f x) \right] + \sin \left[ \frac{1}{2} (e+f x) \right] \right)^5}$$

$$\left( a (1 + \sin [e+f x]) \right)^{5/2} \left( -30 \sqrt{d} (A d (-2 c+5 d) + B (2 c^2-5 c d+5 d^2)) \cos \left[ \frac{1}{2} (e+f x) \right] - \right.$$

$$5 d^{3/2} (-2 B c+2 A d+5 B d) \cos \left[ \frac{3}{2} (e+f x) \right] + 3 B d^{5/2} \cos \left[ \frac{5}{2} (e+f x) \right] + \frac{1}{\sqrt{c+d}}$$

$$15 (c-d)^2 (B c-A d) \left( e+f x - 2 \operatorname{Log} \left[ \operatorname{Sec} \left[ \frac{1}{4} (e+f x) \right]^2 \right] + 2 \operatorname{Log} \left[ -\operatorname{Sec} \left[ \frac{1}{4} (e+f x) \right]^2 \right] \right)^2$$

$$\left. \left( c+d + \sqrt{d} \sqrt{c+d} \cos \left[ \frac{1}{2} (e+f x) \right] - \sqrt{d} \sqrt{c+d} \sin \left[ \frac{1}{2} (e+f x) \right] \right) \right) -$$

$$\frac{1}{\sqrt{c+d}} 15 (c-d)^2 (B c-A d) \left( e+f x - 2 \operatorname{Log} \left[ \operatorname{Sec} \left[ \frac{1}{4} (e+f x) \right]^2 \right] + 2 \operatorname{Log} \left[ \right. \right.$$

$$\left. \left. (c+d) \operatorname{Sec} \left[ \frac{1}{4} (e+f x) \right]^2 + \sqrt{d} \sqrt{c+d} \left( -1 + 2 \operatorname{Tan} \left[ \frac{1}{4} (e+f x) \right] + \operatorname{Tan} \left[ \frac{1}{4} (e+f x) \right]^2 \right) \right] \right) +$$

$$30 \sqrt{d} (A d (-2 c+5 d) + B (2 c^2-5 c d+5 d^2)) \sin \left[ \frac{1}{2} (e+f x) \right] -$$

$$5 d^{3/2} (-2 B c+2 A d+5 B d) \sin \left[ \frac{3}{2} (e+f x) \right] - 3 B d^{5/2} \sin \left[ \frac{5}{2} (e+f x) \right] \Big)$$

**Problem 307: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(A+B \sin [e+f x]) (c+d \sin [e+f x])^3}{\sqrt{a+a \sin [e+f x]}} dx$$

Optimal (type 3, 284 leaves, 7 steps):

$$\frac{\sqrt{2} (A - B) (c - d)^3 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[e+fx]}{\sqrt{2} \sqrt{a+a \sin[e+fx]}}\right]}{\sqrt{a} f} - \frac{(4 (7 A d (21 c^2 - 12 c d + 7 d^2) + B (36 c^3 - 63 c^2 d + 144 c d^2 - 37 d^3)) \cos[e+fx]) / (105 f \sqrt{a+a \sin[e+fx]}) - \frac{1}{105 a f}}{2 d (7 A (9 c - d) d + B (24 c^2 - 15 c d + 31 d^2)) \cos[e+fx] \sqrt{a+a \sin[e+fx]} - \frac{2 (6 B c + 7 A d - B d) \cos[e+fx] (c+d \sin[e+fx])^2}{35 f \sqrt{a+a \sin[e+fx]}} - \frac{2 B \cos[e+fx] (c+d \sin[e+fx])^3}{7 f \sqrt{a+a \sin[e+fx]}}$$

Result (type 3, 375 leaves):

$$\frac{1}{420 f \sqrt{a (1 + \sin[e+fx])}} \left( \cos\left[\frac{1}{2} (e+fx)\right] + \sin\left[\frac{1}{2} (e+fx)\right] \right) \left( (840 + 840 i) (-1)^{3/4} (A - B) (c - d)^3 \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \left(-1 + \tan\left[\frac{1}{4} (e+fx)\right]\right)\right] - 105 (4 A d (6 c^2 - 3 c d + 2 d^2) + B (8 c^3 - 12 c^2 d + 24 c d^2 - 5 d^3)) \cos\left[\frac{1}{2} (e+fx)\right] - 35 d (2 A (6 c - d) d + B (12 c^2 - 6 c d + 5 d^2)) \cos\left[\frac{3}{2} (e+fx)\right] + 21 d^2 (6 B c + 2 A d - B d) \cos\left[\frac{5}{2} (e+fx)\right] + 15 B d^3 \cos\left[\frac{7}{2} (e+fx)\right] + 105 (4 A d (6 c^2 - 3 c d + 2 d^2) + B (8 c^3 - 12 c^2 d + 24 c d^2 - 5 d^3)) \sin\left[\frac{1}{2} (e+fx)\right] - 35 d (2 A (6 c - d) d + B (12 c^2 - 6 c d + 5 d^2)) \sin\left[\frac{3}{2} (e+fx)\right] + 21 d^2 (-2 A d + B (-6 c + d)) \sin\left[\frac{5}{2} (e+fx)\right] + 15 B d^3 \sin\left[\frac{7}{2} (e+fx)\right] \right)$$

**Problem 308: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(A + B \sin[e+fx]) (c + d \sin[e+fx])^2}{\sqrt{a+a \sin[e+fx]}} dx$$

Optimal (type 3, 200 leaves, 6 steps):

$$\frac{\sqrt{2} (A - B) (c - d)^2 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[e+fx]}{\sqrt{2} \sqrt{a+a \sin[e+fx]}}\right]}{\sqrt{a} f} - \frac{4 (5 A (3 c - d) d + B (6 c^2 - 7 c d + 7 d^2)) \cos[e+fx]}{15 f \sqrt{a+a \sin[e+fx]}} - \frac{2 d (4 B c + 5 A d - B d) \cos[e+fx] \sqrt{a+a \sin[e+fx]}}{15 a f} - \frac{2 B \cos[e+fx] (c+d \sin[e+fx])^2}{5 f \sqrt{a+a \sin[e+fx]}}$$

Result (type 3, 246 leaves):

$$\frac{1}{30 f \sqrt{a (1 + \sin[e + f x])}} \left( \cos\left[\frac{1}{2} (e + f x)\right] + \sin\left[\frac{1}{2} (e + f x)\right] \right) \left( (60 + 60 i) (-1)^{3/4} (A - B) (c - d)^2 \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \left(-1 + \tan\left[\frac{1}{4} (e + f x)\right]\right)\right] \right) - 30 (A (4 c - d) d + 2 B (c^2 - c d + d^2)) \cos\left[\frac{1}{2} (e + f x)\right] + 5 d (-2 A d + B (-4 c + d)) \cos\left[\frac{3}{2} (e + f x)\right] + 3 B d^2 \cos\left[\frac{5}{2} (e + f x)\right] + 30 (A (4 c - d) d + 2 B (c^2 - c d + d^2)) \sin\left[\frac{1}{2} (e + f x)\right] + 5 d (-2 A d + B (-4 c + d)) \sin\left[\frac{3}{2} (e + f x)\right] - 3 B d^2 \sin\left[\frac{5}{2} (e + f x)\right] \right)$$

**Problem 309: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(A + B \sin[e + f x]) (c + d \sin[e + f x])}{\sqrt{a + a \sin[e + f x]}} dx$$

Optimal (type 3, 130 leaves, 5 steps):

$$\frac{\sqrt{2} (A - B) (c - d) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[e + f x]}{\sqrt{2} \sqrt{a + a \sin[e + f x]}}\right]}{\sqrt{a} f} - \frac{2 (3 B c + 3 A d - 2 B d) \cos[e + f x]}{3 f \sqrt{a + a \sin[e + f x]}} - \frac{2 B d \cos[e + f x] \sqrt{a + a \sin[e + f x]}}{3 a f}$$

Result (type 3, 135 leaves):

$$\frac{\left( \left( \cos\left[\frac{1}{2} (e + f x)\right] + \sin\left[\frac{1}{2} (e + f x)\right] \right) \left( (-6 - 6 i) (-1)^{3/4} (A - B) (c - d) \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \left(-1 + \tan\left[\frac{1}{4} (e + f x)\right]\right)\right] \right) + 2 \left( \cos\left[\frac{1}{2} (e + f x)\right] - \sin\left[\frac{1}{2} (e + f x)\right] \right) (3 B c + 3 A d - B d + B d \sin[e + f x]) \right)}{\left( 3 f \sqrt{a (1 + \sin[e + f x])} \right)}$$

**Problem 310: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A + B \sin[e + f x]}{\sqrt{a + a \sin[e + f x]}} dx$$

Optimal (type 3, 79 leaves, 3 steps):

$$\frac{\sqrt{2} (A - B) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[e + f x]}{\sqrt{2} \sqrt{a + a \sin[e + f x]}}\right]}{\sqrt{a} f} - \frac{2 B \cos[e + f x]}{f \sqrt{a + a \sin[e + f x]}}$$

Result (type 3, 106 leaves):

$$\left( 2 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) \left( (1 + i) (-1)^{3/4} (A - B) \operatorname{ArcTanh} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \left( -1 + \tan \left[ \frac{1}{4} (e + f x) \right] \right) \right] + B \left( -\cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right) \right) / \left( f \sqrt{a (1 + \sin [e + f x])} \right)$$

**Problem 311: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A + B \sin [e + f x]}{\sqrt{a + a \sin [e + f x]} (c + d \sin [e + f x])} dx$$

Optimal (type 3, 136 leaves, 5 steps):

$$\frac{\sqrt{2} (A - B) \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \cos [e + f x]}{\sqrt{2} \sqrt{a + a \sin [e + f x]}} \right]}{\sqrt{a} (c - d) f} - \frac{2 (B c - A d) \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \sqrt{d} \cos [e + f x]}{\sqrt{c + d} \sqrt{a + a \sin [e + f x]}} \right]}{\sqrt{a} (c - d) \sqrt{d} \sqrt{c + d} f}$$

Result (type 3, 238 leaves):

$$\frac{1}{(c - d) \sqrt{d} \sqrt{c + d} f \sqrt{a (1 + \sin [e + f x])}} \left( (-1)^{3/4} \left( (2 + 2i) (A - B) \sqrt{d} \sqrt{c + d} \operatorname{ArcTanh} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \left( -1 + \tan \left[ \frac{1}{4} (e + f x) \right] \right) \right] + (-1)^{1/4} (B c - A d) \left( \log \left[ \sec \left[ \frac{1}{4} (e + f x) \right] \right]^2 \left( \sqrt{c + d} + \sqrt{d} \cos \left[ \frac{1}{2} (e + f x) \right] - \sqrt{d} \sin \left[ \frac{1}{2} (e + f x) \right] \right) - \log \left[ \sec \left[ \frac{1}{4} (e + f x) \right] \right]^2 \left( \sqrt{c + d} - \sqrt{d} \cos \left[ \frac{1}{2} (e + f x) \right] + \sqrt{d} \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right) \right) \right) \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)$$

**Problem 312: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A + B \sin [e + f x]}{\sqrt{a + a \sin [e + f x]} (c + d \sin [e + f x])^2} dx$$

Optimal (type 3, 207 leaves, 6 steps):

$$\begin{aligned}
 & - \frac{\sqrt{2} (A - B) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[e+fx]}{\sqrt{2} \sqrt{a+a \sin[e+fx]}}\right]}{\sqrt{a} (c-d)^2 f} + \\
 & \frac{(A d (3 c+d) - B (c^2 + c d + 2 d^2)) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{d} \cos[e+fx]}{\sqrt{c+d} \sqrt{a+a \sin[e+fx]}}\right]}{\sqrt{a} (c-d)^2 \sqrt{d} (c+d)^{3/2} f} - \\
 & \frac{(B c - A d) \cos[e+fx]}{(c^2 - d^2) f \sqrt{a+a \sin[e+fx]} (c+d \sin[e+fx])}
 \end{aligned}$$

Result (type 3, 374 leaves):

$$\begin{aligned}
 & \frac{1}{4 (c-d)^2 f \sqrt{a} (1 + \sin[e+fx])} \left( \cos\left[\frac{1}{2} (e+fx)\right] + \sin\left[\frac{1}{2} (e+fx)\right] \right) \\
 & \left( (8+8i) (-1)^{3/4} (A-B) \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \left(-1 + \tan\left[\frac{1}{4} (e+fx)\right]\right)\right] - \right. \\
 & \frac{1}{\sqrt{d} (c+d)^{3/2}} (-A d (3 c+d) + B (c^2 + c d + 2 d^2)) \left( e+fx - 2 \operatorname{Log}\left[\operatorname{Sec}\left[\frac{1}{4} (e+fx)\right]\right]^2 \right) + \\
 & \left. 2 \operatorname{Log}\left[\operatorname{Sec}\left[\frac{1}{4} (e+fx)\right]\right]^2 \left( \sqrt{c+d} + \sqrt{d} \cos\left[\frac{1}{2} (e+fx)\right] - \sqrt{d} \sin\left[\frac{1}{2} (e+fx)\right] \right) \right) + \\
 & \frac{1}{\sqrt{d} (c+d)^{3/2}} (-A d (3 c+d) + B (c^2 + c d + 2 d^2)) \left( e+fx - 2 \operatorname{Log}\left[\operatorname{Sec}\left[\frac{1}{4} (e+fx)\right]\right]^2 \right) + \\
 & \left. 2 \operatorname{Log}\left[\operatorname{Sec}\left[\frac{1}{4} (e+fx)\right]\right]^2 \left( \sqrt{c+d} - \sqrt{d} \cos\left[\frac{1}{2} (e+fx)\right] + \sqrt{d} \sin\left[\frac{1}{2} (e+fx)\right] \right) \right) - \\
 & \frac{4 (c-d) (B c - A d) \left( \cos\left[\frac{1}{2} (e+fx)\right] - \sin\left[\frac{1}{2} (e+fx)\right] \right)}{(c+d) (c+d \sin[e+fx])}
 \end{aligned}$$

**Problem 313: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sin[e+fx]}{\sqrt{a+a \sin[e+fx]} (c+d \sin[e+fx])^3} dx$$

Optimal (type 3, 309 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{\sqrt{2} (A - B) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[e+fx]}{\sqrt{2} \sqrt{a+a \sin[e+fx]}}\right]}{\sqrt{a} (c-d)^3 f} + \\
 & \left( (A d (15 c^2 + 10 c d + 7 d^2) - B (3 c^3 + 6 c^2 d + 19 c d^2 + 4 d^3)) \right. \\
 & \quad \left. \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{d} \cos[e+fx]}{\sqrt{c+d} \sqrt{a+a \sin[e+fx]}}\right] \right) / \left( 4 \sqrt{a} (c-d)^3 \sqrt{d} (c+d)^{5/2} f \right) - \\
 & \frac{(B c - A d) \cos[e+fx]}{2 (c^2 - d^2) f \sqrt{a+a \sin[e+fx]} (c+d \sin[e+fx])^2} + \\
 & \frac{(A d (7 c + d) - B (3 c^2 + c d + 4 d^2)) \cos[e+fx]}{4 (c^2 - d^2)^2 f \sqrt{a+a \sin[e+fx]} (c+d \sin[e+fx])}
 \end{aligned}$$

Result(type 3, 847 leaves):



$$\begin{aligned}
 & \left( (2+2i) (A-B) \operatorname{ArcTanh} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \operatorname{Sec} \left[ \frac{1}{4} (e+fx) \right] \left( \cos \left[ \frac{1}{4} (e+fx) \right] - \sin \left[ \frac{1}{4} (e+fx) \right] \right) \right] \right. \\
 & \quad \left. \left( \cos \left[ \frac{1}{2} (e+fx) \right] + \sin \left[ \frac{1}{2} (e+fx) \right] \right) \right) / \\
 & \quad \left( (-1)^{1/4} c^3 - 3 (-1)^{1/4} c^2 d + 3 (-1)^{1/4} c d^2 - (-1)^{1/4} d^3 \right) f \sqrt{a (1 + \sin[e+fx])} - \\
 & \quad \left( -A d (15 c^2 + 10 c d + 7 d^2) + B (3 c^3 + 6 c^2 d + 19 c d^2 + 4 d^3) \right) \left( e+fx - 2 \operatorname{Log} \left[ \operatorname{Sec} \left[ \frac{1}{4} (e+fx) \right] \right]^2 \right) + \\
 & \quad 2 \operatorname{Log} \left[ \operatorname{Sec} \left[ \frac{1}{4} (e+fx) \right] \right]^2 \left( \sqrt{c+d} + \sqrt{d} \cos \left[ \frac{1}{2} (e+fx) \right] - \sqrt{d} \sin \left[ \frac{1}{2} (e+fx) \right] \right) \left. \right) \\
 & \quad \left( \cos \left[ \frac{1}{2} (e+fx) \right] + \sin \left[ \frac{1}{2} (e+fx) \right] \right) \right) / \left( 16 (c-d)^3 \sqrt{d} (c+d)^{5/2} f \sqrt{a (1 + \sin[e+fx])} \right) + \\
 & \quad \left( -A d (15 c^2 + 10 c d + 7 d^2) + B (3 c^3 + 6 c^2 d + 19 c d^2 + 4 d^3) \right) \left( e+fx - 2 \operatorname{Log} \left[ \operatorname{Sec} \left[ \frac{1}{4} (e+fx) \right] \right]^2 \right) + \\
 & \quad 2 \operatorname{Log} \left[ \operatorname{Sec} \left[ \frac{1}{4} (e+fx) \right] \right]^2 \left( \sqrt{c+d} - \sqrt{d} \cos \left[ \frac{1}{2} (e+fx) \right] + \sqrt{d} \sin \left[ \frac{1}{2} (e+fx) \right] \right) \left. \right) \\
 & \quad \left( \cos \left[ \frac{1}{2} (e+fx) \right] + \sin \left[ \frac{1}{2} (e+fx) \right] \right) \right) / \left( 16 (c-d)^3 \sqrt{d} (c+d)^{5/2} f \sqrt{a (1 + \sin[e+fx])} \right) + \\
 & \quad \left( \cos \left[ \frac{1}{2} (e+fx) \right] + \sin \left[ \frac{1}{2} (e+fx) \right] \right) \\
 & \quad \left( -B c \cos \left[ \frac{1}{2} (e+fx) \right] + A d \cos \left[ \frac{1}{2} (e+fx) \right] + B c \sin \left[ \frac{1}{2} (e+fx) \right] - A d \sin \left[ \frac{1}{2} (e+fx) \right] \right) \right) / \\
 & \quad \left( 2 (c-d) (c+d) f \sqrt{a (1 + \sin[e+fx])} (c+d \sin[e+fx])^2 \right) + \\
 & \quad \left( \cos \left[ \frac{1}{2} (e+fx) \right] + \sin \left[ \frac{1}{2} (e+fx) \right] \right) \\
 & \quad \left( -3 B c^2 \cos \left[ \frac{1}{2} (e+fx) \right] + 7 A c d \cos \left[ \frac{1}{2} (e+fx) \right] - B c d \cos \left[ \frac{1}{2} (e+fx) \right] + \right. \\
 & \quad A d^2 \cos \left[ \frac{1}{2} (e+fx) \right] - 4 B d^2 \cos \left[ \frac{1}{2} (e+fx) \right] + 3 B c^2 \sin \left[ \frac{1}{2} (e+fx) \right] - 7 A c d \\
 & \quad \left. \sin \left[ \frac{1}{2} (e+fx) \right] + B c d \sin \left[ \frac{1}{2} (e+fx) \right] - A d^2 \sin \left[ \frac{1}{2} (e+fx) \right] + 4 B d^2 \sin \left[ \frac{1}{2} (e+fx) \right] \right) \right) / \\
 & \quad \left( 4 (c-d)^2 (c+d)^2 f \sqrt{a (1 + \sin[e+fx])} (c+d \sin[e+fx]) \right)
 \end{aligned}$$

**Problem 314: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(A+B \sin[e+fx]) (c+d \sin[e+fx])^3}{(a+a \sin[e+fx])^{3/2}} dx$$

Optimal (type 3, 283 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{(c-d)^2 (3B(c-5d) + A(c+11d)) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[e+fx]}{\sqrt{2} \sqrt{a+a \sin[e+fx]}}\right]}{2\sqrt{2} a^{3/2} f} + \\
 & (d(15Ac^2 - 99Bc^2 - 120Acd + 168Bcd + 65Ad^2 - 93Bd^2) \cos[e+fx]) / \\
 & \left(15af \sqrt{a+a \sin[e+fx]}\right) + \frac{d^2(15Ac - 51Bc - 35Ad + 39Bd) \cos[e+fx] \sqrt{a+a \sin[e+fx]}}{30a^2 f} + \\
 & \frac{(5A-9B)d \cos[e+fx] (c+d \sin[e+fx])^2}{10af \sqrt{a+a \sin[e+fx]}} - \frac{(A-B) \cos[e+fx] (c+d \sin[e+fx])^3}{2f (a+a \sin[e+fx])^{3/2}}
 \end{aligned}$$

Result (type 3, 684 leaves):

$$\begin{aligned}
 & \frac{1}{60f (a(1+\sin[e+fx]))^{3/2}} \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right) \\
 & \left( -30Ac^3 \cos\left[\frac{1}{2}(e+fx)\right] + 30Bc^3 \cos\left[\frac{1}{2}(e+fx)\right] + 90Ac^2d \cos\left[\frac{1}{2}(e+fx)\right] - \right. \\
 & 270Bc^2d \cos\left[\frac{1}{2}(e+fx)\right] - 270Acd^2 \cos\left[\frac{1}{2}(e+fx)\right] + 330Bcd^2 \cos\left[\frac{1}{2}(e+fx)\right] + \\
 & 110Ad^3 \cos\left[\frac{1}{2}(e+fx)\right] - 165Bd^3 \cos\left[\frac{1}{2}(e+fx)\right] - 180Bc^2d \cos\left[\frac{3}{2}(e+fx)\right] - \\
 & 180Acd^2 \cos\left[\frac{3}{2}(e+fx)\right] + 210Bcd^2 \cos\left[\frac{3}{2}(e+fx)\right] + 70Ad^3 \cos\left[\frac{3}{2}(e+fx)\right] - \\
 & 123Bd^3 \cos\left[\frac{3}{2}(e+fx)\right] + 30Bcd^2 \cos\left[\frac{5}{2}(e+fx)\right] + 10Ad^3 \cos\left[\frac{5}{2}(e+fx)\right] - \\
 & 9Bd^3 \cos\left[\frac{5}{2}(e+fx)\right] + 3Bd^3 \cos\left[\frac{7}{2}(e+fx)\right] + 30Ac^3 \sin\left[\frac{1}{2}(e+fx)\right] - \\
 & 30Bc^3 \sin\left[\frac{1}{2}(e+fx)\right] - 90Ac^2d \sin\left[\frac{1}{2}(e+fx)\right] + 270Bc^2d \sin\left[\frac{1}{2}(e+fx)\right] + \\
 & 270Acd^2 \sin\left[\frac{1}{2}(e+fx)\right] - 330Bcd^2 \sin\left[\frac{1}{2}(e+fx)\right] - 110Ad^3 \sin\left[\frac{1}{2}(e+fx)\right] + \\
 & 165Bd^3 \sin\left[\frac{1}{2}(e+fx)\right] + (30+30i)(-1)^{3/4} (c-d)^2 (3B(c-5d) + A(c+11d)) \\
 & \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right)(-1)^{3/4} \left(-1 + \tan\left[\frac{1}{4}(e+fx)\right]\right)\right] \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^2 - \\
 & 180Bc^2d \sin\left[\frac{3}{2}(e+fx)\right] - 180Acd^2 \sin\left[\frac{3}{2}(e+fx)\right] + 210Bcd^2 \sin\left[\frac{3}{2}(e+fx)\right] + \\
 & 70Ad^3 \sin\left[\frac{3}{2}(e+fx)\right] - 123Bd^3 \sin\left[\frac{3}{2}(e+fx)\right] - 30Bcd^2 \sin\left[\frac{5}{2}(e+fx)\right] - \\
 & \left. 10Ad^3 \sin\left[\frac{5}{2}(e+fx)\right] + 9Bd^3 \sin\left[\frac{5}{2}(e+fx)\right] + 3Bd^3 \sin\left[\frac{7}{2}(e+fx)\right] \right)
 \end{aligned}$$

**Problem 315: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(A+B \sin[e+fx]) (c+d \sin[e+fx])^2}{(a+a \sin[e+fx])^{3/2}} dx$$

Optimal (type 3, 203 leaves, 6 steps):

$$\frac{(c-d)(Ac+3Bc+7Ad-11Bd) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[e+fx]}{\sqrt{2} \sqrt{a+a \sin[e+fx]}}\right]}{2\sqrt{2} a^{3/2} f} + \frac{d(3Ac-15Bc-9Ad+13Bd) \cos[e+fx]}{3af \sqrt{a+a \sin[e+fx]}} + \frac{(3A-7B)d^2 \cos[e+fx] \sqrt{a+a \sin[e+fx]}}{6a^2 f} - \frac{(A-B) \cos[e+fx] (c+d \sin[e+fx])^2}{2f (a+a \sin[e+fx])^{3/2}}$$

Result (type 3, 357 leaves):

$$\frac{1}{6f (a(1+\sin[e+fx]))^{3/2}} \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right) \left( 6(A-B)(c-d)^2 \sin\left[\frac{1}{2}(e+fx)\right] - 3(A-B)(c-d)^2 \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right) \right) + (3+3i)(-1)^{3/4}(c-d)(Ac+3Bc+7Ad-11Bd) \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right)(-1)^{3/4} \left(-1 + \tan\left[\frac{1}{4}(e+fx)\right]\right)\right] \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^2 + 6d(-4Bc-2Ad+3Bd) \cos\left[\frac{1}{2}(e+fx)\right] \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^2 - 2Bd^2 \cos\left[\frac{3}{2}(e+fx)\right] \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^2 - 6d(-4Bc-2Ad+3Bd) \sin\left[\frac{1}{2}(e+fx)\right] \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^2 - 2Bd^2 \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^2 \sin\left[\frac{3}{2}(e+fx)\right]$$

**Problem 316: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(A+B \sin[e+fx])(c+d \sin[e+fx])}{(a+a \sin[e+fx])^{3/2}} dx$$

Optimal (type 3, 133 leaves, 5 steps):

$$\frac{(Ac+3Bc+3Ad-7Bd) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[e+fx]}{\sqrt{2} \sqrt{a+a \sin[e+fx]}}\right]}{2\sqrt{2} a^{3/2} f} - \frac{(A-B)(c-d) \cos[e+fx]}{2f (a+a \sin[e+fx])^{3/2}} - \frac{2Bd \cos[e+fx]}{af \sqrt{a+a \sin[e+fx]}}$$

Result (type 3, 246 leaves):

$$\frac{1}{2 f (a (1 + \sin [e + f x]))^{3/2}} \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) \left( 2 (A - B) (c - d) \sin \left[ \frac{1}{2} (e + f x) \right] - (A - B) (c - d) \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) + (1 + i) (-1)^{3/4} (A c + 3 B c + 3 A d - 7 B d) \operatorname{ArcTanh} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \left( -1 + \tan \left[ \frac{1}{4} (e + f x) \right] \right) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 - 4 B d \cos \left[ \frac{1}{2} (e + f x) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 + 4 B d \sin \left[ \frac{1}{2} (e + f x) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 \right)$$

**Problem 317: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A + B \sin [e + f x]}{(a + a \sin [e + f x])^{3/2}} dx$$

Optimal (type 3, 87 leaves, 3 steps):

$$-\frac{(A + 3 B) \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \cos [e + f x]}{\sqrt{2} \sqrt{a + a \sin [e + f x]}} \right]}{2 \sqrt{2} a^{3/2} f} - \frac{(A - B) \cos [e + f x]}{2 f (a + a \sin [e + f x])^{3/2}}$$

Result (type 3, 150 leaves):

$$\left( \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) \left( 2 (A - B) \sin \left[ \frac{1}{2} (e + f x) \right] + (-A + B) \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) + (1 + i) (-1)^{3/4} (A + 3 B) \operatorname{ArcTanh} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \left( -1 + \tan \left[ \frac{1}{4} (e + f x) \right] \right) \right] \right) \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 \right) / \left( 2 f (a (1 + \sin [e + f x]))^{3/2} \right)$$

**Problem 318: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sin [e + f x]}{(a + a \sin [e + f x])^{3/2} (c + d \sin [e + f x])} dx$$

Optimal (type 3, 187 leaves, 6 steps):

$$\begin{aligned}
 & - \frac{(A(c-5d) + B(3c+d)) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[e+fx]}{\sqrt{2} \sqrt{a+a \sin[e+fx]}}\right]}{2\sqrt{2} a^{3/2} (c-d)^2 f} + \\
 & \frac{2\sqrt{d} (Bc - Ad) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{d} \cos[e+fx]}{\sqrt{c+d} \sqrt{a+a \sin[e+fx]}}\right]}{a^{3/2} (c-d)^2 \sqrt{c+d} f} - \frac{(A-B) \cos[e+fx]}{2(c-d) f (a+a \sin[e+fx])^{3/2}}
 \end{aligned}$$

Result (type 3, 419 leaves):

$$\begin{aligned}
 & \frac{1}{2(c-d)^2 f (a(1+\sin[e+fx]))^{3/2}} \\
 & \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right) \left( 2(A-B)(c-d) \sin\left[\frac{1}{2}(e+fx)\right] + (-A+B)(c-d) \right. \\
 & \quad \left. \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right) + (1+i)(-1)^{3/4} (A(c-5d) + B(3c+d)) \right. \\
 & \quad \left. \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right)(-1)^{3/4} \left(-1 + \tan\left[\frac{1}{4}(e+fx)\right]\right)\right] \right) \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^2 + \\
 & \quad \frac{1}{\sqrt{c+d}} \sqrt{d} (Bc - Ad) \left( e+fx - 2 \operatorname{Log}\left[\operatorname{Sec}\left[\frac{1}{4}(e+fx)\right]\right]^2 \right) + \\
 & \quad 2 \operatorname{Log}\left[\operatorname{Sec}\left[\frac{1}{4}(e+fx)\right]\right]^2 \left( \sqrt{c+d} + \sqrt{d} \cos\left[\frac{1}{2}(e+fx)\right] - \sqrt{d} \sin\left[\frac{1}{2}(e+fx)\right] \right) \left. \right) \\
 & \quad \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^2 + \frac{1}{\sqrt{c+d}} \\
 & \quad \sqrt{d} (-Bc + Ad) \left( e+fx - 2 \operatorname{Log}\left[\operatorname{Sec}\left[\frac{1}{4}(e+fx)\right]\right]^2 \right) + \\
 & \quad 2 \operatorname{Log}\left[\operatorname{Sec}\left[\frac{1}{4}(e+fx)\right]\right]^2 \left( \sqrt{c+d} - \sqrt{d} \cos\left[\frac{1}{2}(e+fx)\right] + \sqrt{d} \sin\left[\frac{1}{2}(e+fx)\right] \right) \left. \right) \\
 & \quad \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^2 \left. \right)
 \end{aligned}$$

**Problem 319: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sin[e+fx]}{(a + a \sin[e+fx])^{3/2} (c + d \sin[e+fx])^2} dx$$

Optimal (type 3, 292 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{(A c + 3 B c - 9 A d + 5 B d) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [e+f x]}{\sqrt{2} \sqrt{a+a \sin [e+f x]}}\right]}{2 \sqrt{2} a^{3 / 2}(c-d)^3 f} \\
 & \left(\sqrt{d}(A d(5 c+3 d)-B(3 c^2+3 c d+2 d^2)) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{d} \cos [e+f x]}{\sqrt{c+d} \sqrt{a+a \sin [e+f x]}}\right]\right) / \\
 & \left(a^{3 / 2}(c-d)^3(c+d)^{3 / 2} f\right)-\frac{(A-B) \cos [e+f x]}{2(c-d) f(a+a \sin [e+f x])^{3 / 2}(c+d \sin [e+f x])}+ \\
 & \frac{d(B(3 c+d)-A(c+3 d)) \cos [e+f x]}{2 a(c-d)^2(c+d) f \sqrt{a+a \sin [e+f x]}(c+d \sin [e+f x])}
 \end{aligned}$$

Result (type 3, 745 leaves):

$$\begin{aligned}
 & \frac{(-A+B)\left(\cos \left[\frac{1}{2}(e+f x)\right]+\sin \left[\frac{1}{2}(e+f x)\right]\right)^2}{2(c-d)^2 f(a(1+\sin [e+f x]))^{3 / 2}}+ \\
 & \left((1+i)(A c+3 B c-9 A d+5 B d) \operatorname{ArcTanh}\left[\left(\frac{1}{2}+\frac{i}{2}\right)(-1)^{3 / 4} \sec \left[\frac{1}{4}(e+f x)\right]\right.\right. \\
 & \quad \left.\left.\left(\cos \left[\frac{1}{4}(e+f x)\right]-\sin \left[\frac{1}{4}(e+f x)\right]\right)\right]\right)\left(\cos \left[\frac{1}{2}(e+f x)\right]+\sin \left[\frac{1}{2}(e+f x)\right]\right)^3) / \\
 & \left(\left(2(-1)^{1 / 4} c^3-6(-1)^{1 / 4} c^2 d+6(-1)^{1 / 4} c d^2-2(-1)^{1 / 4} d^3\right) f(a(1+\sin [e+f x]))^{3 / 2}\right)+ \\
 & \left(\sqrt{d}(-A d(5 c+3 d)+B(3 c^2+3 c d+2 d^2))\left(e+f x-2 \log \left[\sec \left[\frac{1}{4}(e+f x)\right]^2\right]+2 \log \left[\sec \left[\frac{1}{4}(e+f x)\right]^2\right.\right.\right. \\
 & \quad \left.\left.\left(\sqrt{c+d}+\sqrt{d} \cos \left[\frac{1}{2}(e+f x)\right]-\sqrt{d} \sin \left[\frac{1}{2}(e+f x)\right]\right)\right]\right)\right) \\
 & \left(\cos \left[\frac{1}{2}(e+f x)\right]+\sin \left[\frac{1}{2}(e+f x)\right]\right)^3) / \left(4(c-d)^3(c+d)^{3 / 2} f(a(1+\sin [e+f x]))^{3 / 2}\right)+ \\
 & \left(\sqrt{d}(A d(5 c+3 d)-B(3 c^2+3 c d+2 d^2))\left(e+f x-2 \log \left[\sec \left[\frac{1}{4}(e+f x)\right]^2\right]+2 \log \left[\sec \left[\frac{1}{4}(e+f x)\right]^2\right.\right.\right. \\
 & \quad \left.\left.\left(\sqrt{c+d}-\sqrt{d} \cos \left[\frac{1}{2}(e+f x)\right]+\sqrt{d} \sin \left[\frac{1}{2}(e+f x)\right]\right)\right]\right)\right) \\
 & \left(\cos \left[\frac{1}{2}(e+f x)\right]+\sin \left[\frac{1}{2}(e+f x)\right]\right)^3) / \left(4(c-d)^3(c+d)^{3 / 2} f(a(1+\sin [e+f x]))^{3 / 2}\right)+ \\
 & \left(\left(\cos \left[\frac{1}{2}(e+f x)\right]+\sin \left[\frac{1}{2}(e+f x)\right]\right)\left(A \sin \left[\frac{1}{2}(e+f x)\right]-B \sin \left[\frac{1}{2}(e+f x)\right]\right)\right) / \\
 & \left((c-d)^2 f(a(1+\sin [e+f x]))^{3 / 2}\right)+ \\
 & \left(\left(\cos \left[\frac{1}{2}(e+f x)\right]+\sin \left[\frac{1}{2}(e+f x)\right]\right)^3\left(B c d \cos \left[\frac{1}{2}(e+f x)\right]-A d^2 \cos \left[\frac{1}{2}(e+f x)\right]-B c d \sin \left[\frac{1}{2}(e+f x)\right]+A d^2 \sin \left[\frac{1}{2}(e+f x)\right]\right)\right) / \\
 & \left((c-d)^2(c+d) f(a(1+\sin [e+f x]))^{3 / 2}(c+d \sin [e+f x])\right)
 \end{aligned}$$

**Problem 320: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sin[e + f x]}{(a + a \sin[e + f x])^{3/2} (c + d \sin[e + f x])^3} dx$$

Optimal (type 3, 402 leaves, 8 steps):

$$\frac{(A(c - 13d) + 3B(c + 3d)) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[e + f x]}{\sqrt{2} \sqrt{a + a \sin[e + f x]}}\right]}{2\sqrt{2} a^{3/2} (c - d)^4 f} - \frac{\left(\sqrt{d} (Ad(35c^2 + 42cd + 19d^2) - 3B(5c^3 + 10c^2d + 13cd^2 + 4d^3)) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{d} \cos[e + f x]}{\sqrt{c+d} \sqrt{a + a \sin[e + f x]}}\right]\right) / (4a^{3/2} (c - d)^4 (c + d)^{5/2} f) - \frac{(A - B) \cos[e + f x]}{2(c - d) f (a + a \sin[e + f x])^{3/2} (c + d \sin[e + f x])^2} + \frac{d(B(2c + d) - A(c + 2d)) \cos[e + f x]}{2a(c - d)^2 (c + d) f \sqrt{a + a \sin[e + f x]} (c + d \sin[e + f x])^2} + \frac{d(3B(3c^2 + 3cd + 2d^2) - A(2c^2 + 15cd + 7d^2)) \cos[e + f x]}{4a(c - d)^3 (c + d)^2 f \sqrt{a + a \sin[e + f x]} (c + d \sin[e + f x])}$$

Result (type 3, 1395 leaves):

$$\left( (1 + i) (Ac + 3Bc - 13Ad + 9Bd) \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \operatorname{Sec}\left[\frac{1}{4}(e + fx)\right] \left(\cos\left[\frac{1}{4}(e + fx)\right] - \sin\left[\frac{1}{4}(e + fx)\right]\right)\right] \right) \left(\cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right]\right)^3 / \left(\left(2(-1)^{1/4} c^4 - 8(-1)^{1/4} c^3 d + 12(-1)^{1/4} c^2 d^2 - 8(-1)^{1/4} c d^3 + 2(-1)^{1/4} d^4\right) f (a(1 + \sin[e + fx]))^{3/2}\right) + \frac{\left(\sqrt{d} (-Ad(35c^2 + 42cd + 19d^2) + 3B(5c^3 + 10c^2d + 13cd^2 + 4d^3)) (e + fx - 2 \operatorname{Log}\left[\operatorname{Sec}\left[\frac{1}{4}(e + fx)\right]\right]^2\right) + 2 \operatorname{Log}\left[\operatorname{Sec}\left[\frac{1}{4}(e + fx)\right]\right]^2 \left(\sqrt{c+d} + \sqrt{d} \cos\left[\frac{1}{2}(e + fx)\right] - \sqrt{d} \sin\left[\frac{1}{2}(e + fx)\right]\right)\right) \left(\cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right]\right)^3 / \left(16(c - d)^4 (c + d)^{5/2} f (a(1 + \sin[e + fx]))^{3/2}\right) - \frac{\left(\sqrt{d} (-Ad(35c^2 + 42cd + 19d^2) + 3B(5c^3 + 10c^2d + 13cd^2 + 4d^3)) (e + fx - 2 \operatorname{Log}\left[\operatorname{Sec}\left[\frac{1}{4}(e + fx)\right]\right]^2\right) +$$

$$\frac{2 \operatorname{Log}\left[\operatorname{Sec}\left[\frac{1}{4}(e+fx)\right]^2\left(\sqrt{c+d}-\sqrt{d} \cos\left[\frac{1}{2}(e+fx)\right]+\sqrt{d} \sin\left[\frac{1}{2}(e+fx)\right]\right)\right]}{\left(\cos\left[\frac{1}{2}(e+fx)\right]+\sin\left[\frac{1}{2}(e+fx)\right]\right)^3} \Big/ \left(16(c-d)^4(c+d)^{5/2} f(a(1+\sin[e+fx]))^{3/2}\right) +$$


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$$\frac{16(c-d)^3(c+d)^2 f(a(1+\sin[e+fx]))^{3/2}(c+d \sin[e+fx])^2}{\left(\cos\left[\frac{1}{2}(e+fx)\right]+\sin\left[\frac{1}{2}(e+fx)\right]\right)} \left(-8 A c^4 \cos\left[\frac{1}{2}(e+fx)\right]+8 B c^4 \cos\left[\frac{1}{2}(e+fx)\right]-8 A c^3 d \cos\left[\frac{1}{2}(e+fx)\right]+26 B c^3 d \cos\left[\frac{1}{2}(e+fx)\right]-22 A c^2 d^2 \cos\left[\frac{1}{2}(e+fx)\right]+6 B c^2 d^2 \cos\left[\frac{1}{2}(e+fx)\right]-10 A c d^3 \cos\left[\frac{1}{2}(e+fx)\right]+4 B c d^3 \cos\left[\frac{1}{2}(e+fx)\right]+4 B d^4 \cos\left[\frac{1}{2}(e+fx)\right]-8 A c^3 d \cos\left[\frac{3}{2}(e+fx)\right]+26 B c^3 d \cos\left[\frac{3}{2}(e+fx)\right]-40 A c^2 d^2 \cos\left[\frac{3}{2}(e+fx)\right]+31 B c^2 d^2 \cos\left[\frac{3}{2}(e+fx)\right]-25 A c d^3 \cos\left[\frac{3}{2}(e+fx)\right]+13 B c d^3 \cos\left[\frac{3}{2}(e+fx)\right]+A d^4 \cos\left[\frac{3}{2}(e+fx)\right]+2 B d^4 \cos\left[\frac{3}{2}(e+fx)\right]+2 A c^2 d^2 \cos\left[\frac{5}{2}(e+fx)\right]-9 B c^2 d^2 \cos\left[\frac{5}{2}(e+fx)\right]+15 A c d^3 \cos\left[\frac{5}{2}(e+fx)\right]-9 B c d^3 \cos\left[\frac{5}{2}(e+fx)\right]+7 A d^4 \cos\left[\frac{5}{2}(e+fx)\right]-6 B d^4 \cos\left[\frac{5}{2}(e+fx)\right]+8 A c^4 \sin\left[\frac{1}{2}(e+fx)\right]-8 B c^4 \sin\left[\frac{1}{2}(e+fx)\right]+8 A c^3 d \sin\left[\frac{1}{2}(e+fx)\right]-26 B c^3 d \sin\left[\frac{1}{2}(e+fx)\right]+22 A c^2 d^2 \sin\left[\frac{1}{2}(e+fx)\right]-6 B c^2 d^2 \sin\left[\frac{1}{2}(e+fx)\right]+10 A c d^3 \sin\left[\frac{1}{2}(e+fx)\right]-4 B c d^3 \sin\left[\frac{1}{2}(e+fx)\right]-4 B d^4 \sin\left[\frac{1}{2}(e+fx)\right]-8 A c^3 d \sin\left[\frac{3}{2}(e+fx)\right]+26 B c^3 d \sin\left[\frac{3}{2}(e+fx)\right]-40 A c^2 d^2 \sin\left[\frac{3}{2}(e+fx)\right]+31 B c^2 d^2 \sin\left[\frac{3}{2}(e+fx)\right]-25 A c d^3 \sin\left[\frac{3}{2}(e+fx)\right]+13 B c d^3 \sin\left[\frac{3}{2}(e+fx)\right]+A d^4 \sin\left[\frac{3}{2}(e+fx)\right]+2 B d^4 \sin\left[\frac{3}{2}(e+fx)\right]-2 A c^2 d^2 \sin\left[\frac{5}{2}(e+fx)\right]+9 B c^2 d^2 \sin\left[\frac{5}{2}(e+fx)\right]-15 A c d^3 \sin\left[\frac{5}{2}(e+fx)\right]+9 B c d^3 \sin\left[\frac{5}{2}(e+fx)\right]-7 A d^4 \sin\left[\frac{5}{2}(e+fx)\right]+6 B d^4 \sin\left[\frac{5}{2}(e+fx)\right]\right)$$

**Problem 321: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(A+B \sin[e+fx])(c+d \sin[e+fx])^3}{(a+a \sin[e+fx])^{5/2}} dx$$

Optimal (type 3, 308 leaves, 7 steps):



$$\begin{aligned}
 & - \frac{1}{16 \sqrt{2} a^{5/2} f} \\
 & (c-d) (B (5 c^2 + 62 c d - 163 d^2) + 3 A (c^2 + 6 c d + 25 d^2)) \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \operatorname{Cos}[e+f x]}{\sqrt{2} \sqrt{a+a \operatorname{Sin}[e+f x]}} \right] + \\
 & \frac{d (A (9 c^2 + 36 c d - 93 d^2) + B (15 c^2 - 228 c d + 197 d^2)) \operatorname{Cos}[e+f x]}{24 a^2 f \sqrt{a+a \operatorname{Sin}[e+f x]}} + \\
 & \frac{d^2 (9 A c + 15 B c + 39 A d - 95 B d) \operatorname{Cos}[e+f x] \sqrt{a+a \operatorname{Sin}[e+f x]}}{48 a^3 f} - \\
 & \frac{(3 A c + 5 B c + 9 A d - 17 B d) \operatorname{Cos}[e+f x] (c+d \operatorname{Sin}[e+f x])^2}{16 a f (a+a \operatorname{Sin}[e+f x])^{3/2}} - \\
 & \frac{(A-B) \operatorname{Cos}[e+f x] (c+d \operatorname{Sin}[e+f x])^3}{4 f (a+a \operatorname{Sin}[e+f x])^{5/2}}
 \end{aligned}$$

Result (type 3, 523 leaves):

$$\begin{aligned}
 & \frac{1}{48 f (a (1 + \operatorname{Sin}[e+f x]))^{5/2}} \left( \operatorname{Cos} \left[ \frac{1}{2} (e+f x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (e+f x) \right] \right) \\
 & \left( 24 (A-B) (c-d)^3 \operatorname{Sin} \left[ \frac{1}{2} (e+f x) \right] - 12 (A-B) (c-d)^3 \left( \operatorname{Cos} \left[ \frac{1}{2} (e+f x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (e+f x) \right] \right) + 6 \right. \\
 & (c-d)^2 (B (5 c - 29 d) + 3 A (c+7 d)) \operatorname{Sin} \left[ \frac{1}{2} (e+f x) \right] \left( \operatorname{Cos} \left[ \frac{1}{2} (e+f x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (e+f x) \right] \right)^2 - \\
 & 3 (c-d)^2 (B (5 c - 29 d) + 3 A (c+7 d)) \left( \operatorname{Cos} \left[ \frac{1}{2} (e+f x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (e+f x) \right] \right)^3 + \\
 & (3+3 i) (-1)^{3/4} (c-d) (B (5 c^2 + 62 c d - 163 d^2) + 3 A (c^2 + 6 c d + 25 d^2)) \\
 & \operatorname{ArcTanh} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \left( -1 + \operatorname{Tan} \left[ \frac{1}{4} (e+f x) \right] \right) \right] \left( \operatorname{Cos} \left[ \frac{1}{2} (e+f x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (e+f x) \right] \right)^4 - \\
 & 16 B d^3 \operatorname{Cos} \left[ \frac{3}{2} (e+f x) \right] \left( \operatorname{Cos} \left[ \frac{1}{2} (e+f x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (e+f x) \right] \right)^4 + \\
 & (24+24 i) d^2 (-6 B c - 2 A d + 5 B d) \left( \operatorname{Cos} \left[ \frac{1}{2} (e+f x) \right] + i \operatorname{Sin} \left[ \frac{1}{2} (e+f x) \right] \right) \\
 & \left( \operatorname{Cos} \left[ \frac{1}{2} (e+f x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (e+f x) \right] \right)^4 + (24+24 i) d^2 (6 B c + 2 A d - 5 B d) \\
 & \left( i \operatorname{Cos} \left[ \frac{1}{2} (e+f x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (e+f x) \right] \right) \left( \operatorname{Cos} \left[ \frac{1}{2} (e+f x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (e+f x) \right] \right)^4 - \\
 & 16 B d^3 \left( \operatorname{Cos} \left[ \frac{1}{2} (e+f x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (e+f x) \right] \right)^4 \operatorname{Sin} \left[ \frac{3}{2} (e+f x) \right] \left. \right)
 \end{aligned}$$

**Problem 322: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(A+B \operatorname{Sin}[e+f x]) (c+d \operatorname{Sin}[e+f x])^2}{(a+a \operatorname{Sin}[e+f x])^{5/2}} dx$$

Optimal (type 3, 219 leaves, 6 steps):

$$-\frac{1}{16\sqrt{2}a^{5/2}f} \left( B(5c^2 + 38cd - 75d^2) + A(3c^2 + 10cd + 19d^2) \right) \text{ArcTanh} \left[ \frac{\sqrt{a} \cos[e+fx]}{\sqrt{2}\sqrt{a+a\sin[e+fx]}} \right] - \frac{(c-d)(3Ac + 5Bc + 5Ad - 13Bd) \cos[e+fx]}{16af(a+a\sin[e+fx])^{3/2}} + \frac{(A-9B)d^2 \cos[e+fx]}{4a^2f\sqrt{a+a\sin[e+fx]}} - \frac{(A-B)\cos[e+fx](c+d\sin[e+fx])^2}{4f(a+a\sin[e+fx])^{5/2}}$$

Result (type 3, 544 leaves):

$$\frac{1}{32f(a(1+\sin[e+fx]))^{5/2}} \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right) \left( -11Ac^2 \cos\left[\frac{1}{2}(e+fx)\right] + 3Bc^2 \cos\left[\frac{1}{2}(e+fx)\right] + 6Acd \cos\left[\frac{1}{2}(e+fx)\right] + 10Bcd \cos\left[\frac{1}{2}(e+fx)\right] + 5Ad^2 \cos\left[\frac{1}{2}(e+fx)\right] - 45Bd^2 \cos\left[\frac{1}{2}(e+fx)\right] - 3Ac^2 \cos\left[\frac{3}{2}(e+fx)\right] - 5Bc^2 \cos\left[\frac{3}{2}(e+fx)\right] - 10Acd \cos\left[\frac{3}{2}(e+fx)\right] + 26Bcd \cos\left[\frac{3}{2}(e+fx)\right] + 13Ad^2 \cos\left[\frac{3}{2}(e+fx)\right] - 69Bd^2 \cos\left[\frac{3}{2}(e+fx)\right] + 16Bd^2 \cos\left[\frac{5}{2}(e+fx)\right] + 11Ac^2 \sin\left[\frac{1}{2}(e+fx)\right] - 3Bc^2 \sin\left[\frac{1}{2}(e+fx)\right] - 6Acd \sin\left[\frac{1}{2}(e+fx)\right] - 10Bcd \sin\left[\frac{1}{2}(e+fx)\right] - 5Ad^2 \sin\left[\frac{1}{2}(e+fx)\right] + 45Bd^2 \sin\left[\frac{1}{2}(e+fx)\right] + (2+2i)(-1)^{3/4} (B(5c^2 + 38cd - 75d^2) + A(3c^2 + 10cd + 19d^2)) \text{ArcTanh} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \left( -1 + \tan\left[\frac{1}{4}(e+fx)\right] \right) \right] \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^4 - 3Ac^2 \sin\left[\frac{3}{2}(e+fx)\right] - 5Bc^2 \sin\left[\frac{3}{2}(e+fx)\right] - 10Acd \sin\left[\frac{3}{2}(e+fx)\right] + 26Bcd \sin\left[\frac{3}{2}(e+fx)\right] + 13Ad^2 \sin\left[\frac{3}{2}(e+fx)\right] - 69Bd^2 \sin\left[\frac{3}{2}(e+fx)\right] - 16Bd^2 \sin\left[\frac{5}{2}(e+fx)\right] \right)$$

**Problem 323: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(A+B \sin[e+fx])(c+d \sin[e+fx])}{(a+a \sin[e+fx])^{5/2}} dx$$

Optimal (type 3, 151 leaves, 5 steps):

$$\frac{(3Ac + 5Bc + 5Ad + 19Bd) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[e+fx]}{\sqrt{2} \sqrt{a+a \sin[e+fx]}}\right]}{16 \sqrt{2} a^{5/2} f} - \frac{(A-B)(c-d) \cos[e+fx]}{4f(a+a \sin[e+fx])^{5/2}} - \frac{(3Ac + 5Bc + 5Ad - 13Bd) \cos[e+fx]}{16af(a+a \sin[e+fx])^{3/2}}$$

Result (type 3, 267 leaves):

$$\frac{1}{16f(a(1+\sin[e+fx]))^{5/2}} \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right) + \left( 8(A-B)(c-d) \sin\left[\frac{1}{2}(e+fx)\right] - 4(A-B)(c-d) \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right) + 2(3Ac + 5Bc + 5Ad - 13Bd) \sin\left[\frac{1}{2}(e+fx)\right] \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^2 - (3Ac + 5Bc + 5Ad - 13Bd) \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^3 + (1+i)(-1)^{3/4}(3Ac + 5Bc + 5Ad + 19Bd) \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right)(-1)^{3/4} \left(-1 + \tan\left[\frac{1}{4}(e+fx)\right]\right)\right] \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^4 \right)$$

**Problem 324: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A+B \sin[e+fx]}{(a+a \sin[e+fx])^{5/2}} dx$$

Optimal (type 3, 126 leaves, 4 steps):

$$\frac{(3A+5B) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[e+fx]}{\sqrt{2} \sqrt{a+a \sin[e+fx]}}\right]}{16 \sqrt{2} a^{5/2} f} - \frac{(A-B) \cos[e+fx]}{4f(a+a \sin[e+fx])^{5/2}} - \frac{(3A+5B) \cos[e+fx]}{16af(a+a \sin[e+fx])^{3/2}}$$

Result (type 3, 227 leaves):

$$\frac{1}{16f(a(1+\sin[e+fx]))^{5/2}} \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right) + \left( 8(A-B) \sin\left[\frac{1}{2}(e+fx)\right] + 4(-A+B) \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right) + 2(3A+5B) \sin\left[\frac{1}{2}(e+fx)\right] \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^2 - (3A+5B) \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^3 + (1+i)(-1)^{3/4}(3A+5B) \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right)(-1)^{3/4} \left(-1 + \tan\left[\frac{1}{4}(e+fx)\right]\right)\right] \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^4 \right)$$

**Problem 325: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sin[e + f x]}{(a + a \sin[e + f x])^{5/2} (c + d \sin[e + f x])} dx$$

Optimal (type 3, 261 leaves, 7 steps):

$$\begin{aligned} & - \left( \left( (B (5 c^2 - 34 c d - 3 d^2) + A (3 c^2 - 14 c d + 43 d^2)) \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \cos[e + f x]}{\sqrt{2} \sqrt{a + a \sin[e + f x]}} \right] \right) \right) / \\ & \left( 16 \sqrt{2} a^{5/2} (c - d)^3 f \right) - \frac{2 d^{3/2} (B c - A d) \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \sqrt{d} \cos[e + f x]}{\sqrt{c+d} \sqrt{a + a \sin[e + f x]}} \right]}{a^{5/2} (c - d)^3 \sqrt{c+d} f} - \\ & \frac{(A - B) \cos[e + f x]}{4 (c - d) f (a + a \sin[e + f x])^{5/2}} - \frac{(3 A c + 5 B c - 11 A d + 3 B d) \cos[e + f x]}{16 a (c - d)^2 f (a + a \sin[e + f x])^{3/2}} \end{aligned}$$

Result (type 3, 550 leaves):

$$\begin{aligned} & \frac{1}{16 (c - d)^3 f (a (1 + \sin[e + f x]))^{5/2}} \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) \\ & \left( 8 (A - B) (c - d)^2 \sin \left[ \frac{1}{2} (e + f x) \right] + 4 (-A + B) (c - d)^2 \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right) + \\ & 2 (c - d) (3 A c + 5 B c - 11 A d + 3 B d) \sin \left[ \frac{1}{2} (e + f x) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^2 - \\ & (c - d) (3 A c + 5 B c - 11 A d + 3 B d) \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^3 + \\ & (1 + i) (-1)^{3/4} (B (5 c^2 - 34 c d - 3 d^2) + A (3 c^2 - 14 c d + 43 d^2)) \\ & \operatorname{ArcTanh} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \left( -1 + \tan \left[ \frac{1}{4} (e + f x) \right] \right) \right] \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^4 + \\ & \frac{1}{\sqrt{c+d}} 8 d^{3/2} (-B c + A d) \left( e + f x - 2 \log \left[ \sec \left[ \frac{1}{4} (e + f x) \right] \right]^2 \right) + \\ & 2 \log \left[ \sec \left[ \frac{1}{4} (e + f x) \right] \right]^2 \left( \sqrt{c+d} + \sqrt{d} \cos \left[ \frac{1}{2} (e + f x) \right] - \sqrt{d} \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right) \\ & \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^4 + \frac{1}{\sqrt{c+d}} \\ & 8 d^{3/2} (B c - A d) \left( e + f x - 2 \log \left[ \sec \left[ \frac{1}{4} (e + f x) \right] \right]^2 \right) + \\ & 2 \log \left[ \sec \left[ \frac{1}{4} (e + f x) \right] \right]^2 \left( \sqrt{c+d} - \sqrt{d} \cos \left[ \frac{1}{2} (e + f x) \right] + \sqrt{d} \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right) \\ & \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^4 \end{aligned}$$

**Problem 326: Result unnecessarily involves complex numbers and more than**

twice size of optimal antiderivative.

$$\int \frac{A + B \sin[e + f x]}{(a + a \sin[e + f x])^{5/2} (c + d \sin[e + f x])^2} dx$$

Optimal (type 3, 395 leaves, 8 steps):

$$\begin{aligned} & - \left( \left( (B (5 c^2 - 58 c d - 43 d^2) + A (3 c^2 - 22 c d + 115 d^2)) \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \cos[e + f x]}{\sqrt{2} \sqrt{a + a \sin[e + f x]}} \right] \right) / \right. \\ & \quad \left. (16 \sqrt{2} a^{5/2} (c - d)^4 f) \right) + \\ & \left( d^{3/2} (A d (7 c + 5 d) - B (5 c^2 + 5 c d + 2 d^2)) \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \sqrt{d} \cos[e + f x]}{\sqrt{c + d} \sqrt{a + a \sin[e + f x]}} \right] \right) / \\ & \quad (a^{5/2} (c - d)^4 (c + d)^{3/2} f) - \frac{(A - B) \cos[e + f x]}{4 (c - d) f (a + a \sin[e + f x])^{5/2} (c + d \sin[e + f x])} - \\ & \quad \frac{(3 A c + 5 B c - 15 A d + 7 B d) \cos[e + f x]}{16 a (c - d)^2 f (a + a \sin[e + f x])^{3/2} (c + d \sin[e + f x])} - \\ & \quad \frac{d (A (3 c^2 - 16 c d - 35 d^2) + B (5 c^2 + 32 c d + 11 d^2)) \cos[e + f x]}{16 a^2 (c - d)^3 (c + d) f \sqrt{a + a \sin[e + f x]} (c + d \sin[e + f x])} \end{aligned}$$

Result (type 3, 1318 leaves):

$$\begin{aligned} & \left( (1 + i) (3 A c^2 + 5 B c^2 - 22 A c d - 58 B c d + 115 A d^2 - 43 B d^2) \right. \\ & \quad \operatorname{ArcTanh} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \operatorname{Sec} \left[ \frac{1}{4} (e + f x) \right] \left( \cos \left[ \frac{1}{4} (e + f x) \right] - \sin \left[ \frac{1}{4} (e + f x) \right] \right) \right] \\ & \quad \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^5 \Bigg) / \\ & \quad \left( (16 (-1)^{1/4} c^4 - 64 (-1)^{1/4} c^3 d + 96 (-1)^{1/4} c^2 d^2 - 64 (-1)^{1/4} c d^3 + 16 (-1)^{1/4} d^4) \right. \\ & \quad \left. f (a (1 + \sin[e + f x]))^{5/2} \right) + \\ & \left( d^{3/2} (A d (7 c + 5 d) - B (5 c^2 + 5 c d + 2 d^2)) \left( e + f x - 2 \operatorname{Log} \left[ \operatorname{Sec} \left[ \frac{1}{4} (e + f x) \right] \right]^2 \right) + \right. \\ & \quad \left. 2 \operatorname{Log} \left[ \operatorname{Sec} \left[ \frac{1}{4} (e + f x) \right] \right]^2 \left( \sqrt{c + d} + \sqrt{d} \cos \left[ \frac{1}{2} (e + f x) \right] - \sqrt{d} \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right) \\ & \quad \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^5 \Bigg) / \left( 4 (c - d)^4 (c + d)^{3/2} f (a (1 + \sin[e + f x]))^{5/2} \right) + \\ & \left( d^{3/2} (-A d (7 c + 5 d) + B (5 c^2 + 5 c d + 2 d^2)) \left( e + f x - 2 \operatorname{Log} \left[ \operatorname{Sec} \left[ \frac{1}{4} (e + f x) \right] \right]^2 \right) + \right. \\ & \quad \left. 2 \operatorname{Log} \left[ \operatorname{Sec} \left[ \frac{1}{4} (e + f x) \right] \right]^2 \left( \sqrt{c + d} - \sqrt{d} \cos \left[ \frac{1}{2} (e + f x) \right] + \sqrt{d} \sin \left[ \frac{1}{2} (e + f x) \right] \right) \right) \\ & \quad \left( \cos \left[ \frac{1}{2} (e + f x) \right] + \sin \left[ \frac{1}{2} (e + f x) \right] \right)^5 \Bigg) / \left( 4 (c - d)^4 (c + d)^{3/2} f (a (1 + \sin[e + f x]))^{5/2} \right) + \\ & \quad \frac{1}{64 (c - d)^3 (c + d) f (a (1 + \sin[e + f x]))^{5/2} (c + d \sin[e + f x])} \end{aligned}$$

$$\begin{aligned}
& \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right) \\
& \left( -22Ac^3 \cos\left[\frac{1}{2}(e+fx)\right] + 6Bc^3 \cos\left[\frac{1}{2}(e+fx)\right] + 40Ac^2d \cos\left[\frac{1}{2}(e+fx)\right] - \right. \\
& 40Bc^2d \cos\left[\frac{1}{2}(e+fx)\right] + 54Ac^2d^2 \cos\left[\frac{1}{2}(e+fx)\right] - 70Bcd^2 \cos\left[\frac{1}{2}(e+fx)\right] + \\
& 24Ad^3 \cos\left[\frac{1}{2}(e+fx)\right] + 8Bd^3 \cos\left[\frac{1}{2}(e+fx)\right] - 6Ac^3 \cos\left[\frac{3}{2}(e+fx)\right] - \\
& 10Bc^3 \cos\left[\frac{3}{2}(e+fx)\right] + 21Ac^2d \cos\left[\frac{3}{2}(e+fx)\right] - 29Bc^2d \cos\left[\frac{3}{2}(e+fx)\right] + \\
& 54Ac^2d^2 \cos\left[\frac{3}{2}(e+fx)\right] - 86Bcd^2 \cos\left[\frac{3}{2}(e+fx)\right] + 75Ad^3 \cos\left[\frac{3}{2}(e+fx)\right] - \\
& 19Bd^3 \cos\left[\frac{3}{2}(e+fx)\right] + 3Ac^2d \cos\left[\frac{5}{2}(e+fx)\right] + 5Bc^2d \cos\left[\frac{5}{2}(e+fx)\right] - \\
& 16Ac^2d^2 \cos\left[\frac{5}{2}(e+fx)\right] + 32Bcd^2 \cos\left[\frac{5}{2}(e+fx)\right] - 35Ad^3 \cos\left[\frac{5}{2}(e+fx)\right] + \\
& 11Bd^3 \cos\left[\frac{5}{2}(e+fx)\right] + 22Ac^3 \sin\left[\frac{1}{2}(e+fx)\right] - 6Bc^3 \sin\left[\frac{1}{2}(e+fx)\right] - \\
& 40Ac^2d \sin\left[\frac{1}{2}(e+fx)\right] + 40Bc^2d \sin\left[\frac{1}{2}(e+fx)\right] - 54Ac^2d^2 \sin\left[\frac{1}{2}(e+fx)\right] + \\
& 70Bcd^2 \sin\left[\frac{1}{2}(e+fx)\right] - 24Ad^3 \sin\left[\frac{1}{2}(e+fx)\right] - 8Bd^3 \sin\left[\frac{1}{2}(e+fx)\right] - \\
& 6Ac^3 \sin\left[\frac{3}{2}(e+fx)\right] - 10Bc^3 \sin\left[\frac{3}{2}(e+fx)\right] + 21Ac^2d \sin\left[\frac{3}{2}(e+fx)\right] - \\
& 29Bc^2d \sin\left[\frac{3}{2}(e+fx)\right] + 54Ac^2d^2 \sin\left[\frac{3}{2}(e+fx)\right] - \\
& 86Bcd^2 \sin\left[\frac{3}{2}(e+fx)\right] + 75Ad^3 \sin\left[\frac{3}{2}(e+fx)\right] - 19Bd^3 \sin\left[\frac{3}{2}(e+fx)\right] - \\
& 3Ac^2d \sin\left[\frac{5}{2}(e+fx)\right] - 5Bc^2d \sin\left[\frac{5}{2}(e+fx)\right] + 16Ac^2d^2 \sin\left[\frac{5}{2}(e+fx)\right] - \\
& \left. 32Bcd^2 \sin\left[\frac{5}{2}(e+fx)\right] + 35Ad^3 \sin\left[\frac{5}{2}(e+fx)\right] - 11Bd^3 \sin\left[\frac{5}{2}(e+fx)\right] \right)
\end{aligned}$$

**Problem 327: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sin[e + fx]}{(a + a \sin[e + fx])^{5/2} (c + d \sin[e + fx])^3} dx$$

Optimal (type 3, 519 leaves, 9 steps):

$$\begin{aligned}
 & - \left( \left( B (5c^2 - 82cd - 115d^2) + 3A (c^2 - 10cd + 73d^2) \right) \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \operatorname{Cos}[e+fx]}{\sqrt{2} \sqrt{a+a \operatorname{Sin}[e+fx]}} \right] \right) / \\
 & \left( 16\sqrt{2} a^{5/2} (c-d)^5 f \right) + \left( d^{3/2} (3Ad (21c^2 + 30cd + 13d^2) - B (35c^3 + 70c^2d + 67cd^2 + 20d^3)) \right. \\
 & \left. \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \sqrt{d} \operatorname{Cos}[e+fx]}{\sqrt{c+d} \sqrt{a+a \operatorname{Sin}[e+fx]}} \right] \right) / \left( 4a^{5/2} (c-d)^5 (c+d)^{5/2} f \right) - \\
 & \frac{(A-B) \operatorname{Cos}[e+fx]}{4(c-d) f (a+a \operatorname{Sin}[e+fx])^{5/2} (c+d \operatorname{Sin}[e+fx])^2} - \\
 & \frac{(3Ac + 5Bc - 19Ad + 11Bd) \operatorname{Cos}[e+fx]}{16a(c-d)^2 f (a+a \operatorname{Sin}[e+fx])^{3/2} (c+d \operatorname{Sin}[e+fx])^2} - \\
 & \frac{d(A(3c^2 - 20cd - 31d^2) + B(5c^2 + 28cd + 15d^2)) \operatorname{Cos}[e+fx]}{16a^2(c-d)^3 (c+d) f \sqrt{a+a \operatorname{Sin}[e+fx]} (c+d \operatorname{Sin}[e+fx])^2} - \\
 & \frac{(d(3A(c^3 - 7c^2d - 37cd^2 - 21d^3) + B(5c^3 + 73c^2d + 79cd^2 + 35d^3)) \operatorname{Cos}[e+fx])}{(16a^2(c-d)^4 (c+d)^2 f \sqrt{a+a \operatorname{Sin}[e+fx]} (c+d \operatorname{Sin}[e+fx]))}
 \end{aligned}$$

Result (type 3, 2103 leaves):

$$\begin{aligned}
 & \left( (1+i) (3Ac^2 + 5Bc^2 - 30Acd - 82Bcd + 219Ad^2 - 115Bd^2) \right. \\
 & \left. \operatorname{ArcTanh} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \operatorname{Sec} \left[ \frac{1}{4} (e+fx) \right] \left( \operatorname{Cos} \left[ \frac{1}{4} (e+fx) \right] - \operatorname{Sin} \left[ \frac{1}{4} (e+fx) \right] \right) \right] \right) \\
 & \left( \operatorname{Cos} \left[ \frac{1}{2} (e+fx) \right] + \operatorname{Sin} \left[ \frac{1}{2} (e+fx) \right] \right)^5 / \\
 & \left( (16(-1)^{1/4} c^5 - 80(-1)^{1/4} c^4 d + 160(-1)^{1/4} c^3 d^2 - 160(-1)^{1/4} c^2 d^3 + \right. \\
 & \left. 80(-1)^{1/4} c d^4 - 16(-1)^{1/4} d^5) f (a(1 + \operatorname{Sin}[e+fx]))^{5/2} \right) - \\
 & \left( d^{3/2} (-3Ad (21c^2 + 30cd + 13d^2) + B (35c^3 + 70c^2d + 67cd^2 + 20d^3)) \right. \\
 & \left( e+fx - 2 \operatorname{Log} \left[ \operatorname{Sec} \left[ \frac{1}{4} (e+fx) \right]^2 \right] + \right. \\
 & \left. 2 \operatorname{Log} \left[ \operatorname{Sec} \left[ \frac{1}{4} (e+fx) \right]^2 \left( \sqrt{c+d} + \sqrt{d} \operatorname{Cos} \left[ \frac{1}{2} (e+fx) \right] - \sqrt{d} \operatorname{Sin} \left[ \frac{1}{2} (e+fx) \right] \right) \right] \right) \\
 & \left( \operatorname{Cos} \left[ \frac{1}{2} (e+fx) \right] + \operatorname{Sin} \left[ \frac{1}{2} (e+fx) \right] \right)^5 / \left( 16(c-d)^5 (c+d)^{5/2} f (a(1 + \operatorname{Sin}[e+fx]))^{5/2} \right) + \\
 & \left( d^{3/2} (-3Ad (21c^2 + 30cd + 13d^2) + B (35c^3 + 70c^2d + 67cd^2 + 20d^3)) \right. \\
 & \left( e+fx - 2 \operatorname{Log} \left[ \operatorname{Sec} \left[ \frac{1}{4} (e+fx) \right]^2 \right] + \right. \\
 & \left. 2 \operatorname{Log} \left[ \operatorname{Sec} \left[ \frac{1}{4} (e+fx) \right]^2 \left( \sqrt{c+d} - \sqrt{d} \operatorname{Cos} \left[ \frac{1}{2} (e+fx) \right] + \sqrt{d} \operatorname{Sin} \left[ \frac{1}{2} (e+fx) \right] \right) \right] \right) \\
 & \left( \operatorname{Cos} \left[ \frac{1}{2} (e+fx) \right] + \operatorname{Sin} \left[ \frac{1}{2} (e+fx) \right] \right)^5 / \left( 16(c-d)^5 (c+d)^{5/2} f (a(1 + \operatorname{Sin}[e+fx]))^{5/2} \right) +
 \end{aligned}$$

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$$\begin{aligned}
& 128 (c-d)^4 (c+d)^2 f (a (1 + \sin[e+fx]))^{5/2} (c+d \sin[e+fx])^2 \\
& \left( \cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right) \\
& \left( -44 A c^5 \cos\left[\frac{1}{2}(e+fx)\right] + 12 B c^5 \cos\left[\frac{1}{2}(e+fx)\right] + 84 A c^4 d \cos\left[\frac{1}{2}(e+fx)\right] - \right. \\
& 116 B c^4 d \cos\left[\frac{1}{2}(e+fx)\right] + 249 A c^3 d^2 \cos\left[\frac{1}{2}(e+fx)\right] - 433 B c^3 d^2 \cos\left[\frac{1}{2}(e+fx)\right] + \\
& 385 A c^2 d^3 \cos\left[\frac{1}{2}(e+fx)\right] - 277 B c^2 d^3 \cos\left[\frac{1}{2}(e+fx)\right] + 239 A c d^4 \cos\left[\frac{1}{2}(e+fx)\right] - \\
& 95 B c d^4 \cos\left[\frac{1}{2}(e+fx)\right] + 47 A d^5 \cos\left[\frac{1}{2}(e+fx)\right] - 51 B d^5 \cos\left[\frac{1}{2}(e+fx)\right] - \\
& 12 A c^5 \cos\left[\frac{3}{2}(e+fx)\right] - 20 B c^5 \cos\left[\frac{3}{2}(e+fx)\right] + 40 A c^4 d \cos\left[\frac{3}{2}(e+fx)\right] - \\
& 104 B c^4 d \cos\left[\frac{3}{2}(e+fx)\right] + 261 A c^3 d^2 \cos\left[\frac{3}{2}(e+fx)\right] - 581 B c^3 d^2 \cos\left[\frac{3}{2}(e+fx)\right] + \\
& 781 A c^2 d^3 \cos\left[\frac{3}{2}(e+fx)\right] - 665 B c^2 d^3 \cos\left[\frac{3}{2}(e+fx)\right] + 579 A c d^4 \cos\left[\frac{3}{2}(e+fx)\right] - \\
& 299 B c d^4 \cos\left[\frac{3}{2}(e+fx)\right] + 79 A d^5 \cos\left[\frac{3}{2}(e+fx)\right] - 59 B d^5 \cos\left[\frac{3}{2}(e+fx)\right] + \\
& 12 A c^4 d \cos\left[\frac{5}{2}(e+fx)\right] + 20 B c^4 d \cos\left[\frac{5}{2}(e+fx)\right] - 73 A c^3 d^2 \cos\left[\frac{5}{2}(e+fx)\right] + \\
& 217 B c^3 d^2 \cos\left[\frac{5}{2}(e+fx)\right] - 353 A c^2 d^3 \cos\left[\frac{5}{2}(e+fx)\right] + 397 B c^2 d^3 \cos\left[\frac{5}{2}(e+fx)\right] - \\
& 419 A c d^4 \cos\left[\frac{5}{2}(e+fx)\right] + 251 B c d^4 \cos\left[\frac{5}{2}(e+fx)\right] - 127 A d^5 \cos\left[\frac{5}{2}(e+fx)\right] + \\
& 75 B d^5 \cos\left[\frac{5}{2}(e+fx)\right] + 3 A c^3 d^2 \cos\left[\frac{7}{2}(e+fx)\right] + 5 B c^3 d^2 \cos\left[\frac{7}{2}(e+fx)\right] - \\
& 21 A c^2 d^3 \cos\left[\frac{7}{2}(e+fx)\right] + 73 B c^2 d^3 \cos\left[\frac{7}{2}(e+fx)\right] - 111 A c d^4 \cos\left[\frac{7}{2}(e+fx)\right] + \\
& 79 B c d^4 \cos\left[\frac{7}{2}(e+fx)\right] - 63 A d^5 \cos\left[\frac{7}{2}(e+fx)\right] + 35 B d^5 \cos\left[\frac{7}{2}(e+fx)\right] + \\
& 44 A c^5 \sin\left[\frac{1}{2}(e+fx)\right] - 12 B c^5 \sin\left[\frac{1}{2}(e+fx)\right] - 84 A c^4 d \sin\left[\frac{1}{2}(e+fx)\right] + \\
& 116 B c^4 d \sin\left[\frac{1}{2}(e+fx)\right] - 249 A c^3 d^2 \sin\left[\frac{1}{2}(e+fx)\right] + 433 B c^3 d^2 \sin\left[\frac{1}{2}(e+fx)\right] - \\
& 385 A c^2 d^3 \sin\left[\frac{1}{2}(e+fx)\right] + 277 B c^2 d^3 \sin\left[\frac{1}{2}(e+fx)\right] - 239 A c d^4 \sin\left[\frac{1}{2}(e+fx)\right] + \\
& 95 B c d^4 \sin\left[\frac{1}{2}(e+fx)\right] - 47 A d^5 \sin\left[\frac{1}{2}(e+fx)\right] + 51 B d^5 \sin\left[\frac{1}{2}(e+fx)\right] - \\
& 12 A c^5 \sin\left[\frac{3}{2}(e+fx)\right] - 20 B c^5 \sin\left[\frac{3}{2}(e+fx)\right] + 40 A c^4 d \sin\left[\frac{3}{2}(e+fx)\right] - \\
& 104 B c^4 d \sin\left[\frac{3}{2}(e+fx)\right] + 261 A c^3 d^2 \sin\left[\frac{3}{2}(e+fx)\right] - 581 B c^3 d^2 \sin\left[\frac{3}{2}(e+fx)\right] + \\
& 781 A c^2 d^3 \sin\left[\frac{3}{2}(e+fx)\right] - 665 B c^2 d^3 \sin\left[\frac{3}{2}(e+fx)\right] + 579 A c d^4 \sin\left[\frac{3}{2}(e+fx)\right] -
\end{aligned}$$



$$\begin{aligned}
 & 299 B c d^4 \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right]+79 A d^5 \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right]-59 B d^5 \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right]- \\
 & 12 A c^4 d \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right]-20 B c^4 d \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right]+73 A c^3 d^2 \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right]- \\
 & 217 B c^3 d^2 \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right]+353 A c^2 d^3 \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right]-397 B c^2 d^3 \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right]+ \\
 & 419 A c d^4 \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right]-251 B c d^4 \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right]+127 A d^5 \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right]- \\
 & 75 B d^5 \operatorname{Sin}\left[\frac{5}{2}(e+f x)\right]+3 A c^3 d^2 \operatorname{Sin}\left[\frac{7}{2}(e+f x)\right]+5 B c^3 d^2 \operatorname{Sin}\left[\frac{7}{2}(e+f x)\right]- \\
 & 21 A c^2 d^3 \operatorname{Sin}\left[\frac{7}{2}(e+f x)\right]+73 B c^2 d^3 \operatorname{Sin}\left[\frac{7}{2}(e+f x)\right]-111 A c d^4 \operatorname{Sin}\left[\frac{7}{2}(e+f x)\right]+ \\
 & 79 B c d^4 \operatorname{Sin}\left[\frac{7}{2}(e+f x)\right]-63 A d^5 \operatorname{Sin}\left[\frac{7}{2}(e+f x)\right]+35 B d^5 \operatorname{Sin}\left[\frac{7}{2}(e+f x)\right]
 \end{aligned}$$

### Problem 328: Unable to integrate problem.

$$\int (a+a \operatorname{Sin}[e+f x])^2 (A+B \operatorname{Sin}[e+f x]) (c+d \operatorname{Sin}[e+f x])^n dx$$

Optimal (type 6, 221 leaves, 7 steps):

$$\begin{aligned}
 & -\left(\left[8 \sqrt{2} a^2 B \operatorname{AppellF1}\left[\frac{1}{2},-\frac{5}{2},-n,\frac{3}{2},\frac{1}{2}(1-\operatorname{Sin}[e+f x]),\frac{d(1-\operatorname{Sin}[e+f x])}{c+d}\right]\right.\right. \\
 & \quad \left.\left.\operatorname{Cos}[e+f x](c+d \operatorname{Sin}[e+f x])^n\left(\frac{c+d \operatorname{Sin}[e+f x]}{c+d}\right)^{-n}\right] / \left(f \sqrt{1+\operatorname{Sin}[e+f x]}\right)\right) - \\
 & \left(4 \sqrt{2} a^2(A-B) \operatorname{AppellF1}\left[\frac{1}{2},-\frac{3}{2},-n,\frac{3}{2},\frac{1}{2}(1-\operatorname{Sin}[e+f x]),\frac{d(1-\operatorname{Sin}[e+f x])}{c+d}\right]\right. \\
 & \quad \left.\operatorname{Cos}[e+f x](c+d \operatorname{Sin}[e+f x])^n\left(\frac{c+d \operatorname{Sin}[e+f x]}{c+d}\right)^{-n}\right] / \left(f \sqrt{1+\operatorname{Sin}[e+f x]}\right)
 \end{aligned}$$

Result (type 8, 37 leaves):

$$\int (a+a \operatorname{Sin}[e+f x])^2 (A+B \operatorname{Sin}[e+f x]) (c+d \operatorname{Sin}[e+f x])^n dx$$

### Problem 329: Unable to integrate problem.

$$\int (a+a \operatorname{Sin}[e+f x]) (A+B \operatorname{Sin}[e+f x]) (c+d \operatorname{Sin}[e+f x])^n dx$$

Optimal (type 6, 217 leaves, 8 steps):

$$\begin{aligned}
 & - \left( \left[ 4 \sqrt{2} a B \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{3}{2}, -n, \frac{3}{2}, \frac{1}{2} (1 - \sin[e + f x]), \frac{d (1 - \sin[e + f x])}{c + d} \right] \right. \right. \\
 & \quad \left. \left. \cos[e + f x] (c + d \sin[e + f x])^n \left( \frac{c + d \sin[e + f x]}{c + d} \right)^{-n} \right] / \left( f \sqrt{1 + \sin[e + f x]} \right) \right) - \\
 & \left( 2 \sqrt{2} a (A - B) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2}, -n, \frac{3}{2}, \frac{1}{2} (1 - \sin[e + f x]), \frac{d (1 - \sin[e + f x])}{c + d} \right] \right. \\
 & \quad \left. \cos[e + f x] (c + d \sin[e + f x])^n \left( \frac{c + d \sin[e + f x]}{c + d} \right)^{-n} \right] / \left( f \sqrt{1 + \sin[e + f x]} \right)
 \end{aligned}$$

Result (type 8, 35 leaves):

$$\int (a + a \sin[e + f x]) (A + B \sin[e + f x]) (c + d \sin[e + f x])^n dx$$

**Problem 330: Unable to integrate problem.**

$$\int \frac{(A + B \sin[e + f x]) (c + d \sin[e + f x])^n}{a + a \sin[e + f x]} dx$$

Optimal (type 6, 221 leaves, 7 steps):

$$\begin{aligned}
 & - \left( \left[ \sqrt{2} B \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, -n, \frac{3}{2}, \frac{1}{2} (1 - \sin[e + f x]), \frac{d (1 - \sin[e + f x])}{c + d} \right] \right. \right. \\
 & \quad \left. \left. \cos[e + f x] (c + d \sin[e + f x])^n \left( \frac{c + d \sin[e + f x]}{c + d} \right)^{-n} \right] / \left( a f \sqrt{1 + \sin[e + f x]} \right) \right) - \\
 & \left( (A - B) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{3}{2}, -n, \frac{3}{2}, \frac{1}{2} (1 - \sin[e + f x]), \frac{d (1 - \sin[e + f x])}{c + d} \right] \cos[e + f x] \right. \\
 & \quad \left. (c + d \sin[e + f x])^n \left( \frac{c + d \sin[e + f x]}{c + d} \right)^{-n} \right] / \left( \sqrt{2} a f \sqrt{1 + \sin[e + f x]} \right)
 \end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{(A + B \sin[e + f x]) (c + d \sin[e + f x])^n}{a + a \sin[e + f x]} dx$$

**Problem 331: Unable to integrate problem.**

$$\int \frac{(A + B \sin[e + f x]) (c + d \sin[e + f x])^n}{(a + a \sin[e + f x])^2} dx$$

Optimal (type 6, 223 leaves, 7 steps):

$$\begin{aligned}
 & - \left( \left( B \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{3}{2}, -n, \frac{3}{2}, \frac{1}{2} (1 - \sin[e + f x]), \frac{d (1 - \sin[e + f x])}{c + d} \right] \cos[e + f x] \right. \right. \\
 & \quad \left. \left. (c + d \sin[e + f x])^n \left( \frac{c + d \sin[e + f x]}{c + d} \right)^{-n} \right) / \left( \sqrt{2} a^2 f \sqrt{1 + \sin[e + f x]} \right) \right) - \\
 & \left( (A - B) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{5}{2}, -n, \frac{3}{2}, \frac{1}{2} (1 - \sin[e + f x]), \frac{d (1 - \sin[e + f x])}{c + d} \right] \cos[e + f x] \right. \\
 & \quad \left. (c + d \sin[e + f x])^n \left( \frac{c + d \sin[e + f x]}{c + d} \right)^{-n} \right) / \left( 2 \sqrt{2} a^2 f \sqrt{1 + \sin[e + f x]} \right)
 \end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{(A + B \sin[e + f x]) (c + d \sin[e + f x])^n}{(a + a \sin[e + f x])^2} dx$$

**Problem 333: Unable to integrate problem.**

$$\int \sqrt{a + a \sin[e + f x]} (A + B \sin[e + f x]) (c + d \sin[e + f x])^n dx$$

Optimal (type 5, 167 leaves, 4 steps):

$$\begin{aligned}
 & - \frac{2 a B \cos[e + f x] (c + d \sin[e + f x])^{1+n}}{d f (3 + 2 n) \sqrt{a + a \sin[e + f x]}} - \left( 2 a (A d (3 + 2 n) - B (c - 2 d (1 + n))) \right. \\
 & \quad \cos[e + f x] \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, -n, \frac{3}{2}, \frac{d (1 - \sin[e + f x])}{c + d} \right] \\
 & \quad \left. (c + d \sin[e + f x])^n \left( \frac{c + d \sin[e + f x]}{c + d} \right)^{-n} \right) / \left( d f (3 + 2 n) \sqrt{a + a \sin[e + f x]} \right)
 \end{aligned}$$

Result (type 8, 39 leaves):

$$\int \sqrt{a + a \sin[e + f x]} (A + B \sin[e + f x]) (c + d \sin[e + f x])^n dx$$

**Problem 334: Result more than twice size of optimal antiderivative.**

$$\int \frac{(A + B \sin[e + f x]) (c + d \sin[e + f x])^n}{\sqrt{a + a \sin[e + f x]}} dx$$

Optimal (type 6, 220 leaves, 7 steps):

$$\begin{aligned}
 & - \left( \left( (A - B) \operatorname{AppellF1} \left[ 1 + n, \frac{1}{2}, 1, 2 + n, \frac{c + d \sin[e + f x]}{c + d}, \frac{c + d \sin[e + f x]}{c - d} \right] \right. \right. \\
 & \quad \left. \left. \cos[e + f x] \sqrt{\frac{d(1 - \sin[e + f x])}{c + d}} (c + d \sin[e + f x])^{1+n} \right) / \right. \\
 & \quad \left. \left( (c - d) f (1 + n) (1 - \sin[e + f x]) \sqrt{a + a \sin[e + f x]} \right) \right) - \\
 & \left( 2 B \cos[e + f x] \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, -n, \frac{3}{2}, \frac{d(1 - \sin[e + f x])}{c + d} \right] \right. \\
 & \quad \left. (c + d \sin[e + f x])^n \left( \frac{c + d \sin[e + f x]}{c + d} \right)^{-n} \right) / \left( f \sqrt{a + a \sin[e + f x]} \right)
 \end{aligned}$$

Result (type 6, 1282 leaves):

$$\begin{aligned}
 & \frac{1}{a} \left( a^2 B \cos[e + f x] \sin[e + f x] \right. \\
 & \quad (1 + \sin[e + f x])^2 (c + d \sin[e + f x])^{2n} \left( c + \frac{d(-a + a(1 + \sin[e + f x]))}{a} \right)^{-n} \\
 & \quad \left( \left( 4 a (c - d) \operatorname{AppellF1} \left[ 1, \frac{1}{2}, -n, 2, \frac{1}{2} (1 + \sin[e + f x]), -\frac{a d (1 + \sin[e + f x])}{a c - a d} \right] \right) / \right. \\
 & \quad \left( 8 a (c - d) \operatorname{AppellF1} \left[ 1, \frac{1}{2}, -n, 2, \frac{1}{2} (1 + \sin[e + f x]), -\frac{a d (1 + \sin[e + f x])}{a c - a d} \right] + \right. \\
 & \quad a \left( 4 d n \operatorname{AppellF1} \left[ 2, \frac{1}{2}, 1 - n, 3, \frac{1}{2} (1 + \sin[e + f x]), -\frac{a d (1 + \sin[e + f x])}{a c - a d} \right] + \right. \\
 & \quad \left. \left. (c - d) \operatorname{AppellF1} \left[ 2, \frac{3}{2}, -n, 3, \frac{1}{2} (1 + \sin[e + f x]), -\frac{a d (1 + \sin[e + f x])}{a c - a d} \right] \right) \right) \\
 & \quad (1 + \sin[e + f x]) + \left( d (-1 + 2 n) \operatorname{AppellF1} \left[ -\frac{1}{2} - n, -\frac{1}{2}, -n, \frac{1}{2} - n, \right. \right. \\
 & \quad \left. \left. \frac{2}{1 + \sin[e + f x]}, \frac{-c + d}{d (1 + \sin[e + f x])} \right] (-2 a + a (1 + \sin[e + f x])) \right) \Big/ \\
 & \quad \left( (1 + 2 n) \left( 2 a \left( (-c + d) n \operatorname{AppellF1} \left[ \frac{1}{2} - n, -\frac{1}{2}, 1 - n, \frac{3}{2} - n, \frac{2}{1 + \sin[e + f x]}, \right. \right. \right. \right. \\
 & \quad \left. \left. \frac{-c + d}{d (1 + \sin[e + f x])} \right] + d \operatorname{AppellF1} \left[ \frac{1}{2} - n, \frac{1}{2}, -n, \frac{3}{2} - n, \frac{2}{1 + \sin[e + f x]}, \right. \right. \\
 & \quad \left. \left. \frac{-c + d}{d (1 + \sin[e + f x])} \right] \right) + a d (-1 + 2 n) \operatorname{AppellF1} \left[ -\frac{1}{2} - n, -\frac{1}{2}, -n, \frac{1}{2} - \right. \\
 & \quad \left. \left. n, \frac{2}{1 + \sin[e + f x]}, \frac{-c + d}{d (1 + \sin[e + f x])} \right] (1 + \sin[e + f x]) \right) \Big/
 \end{aligned}$$

$$\left( f \sqrt{a(1+\sin[e+fx])} (-a+a(1+\sin[e+fx])) \right.$$

$$\sqrt{\frac{2a^2(1+\sin[e+fx]) - a^2(1+\sin[e+fx])^2}{a^2}}$$

$$\left. \sqrt{1 - \frac{(-a+a(1+\sin[e+fx]))^2}{a^2}} \right) +$$

$$\left( a^2 A \cos[e+fx] (1+\sin[e+fx])^2 (c+d \sin[e+fx])^{2n} \right.$$

$$\left( c + \frac{d(-a+a(1+\sin[e+fx]))}{a} \right)^{-n}$$

$$\left( \left( 4(c-d) \operatorname{AppellF1}\left[1, \frac{1}{2}, -n, 2, \frac{1}{2}(1+\sin[e+fx]), -\frac{ad(1+\sin[e+fx])}{ac-ad}\right] \right) / \right.$$

$$\left( 8a(c-d) \operatorname{AppellF1}\left[1, \frac{1}{2}, -n, 2, \frac{1}{2}(1+\sin[e+fx]), -\frac{ad(1+\sin[e+fx])}{ac-ad}\right] + \right.$$

$$a \left( 4dn \operatorname{AppellF1}\left[2, \frac{1}{2}, 1-n, 3, \frac{1}{2}(1+\sin[e+fx]), -\frac{ad(1+\sin[e+fx])}{ac-ad}\right] + \right.$$

$$\left. \left. (c-d) \operatorname{AppellF1}\left[2, \frac{3}{2}, -n, 3, \frac{1}{2}(1+\sin[e+fx]), -\frac{ad(1+\sin[e+fx])}{ac-ad}\right] \right) \right)$$

$$(1+\sin[e+fx]) \left) - \left( d(-1+2n) \operatorname{AppellF1}\left[-\frac{1}{2}-n, -\frac{1}{2}, -n, \frac{1}{2}-n, \right. \right.$$

$$\left. \left. \frac{2}{1+\sin[e+fx]}, \frac{-c+d}{d(1+\sin[e+fx])}\right] (-2a+a(1+\sin[e+fx])) \right) /$$

$$\left( a(1+2n) \left( 2a \left( (-c+d)n \operatorname{AppellF1}\left[\frac{1}{2}-n, -\frac{1}{2}, 1-n, \frac{3}{2}-n, \frac{2}{1+\sin[e+fx]}, \right. \right. \right.$$

$$\left. \left. \frac{-c+d}{d(1+\sin[e+fx])}\right] + d \operatorname{AppellF1}\left[\frac{1}{2}-n, \frac{1}{2}, -n, \frac{3}{2}-n, \frac{2}{1+\sin[e+fx]}, \right. \right.$$

$$\left. \left. \frac{-c+d}{d(1+\sin[e+fx])}\right] + ad(-1+2n) \operatorname{AppellF1}\left[-\frac{1}{2}-n, -\frac{1}{2}, -n, \frac{1}{2}- \right. \right.$$

$$\left. \left. n, \frac{2}{1+\sin[e+fx]}, \frac{-c+d}{d(1+\sin[e+fx])}\right] (1+\sin[e+fx]) \right) \right) \right) /$$

$$\left( f \sqrt{a(1+\sin[e+fx])} \sqrt{\frac{2a^2(1+\sin[e+fx]) - a^2(1+\sin[e+fx])^2}{a^2}} \right.$$

$$\left. \sqrt{1 - \frac{(-a+a(1+\sin[e+fx]))^2}{a^2}} \right)$$

**Problem 335: Result more than twice size of optimal antiderivative.**

$$\int \frac{(A + B \sin[e + f x]) (c + d \sin[e + f x])^n}{(a + a \sin[e + f x])^{3/2}} dx$$

Optimal (type 6, 269 leaves, 7 steps):

$$- \left( \left( B \operatorname{AppellF1} \left[ 1+n, \frac{1}{2}, 1, 2+n, \frac{c+d \sin[e+f x]}{c+d}, \frac{c+d \sin[e+f x]}{c-d} \right] \right. \right. \\ \left. \left. \cos[e+f x] \sqrt{\frac{d(1-\sin[e+f x])}{c+d}} (c+d \sin[e+f x])^{1+n} \right) / \right. \\ \left. (a(c-d) f (1+n) (1-\sin[e+f x]) \sqrt{a+a \sin[e+f x]}) \right) + \\ \left( (A-B) d \operatorname{AppellF1} \left[ 1+n, \frac{1}{2}, 2, 2+n, \frac{c+d \sin[e+f x]}{c+d}, \frac{c+d \sin[e+f x]}{c-d} \right] \right. \\ \left. \cos[e+f x] \sqrt{\frac{d(1-\sin[e+f x])}{c+d}} (c+d \sin[e+f x])^{1+n} \right) / \\ \left( (c-d)^2 f (1+n) (a-a \sin[e+f x]) \sqrt{a+a \sin[e+f x]} \right)$$

Result (type 6, 1854 leaves):

$$\left( B \cos[e+f x] \sin[e+f x] (1+\sin[e+f x]) \right. \\ \left. (c+d \sin[e+f x])^{2n} \left( c + \frac{d(-a+a(1+\sin[e+f x]))}{a} \right)^{-n} \right. \\ \left. \left( \left( 4 a (c-d) \operatorname{AppellF1} \left[ 1, \frac{1}{2}, -n, 2, \frac{1}{2} (1+\sin[e+f x]), -\frac{a d (1+\sin[e+f x])}{a c-a d} \right] \right. \right. \right. \\ \left. \left. (1+\sin[e+f x]) \right) / \right. \\ \left( 8 a (c-d) \operatorname{AppellF1} \left[ 1, \frac{1}{2}, -n, 2, \frac{1}{2} (1+\sin[e+f x]), -\frac{a d (1+\sin[e+f x])}{a c-a d} \right] \right. + \\ \left. a \left( 4 d n \operatorname{AppellF1} \left[ 2, \frac{1}{2}, 1-n, 3, \frac{1}{2} (1+\sin[e+f x]), -\frac{a d (1+\sin[e+f x])}{a c-a d} \right] \right. + \right. \\ \left. \left. (c-d) \operatorname{AppellF1} \left[ 2, \frac{3}{2}, -n, 3, \frac{1}{2} (1+\sin[e+f x]), -\frac{a d (1+\sin[e+f x])}{a c-a d} \right] \right) \right. \\ \left. (1+\sin[e+f x]) \right) - \left( d (-1+2n) \operatorname{AppellF1} \left[ -\frac{1}{2}-n, -\frac{1}{2}, -n, \frac{1}{2}-n, \right. \right.$$

$$\begin{aligned}
 & \left. \left. \left. \left. \frac{2}{1 + \sin[e + f x]}, \frac{-c + d}{d(1 + \sin[e + f x])} \right] (1 + \sin[e + f x]) (-2a + a(1 + \sin[e + f x])) \right) \right) / \\
 & \left( (1 + 2n) \left( 2a \left( (-c + d)n \operatorname{AppellF1} \left[ \frac{1}{2} - n, -\frac{1}{2}, 1 - n, \frac{3}{2} - n, \frac{2}{1 + \sin[e + f x]}, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{-c + d}{d(1 + \sin[e + f x])} \right] + d \operatorname{AppellF1} \left[ \frac{1}{2} - n, \frac{1}{2}, -n, \frac{3}{2} - n, \frac{2}{1 + \sin[e + f x]}, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{-c + d}{d(1 + \sin[e + f x])} \right] \right) + a d (-1 + 2n) \operatorname{AppellF1} \left[ -\frac{1}{2} - n, -\frac{1}{2}, -n, \right. \right. \\
 & \quad \left. \left. \frac{1}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{-c + d}{d(1 + \sin[e + f x])} \right] (1 + \sin[e + f x]) \right) \right) + \\
 & \left( 2d(-3 + 2n) \operatorname{AppellF1} \left[ \frac{1}{2} - n, -\frac{1}{2}, -n, \frac{3}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{-c + d}{d(1 + \sin[e + f x])} \right] \right. \\
 & \quad \left. (-2a + a(1 + \sin[e + f x])) \right) / \\
 & \left( (-1 + 2n) \left( 2a \left( (-c + d)n \operatorname{AppellF1} \left[ \frac{3}{2} - n, -\frac{1}{2}, 1 - n, \frac{5}{2} - n, \frac{2}{1 + \sin[e + f x]}, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{-c + d}{d(1 + \sin[e + f x])} \right] + d \operatorname{AppellF1} \left[ \frac{3}{2} - n, \frac{1}{2}, -n, \frac{5}{2} - n, \frac{2}{1 + \sin[e + f x]}, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{-c + d}{d(1 + \sin[e + f x])} \right] \right) + a d (-3 + 2n) \operatorname{AppellF1} \left[ \frac{1}{2} - n, -\frac{1}{2}, -n, \right. \right. \\
 & \quad \left. \left. \frac{3}{2} - n, \frac{2}{1 + \sin[e + f x]}, \frac{-c + d}{d(1 + \sin[e + f x])} \right] (1 + \sin[e + f x]) \right) \right) \right) / \\
 & \left( 2f \sqrt{a(1 + \sin[e + f x])} (-a + a(1 + \sin[e + f x])) \right. \\
 & \quad \sqrt{\frac{2a^2(1 + \sin[e + f x]) - a^2(1 + \sin[e + f x])^2}{a^2}} \\
 & \quad \left. \sqrt{1 - \frac{(-a + a(1 + \sin[e + f x]))^2}{a^2}} \right) + \\
 & \left( A \cos[e + f x] (1 + \sin[e + f x]) (c + d \sin[e + f x])^{2n} \right. \\
 & \quad \left( c + \frac{d(-a + a(1 + \sin[e + f x]))}{a} \right)^{-n} \\
 & \quad \left( \left( 4a^2(c - d) \operatorname{AppellF1} \left[ 1, \frac{1}{2}, -n, 2, \frac{1}{2}(1 + \sin[e + f x]), \right. \right. \right. \right. \\
 & \quad \left. \left. \left. - \frac{a d(1 + \sin[e + f x])}{a c - a d} \right] (1 + \sin[e + f x]) \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( 8 a (c-d) \operatorname{AppellF1}\left[1, \frac{1}{2}, -n, 2, \frac{1}{2} (1+\sin[e+fx]), -\frac{ad(1+\sin[e+fx])}{ac-ad}\right] + \right. \\
 & a \left( 4 d n \operatorname{AppellF1}\left[2, \frac{1}{2}, 1-n, 3, \frac{1}{2} (1+\sin[e+fx]), -\frac{ad(1+\sin[e+fx])}{ac-ad}\right] + \right. \\
 & \quad \left. (c-d) \operatorname{AppellF1}\left[2, \frac{3}{2}, -n, 3, \frac{1}{2} (1+\sin[e+fx]), -\frac{ad(1+\sin[e+fx])}{ac-ad}\right] \right) \\
 & \left. (1+\sin[e+fx]) \right) - \left( ad(-1+2n) \operatorname{AppellF1}\left[-\frac{1}{2}-n, -\frac{1}{2}, -n, \frac{1}{2}-n, \right. \right. \\
 & \quad \left. \frac{2}{1+\sin[e+fx]}, \frac{-c+d}{d(1+\sin[e+fx])}\right] (1+\sin[e+fx]) (-2a+a(1+\sin[e+fx])) \Big) \Big) / \\
 & \left( (1+2n) \left( 2a \left( (-c+d)n \operatorname{AppellF1}\left[\frac{1}{2}-n, -\frac{1}{2}, 1-n, \frac{3}{2}-n, \frac{2}{1+\sin[e+fx]}, \right. \right. \right. \right. \\
 & \quad \left. \frac{-c+d}{d(1+\sin[e+fx])}\right] + d \operatorname{AppellF1}\left[\frac{1}{2}-n, \frac{1}{2}, -n, \frac{3}{2}-n, \frac{2}{1+\sin[e+fx]}, \right. \\
 & \quad \left. \frac{-c+d}{d(1+\sin[e+fx])}\right] \Big) + ad(-1+2n) \operatorname{AppellF1}\left[-\frac{1}{2}-n, -\frac{1}{2}, -n, \right. \\
 & \quad \left. \frac{1}{2}-n, \frac{2}{1+\sin[e+fx]}, \frac{-c+d}{d(1+\sin[e+fx])}\right] (1+\sin[e+fx]) \Big) \Big) - \\
 & \left( 2ad(-3+2n) \operatorname{AppellF1}\left[\frac{1}{2}-n, -\frac{1}{2}, -n, \frac{3}{2}-n, \frac{2}{1+\sin[e+fx]}, \frac{-c+d}{d(1+\sin[e+fx])}\right] \right) \\
 & \left. (-2a+a(1+\sin[e+fx])) \Big) \Big) / \\
 & \left( (-1+2n) \left( 2a \left( (-c+d)n \operatorname{AppellF1}\left[\frac{3}{2}-n, -\frac{1}{2}, 1-n, \frac{5}{2}-n, \frac{2}{1+\sin[e+fx]}, \right. \right. \right. \right. \right. \\
 & \quad \left. \frac{-c+d}{d(1+\sin[e+fx])}\right] + d \operatorname{AppellF1}\left[\frac{3}{2}-n, \frac{1}{2}, -n, \frac{5}{2}-n, \frac{2}{1+\sin[e+fx]}, \right. \\
 & \quad \left. \frac{-c+d}{d(1+\sin[e+fx])}\right] \Big) + ad(-3+2n) \operatorname{AppellF1}\left[\frac{1}{2}-n, -\frac{1}{2}, -n, \right. \\
 & \quad \left. \frac{3}{2}-n, \frac{2}{1+\sin[e+fx]}, \frac{-c+d}{d(1+\sin[e+fx])}\right] (1+\sin[e+fx]) \Big) \Big) \Big) \Big) / \\
 & \left( 2a^2 f \sqrt{a(1+\sin[e+fx])} \sqrt{\frac{2a^2(1+\sin[e+fx]) - a^2(1+\sin[e+fx])^2}{a^2}} \right. \\
 & \left. \sqrt{1 - \frac{(-a+a(1+\sin[e+fx]))^2}{a^2}} \right)
 \end{aligned}$$

Problem 336: Result more than twice size of optimal antiderivative.



$$\int (a + a \sin[e + f x])^m (A + B \sin[e + f x]) (c + d \sin[e + f x])^2 dx$$

Optimal (type 5, 351 leaves, 6 steps):

$$\begin{aligned} & \left( (d (A d (3 + m) + B (2 c + d m)) - 2 (2 + m) (A c d (3 + m) + B (c^2 + d^2 + c d m))) \right. \\ & \quad \left. \cos[e + f x] (a + a \sin[e + f x])^m \right) / (f (1 + m) (2 + m) (3 + m)) - \\ & \left( 2^{\frac{1}{2}+m} (A (3 + m) (2 c d m (2 + m) + d^2 (1 + m + m^2) + c^2 (2 + 3 m + m^2)) + \right. \\ & \quad \left. B (d^2 m (5 + 3 m + m^2) + c^2 m (6 + 5 m + m^2) + 2 c d (3 + 4 m + 4 m^2 + m^3))) \right) \\ & \quad \cos[e + f x] \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{2} - m, \frac{3}{2}, \frac{1}{2} (1 - \sin[e + f x])\right] \\ & \quad \left(1 + \sin[e + f x]\right)^{-\frac{1}{2}-m} (a + a \sin[e + f x])^m \Big/ (f (1 + m) (2 + m) (3 + m)) - \\ & \quad \frac{d (A d (3 + m) + B (2 c + d m)) \cos[e + f x] (a + a \sin[e + f x])^{1+m}}{a f (2 + m) (3 + m)} - \\ & \quad \frac{B \cos[e + f x] (a + a \sin[e + f x])^m (c + d \sin[e + f x])^2}{f (3 + m)} \end{aligned}$$

Result (type 5, 23845 leaves): Display of huge result suppressed!

**Problem 338: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (a + a \sin[e + f x])^m (A + B \sin[e + f x]) dx$$

Optimal (type 5, 117 leaves, 3 steps):

$$\begin{aligned} & \frac{B \cos[e + f x] (a + a \sin[e + f x])^m}{f (1 + m)} - \frac{1}{f (1 + m)} 2^{\frac{1}{2}+m} (A + A m + B m) \cos[e + f x] \\ & \quad \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{2} - m, \frac{3}{2}, \frac{1}{2} (1 - \sin[e + f x])\right] (1 + \sin[e + f x])^{-\frac{1}{2}-m} (a + a \sin[e + f x])^m \end{aligned}$$

Result (type 5, 295 leaves):

$$\begin{aligned} & -\frac{1}{f} (a (1 + \sin[e + f x]))^m \\ & \left( \frac{1}{-1 + m^2} 2^{-1-2m} B e^{-i (e+f x)} (1 + i e^{-i (e+f x)})^{-2m} \left( e^{-\frac{1}{4} i (2e+\pi+2fx)} (i + e^{i (e+f x)}) \right)^{2m} \right. \\ & \quad \left( e^{2i (e+f x)} (-1 + m) \operatorname{Hypergeometric2F1}[-1 - m, -2m, -m, -i e^{-i (e+f x)}] - \right. \\ & \quad \left. (1 + m) \operatorname{Hypergeometric2F1}[1 - m, -2m, 2 - m, -i e^{-i (e+f x)}] \right) + \\ & \quad \left( 2 \sqrt{2} A \cos\left[\frac{1}{4} (2e - \pi + 2fx)\right] \right)^{1+2m} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{2} + m, \frac{3}{2} + m, \right. \\ & \quad \left. \sin\left[\frac{1}{4} (2e + \pi + 2fx)\right]^2 \right] \sin\left[\frac{1}{4} (2e - \pi + 2fx)\right] \Big/ \\ & \quad \left( (1 + 2m) \sqrt{1 - \sin[e + f x]} \right) \sin\left[\frac{1}{4} (2e + \pi + 2fx)\right]^{-2m} \end{aligned}$$

### Problem 339: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sin[e + f x])^m (A + B \sin[e + f x])}{c + d \sin[e + f x]} dx$$

Optimal (type 6, 191 leaves, 6 steps):

$$- \left( \left( \sqrt{2} (B c - A d) \operatorname{AppellF1} \left[ \frac{1}{2} + m, \frac{1}{2}, 1, \frac{3}{2} + m, \frac{1}{2} (1 + \sin[e + f x]) \right], - \frac{d (1 + \sin[e + f x])}{c - d} \right) \right. \\ \left. \cos[e + f x] (a + a \sin[e + f x])^m \right) / \left( (c - d) d f (1 + 2m) \sqrt{1 - \sin[e + f x]} \right) - \\ \frac{1}{d f} 2^{\frac{1}{2} + m} B \cos[e + f x] \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1}{2} - m, \frac{3}{2}, \frac{1}{2} (1 - \sin[e + f x]) \right] \\ (1 + \sin[e + f x])^{-\frac{1}{2} - m} (a + a \sin[e + f x])^m$$

Result (type 6, 1022 leaves):

$$- \frac{1}{f} \cos \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{-2m} \\ \left( - \left( \left( 6 A (c + d) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} - m, 1, \frac{3}{2}, \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c + d} \right] \right) \right. \right. \\ \left. \cos \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{-1+2m} \left( \cos \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{\frac{1}{2} - m} \right. \\ \left. \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right] \left( 1 - \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{-\frac{1}{2} + m} \right) / \\ \left( (c + d - 2 d \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2) \left( -3 (c + d) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} - m, 1, \frac{3}{2}, \right. \right. \right. \\ \left. \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c + d} \right] + \left( -4 d \right. \right. \\ \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} - m, 2, \frac{5}{2}, \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c + d} \right] \right) + \right. \\ \left. (c + d) (-1 + 2m) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} - m, 1, \frac{5}{2}, \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\ \left. \left. \frac{2 d \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c + d} \right] \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \right) + \\ B \left( - \left( \left( 2 \cos \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{1+2m} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1}{2} (1 + 2m), \frac{1}{2} (3 + 2m), \right. \right. \right. \right.$$

$$\begin{aligned}
 & \left. \begin{aligned}
 & \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \Big/ \\
 & \left( d(1+2m) \sqrt{\sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right) + \left( 6c(c+d) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2} - m, 1, \right. \right. \\
 & \left. \left. \frac{3}{2}, \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \frac{2d \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^{-1+2m} \right. \\
 & \left. \left. \left( \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^{\frac{1}{2}-m} \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \left(1 - \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{-\frac{1}{2}+m} \right) \Big/ \right. \\
 & \left. \left( d(c+d - 2d \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2) \left( -3(c+d) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2} - m, 1, \frac{3}{2}, \right. \right. \right. \right. \\
 & \left. \left. \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \frac{2d \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] + \left( -4d \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \right. \\
 & \left. \left. \frac{1}{2} - m, 2, \frac{5}{2}, \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \frac{2d \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] + \right. \\
 & \left. \left. (c+d)(-1+2m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{3}{2} - m, 1, \frac{5}{2}, \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{2d \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) \right) \right) \left( a + a \sin[e + fx] \right)^m
 \end{aligned}
 \right.
 \end{aligned}$$

### Problem 340: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sin[e + fx])^m (A + B \sin[e + fx])}{(c + d \sin[e + fx])^2} dx$$

Optimal (type 6, 293 leaves, 7 steps):

$$\begin{aligned}
 & \left( \sqrt{2} (Ad(c(1-m) - dm) - B(d^2 - c^2m - cdm)) \operatorname{AppellF1}\left[\frac{1}{2} + m, \frac{1}{2}, 1, \frac{3}{2} + m, \right. \right. \\
 & \left. \left. \frac{1}{2} (1 + \sin[e + fx]), -\frac{d(1 + \sin[e + fx])}{c-d}\right] \cos[e + fx] (a + a \sin[e + fx])^m \right) \Big/ \\
 & \left( (c-d)^2 d(c+d) f(1+2m) \sqrt{1 - \sin[e + fx]} \right) + \frac{1}{d(c^2 - d^2) f} \\
 & 2^{\frac{1}{2}+m} (Bc - Ad) m \cos[e + fx] \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{2} - m, \frac{3}{2}, \frac{1}{2} (1 - \sin[e + fx])\right] \\
 & (1 + \sin[e + fx])^{-\frac{1}{2}+m} (a + a \sin[e + fx])^m - \frac{(Bc - Ad) \cos[e + fx] (a + a \sin[e + fx])^m}{(c^2 - d^2) f (c + d \sin[e + fx])}
 \end{aligned}$$

Result (type 6, 1332 leaves):

$$\begin{aligned}
& -\frac{1}{f} \operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^{-2m} \\
& \left( -\left( \left( 6A(c+d) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}-m, 2, \frac{3}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, \frac{2d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right) \right. \right. \\
& \quad \operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^{-1+2m} \left(\operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)^{\frac{1}{2}-m} \\
& \quad \left. \left. \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right] \left(1 - \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)^{-\frac{1}{2}+m} \right) \right) / \\
& \left( \left( c+d - 2d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)^2 \left( -3(c+d) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}-m, 2, \right. \right. \right. \\
& \quad \left. \left. \frac{3}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, \frac{2d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] + \left( -8d \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}-m, 3, \frac{5}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, \frac{2d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] + \right. \right. \\
& \quad \left. \left. (c+d)(-1+2m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{3}{2}-m, 2, \frac{5}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, \right. \right. \\
& \quad \left. \left. \frac{2d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] \right) \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right) \right) + \\
& B \left( -\left( \left( 6(c+d) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}-m, 1, \frac{3}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, \right. \right. \right. \\
& \quad \left. \left. \frac{2d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] \operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^{-1+2m} \left(\operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)^{\frac{1}{2}-m} \right. \right. \\
& \quad \left. \left. \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right] \left(1 - \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)^{-\frac{1}{2}+m} \right) \right) / \\
& \left( d \left( c+d - 2d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)^2 \left( -3(c+d) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}-m, 1, \frac{3}{2}, \right. \right. \right. \\
& \quad \left. \left. \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, \frac{2d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] + \left( -4d \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \\
& \quad \left. \left. \frac{1}{2}-m, 2, \frac{5}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, \frac{2d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] + \right. \right. \\
& \quad \left. \left. (c+d)(-1+2m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{3}{2}-m, 1, \frac{5}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\right) + \\
 & \left(6 c(c+d) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}-m, 2, \frac{3}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right], \right. \\
 & \left. \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \operatorname{Cos}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^{-1+2 m}\left(\operatorname{Cos}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{\frac{1}{2}-m} \right. \\
 & \left. \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]\left(1-\operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{-\frac{1}{2}+m}\right) / \\
 & \left(d\left(c+d-2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^2\left(-3(c+d) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}-m, 2, \frac{3}{2}, \right. \right. \right. \\
 & \left. \left. \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] + \left(-8 d \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \left. \left. \frac{1}{2}-m, 3, \frac{5}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] + \right. \right. \\
 & \left. \left. (c+d)(-1+2 m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{3}{2}-m, 2, \frac{5}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \left. \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\right)\right) \left(a+a \operatorname{Sin}[e+f x]\right)^m
 \end{aligned}$$

**Problem 341: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a+a \operatorname{Sin}[e+f x])^m (A+B \operatorname{Sin}[e+f x])}{(c+d \operatorname{Sin}[e+f x])^3} dx$$

Optimal (type 6, 467 leaves, 8 steps):

$$\left( (B (2 d^3 m + c^3 (1 - m) m + 2 c^2 d (1 - m) m - c d^2 (3 - 3 m + m^2)) - A d (2 c d (2 - m) m - c^2 (2 - 3 m + m^2) - d^2 (1 - m + m^2))) \operatorname{AppellF1}\left[\frac{1}{2} + m, \frac{1}{2}, 1, \frac{3}{2} + m, \frac{1}{2} (1 + \operatorname{Sin}[e + f x]), -\frac{d (1 + \operatorname{Sin}[e + f x])}{c - d}\right] \operatorname{Cos}[e + f x] (a + a \operatorname{Sin}[e + f x])^m \right) /$$

$$\left( \sqrt{2} (c - d)^3 d (c + d)^2 f (1 + 2 m) \sqrt{1 - \operatorname{Sin}[e + f x]} \right) - \frac{1}{d (c^2 - d^2)^2 f}$$

$$2^{-\frac{1}{2} + m} m (A d (c (3 - m) - d m) - B (2 d^2 + c^2 (1 - m) - c d m)) \operatorname{Cos}[e + f x] \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{2} - m, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sin}[e + f x])\right] (1 + \operatorname{Sin}[e + f x])^{-\frac{1}{2} - m} (a + a \operatorname{Sin}[e + f x])^m - \frac{(B c - A d) \operatorname{Cos}[e + f x] (a + a \operatorname{Sin}[e + f x])^m}{2 (c^2 - d^2) f (c + d \operatorname{Sin}[e + f x])^2} + \frac{((A d (c (3 - m) - d m) - B (2 d^2 + c^2 (1 - m) - c d m)) \operatorname{Cos}[e + f x] (a + a \operatorname{Sin}[e + f x])^m)}{(2 (c^2 - d^2)^2 f (c + d \operatorname{Sin}[e + f x]))} /$$

Result (type 6, 1332 leaves):

$$-\frac{1}{f} \operatorname{Cos}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^{-2m}$$

$$\left( - \left( \left( 6 A (c + d) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2} - m, 3, \frac{3}{2}, \operatorname{Sin}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, \frac{2 d \operatorname{Sin}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c + d}\right] \right)^2 \operatorname{Cos}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^{-1+2m} \left(\operatorname{Cos}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^{\frac{1}{2}-m} \operatorname{Sin}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right] \left(1 - \operatorname{Sin}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^{-\frac{1}{2}+m} \right) /$$

$$\left( (c + d - 2 d \operatorname{Sin}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2)^3 \left( -3 (c + d) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2} - m, 3, \frac{3}{2}, \operatorname{Sin}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, \frac{2 d \operatorname{Sin}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c + d}\right] + \left( -12 d \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2} - m, 4, \frac{5}{2}, \operatorname{Sin}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, \frac{2 d \operatorname{Sin}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c + d}\right] + (c + d) (-1 + 2 m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{3}{2} - m, 3, \frac{5}{2}, \operatorname{Sin}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, \frac{2 d \operatorname{Sin}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c + d}\right] \right) \operatorname{Sin}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right) \right) /$$

$$\begin{aligned}
 & B \left( - \left( \left( 6 (c+d) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} - m, 2, \frac{3}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right] \right]^2, \right. \right. \right. \\
 & \quad \left. \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{-1+2m} \left( \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{\frac{1}{2}-m} \right. \\
 & \quad \left. \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right] \left( 1 - \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{-\frac{1}{2}+m} \right) / \\
 & \left( d \left( c+d - 2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right] \right)^2 \left( -3 (c+d) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} - m, 2, \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] + \left( -8 d \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \frac{1}{2} - m, 3, \frac{5}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] + \right. \\
 & \quad \left. (c+d) (-1+2m) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} - m, 2, \frac{5}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \right) + \\
 & \left( 6 c (c+d) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} - m, 3, \frac{3}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right] \right]^2, \right. \\
 & \quad \left. \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{-1+2m} \left( \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{\frac{1}{2}-m} \right. \\
 & \quad \left. \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right] \left( 1 - \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{-\frac{1}{2}+m} \right) / \\
 & \left( d \left( c+d - 2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right] \right)^3 \left( -3 (c+d) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} - m, 3, \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] + \left( -12 d \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \frac{1}{2} - m, 4, \frac{5}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] + \right. \\
 & \quad \left. (c+d) (-1+2m) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} - m, 3, \frac{5}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \right)
 \end{aligned}$$

$$\left. \left. \left. \left. \left. \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \right] \right] \right] \right] (a+a \operatorname{Sin}[e+f x])^m$$

**Problem 342: Result more than twice size of optimal antiderivative.**

$$\int (a+a \operatorname{Sin}[e+f x])^m (A+B \operatorname{Sin}[e+f x]) (c+d \operatorname{Sin}[e+f x])^{3/2} dx$$

Optimal (type 6, 284 leaves, 9 steps):

$$\begin{aligned} & \left( \sqrt{2} (A-B) (c-d) \operatorname{AppellF1}\left[\frac{1}{2}+m, \frac{1}{2}, -\frac{3}{2}, \frac{3}{2}+m, \frac{1}{2} (1+\operatorname{Sin}[e+f x]), -\frac{d(1+\operatorname{Sin}[e+f x])}{c-d}\right] \right. \\ & \quad \left. \operatorname{Cos}[e+f x] (a+a \operatorname{Sin}[e+f x])^m \sqrt{c+d \operatorname{Sin}[e+f x]} \right) / \\ & \left( f (1+2m) \sqrt{1-\operatorname{Sin}[e+f x]} \sqrt{\frac{c+d \operatorname{Sin}[e+f x]}{c-d}} \right) + \\ & \left( \sqrt{2} B (c-d) \operatorname{AppellF1}\left[\frac{3}{2}+m, \frac{1}{2}, -\frac{3}{2}, \frac{5}{2}+m, \frac{1}{2} (1+\operatorname{Sin}[e+f x]), -\frac{d(1+\operatorname{Sin}[e+f x])}{c-d}\right] \right. \\ & \quad \left. \operatorname{Cos}[e+f x] (a+a \operatorname{Sin}[e+f x])^{1+m} \sqrt{c+d \operatorname{Sin}[e+f x]} \right) / \\ & \left( a f (3+2m) \sqrt{1-\operatorname{Sin}[e+f x]} \sqrt{\frac{c+d \operatorname{Sin}[e+f x]}{c-d}} \right) \end{aligned}$$

Result (type 6, 4033 leaves):

$$\begin{aligned} & -\frac{1}{f} \operatorname{Cos}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^{-2m} \left( -\left( \left( 3 B d (c+d) \right. \right. \right. \\ & \quad \left. \left. \left. \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}-m, -\frac{1}{2}, \frac{3}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \right. \right. \right. \\ & \quad \left. \left. \left. \operatorname{Cos}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^{3+2m} \left( \operatorname{Cos}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \right)^{\frac{1}{2}+\frac{1}{2}(-4-2m)} \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right] \right. \right. \right. \\ & \quad \left. \left. \left. \left( 1-\operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \right)^{\frac{3}{2}+m} \sqrt{c+d-2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2} \right) / \left( -3 (c+d) \right. \right. \right. \\ & \quad \left. \left. \left. \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}-m, -\frac{1}{2}, \frac{3}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \right) \right) + \\ & \quad \left( 2 d \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}-m, \frac{1}{2}, \frac{5}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \right) + \end{aligned}$$



$$\begin{aligned}
 & \left. \left( (c+d) (3+2m) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2}-m, -\frac{1}{2}, \frac{5}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) - \\
 & \left( 6 B c (c+d) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2}-m, -\frac{1}{2}, \frac{3}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{1+2m} \right. \\
 & \quad \left. \left( \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{\frac{1}{2}+\frac{1}{2}(-2-2m)} \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right] \right. \\
 & \quad \left. \left( 1 - \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{\frac{1}{2}+m} \sqrt{c+d - 2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2} \right) / \\
 & \left( -3 (c+d) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2}-m, -\frac{1}{2}, \frac{3}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] + \right. \\
 & \quad \left. \left( 2 d \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2}-m, \frac{1}{2}, \frac{5}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] + \right. \right. \\
 & \quad \left. (c+d) (1+2m) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2}-m, -\frac{1}{2}, \frac{5}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) - \\
 & \left( 6 A d (c+d) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2}-m, -\frac{1}{2}, \frac{3}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{1+2m} \right. \\
 & \quad \left. \left( \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{\frac{1}{2}+\frac{1}{2}(-2-2m)} \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right] \right. \\
 & \quad \left. \left( 1 - \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{\frac{1}{2}+m} \sqrt{c+d - 2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2} \right) / \\
 & \left( -3 (c+d) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2}-m, -\frac{1}{2}, \frac{3}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] + \\
 & \left( 2 d \operatorname{AppellF1}\left[\frac{3}{2},-\frac{1}{2}-m,\frac{1}{2},\frac{5}{2},\operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2,\frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right]^2 + \right. \\
 & \quad (c+d)(1+2 m) \operatorname{AppellF1}\left[\frac{3}{2},\frac{1}{2}-m,-\frac{1}{2},\frac{5}{2},\operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2, \\
 & \quad \left. \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) + \\
 & \left( 6 A c(c+d) \operatorname{AppellF1}\left[\frac{1}{2},\frac{1}{2}-m,-\frac{1}{2},\frac{3}{2},\operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2,\right. \\
 & \quad \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\left.] \operatorname{Cos}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^{-1+2 m}\right. \\
 & \quad \left(\operatorname{Cos}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{\frac{1}{2}-m} \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right] \\
 & \quad \left. \left(1-\operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{-\frac{1}{2}+m} \sqrt{c+d-2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}\right) / \\
 & \left( 3(c+d) \operatorname{AppellF1}\left[\frac{1}{2},\frac{1}{2}-m,-\frac{1}{2},\frac{3}{2},\operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2,\frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right]^2 - \\
 & \left( 2 d \operatorname{AppellF1}\left[\frac{3}{2},\frac{1}{2}-m,\frac{1}{2},\frac{5}{2},\operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2,\frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right]^2 + \right. \\
 & \quad (c+d)(-1+2 m) \operatorname{AppellF1}\left[\frac{3}{2},\frac{3}{2}-m,-\frac{1}{2},\frac{5}{2},\operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2, \\
 & \quad \left. \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) + \\
 & \left( 3 B d(c+d) \operatorname{AppellF1}\left[\frac{1}{2},\frac{1}{2}-m,-\frac{1}{2},\frac{3}{2},\operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2,\right. \\
 & \quad \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\left.] \operatorname{Cos}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^{-1+2 m}\right. \\
 & \quad \left(\operatorname{Cos}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{\frac{1}{2}-m} \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right] \\
 & \quad \left. \left(1-\operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{-\frac{1}{2}+m} \sqrt{c+d-2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}\right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( 3 (c+d) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}-m, -\frac{1}{2}, \frac{3}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] - \right. \\
 & \left( 2 d \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2}-m, \frac{1}{2}, \frac{5}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] + \right. \\
 & \quad (c+d) (-1+2m) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2}-m, -\frac{1}{2}, \frac{5}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \\
 & \quad \left. \left. \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \right) \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \\
 & \left( 10 B d (c+d) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2}-m, -\frac{1}{2}, \frac{5}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{1+2m} \right. \\
 & \quad \left( \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{\frac{1}{2}(-1-2m)} \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^3 \\
 & \quad \left. \left( 1 - \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{\frac{1}{2}+m} \sqrt{c+d - 2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2} \right) / \\
 & \left( -5 (c+d) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2}-m, -\frac{1}{2}, \frac{5}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] + \right. \\
 & \left( 2 d \operatorname{AppellF1} \left[ \frac{5}{2}, -\frac{1}{2}-m, \frac{1}{2}, \frac{7}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] + \right. \\
 & \quad (c+d) (1+2m) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{2}-m, -\frac{1}{2}, \frac{7}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \\
 & \quad \left. \left. \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \right) \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \\
 & \left( 10 B c (c+d) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2}-m, -\frac{1}{2}, \frac{5}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{-1+2m} \right. \\
 & \quad \left( \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{\frac{1}{2}(1-2m)} \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^3
 \end{aligned}$$

$$\begin{aligned}
 & \left( 1 - \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right)^{-\frac{1}{2}+m} \sqrt{c+d-2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2} / \\
 & \left( 3 \left( -5 (c+d) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}-m, -\frac{1}{2}, \frac{5}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right], \right. \right. \\
 & \quad \left. \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] + \left( 2 d \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{2}-m, \frac{1}{2}, \frac{7}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right], \right. \right. \\
 & \quad \left. \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] + (c+d) (-1+2 m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{3}{2}-m, -\frac{1}{2}, \frac{7}{2}, \right. \\
 & \quad \left. \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right) \right) + \\
 & \left( 10 A d (c+d) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}-m, -\frac{1}{2}, \frac{5}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right], \right. \\
 & \quad \left. \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] \operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^{-1+2 m} \right. \\
 & \quad \left. \left( \operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right)^{\frac{1}{2}(1-2 m)} \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^3 \right. \\
 & \quad \left. \left( 1 - \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right)^{-\frac{1}{2}+m} \sqrt{c+d-2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2} / \right. \\
 & \quad \left( 3 \left( -5 (c+d) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}-m, -\frac{1}{2}, \frac{5}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right], \right. \right. \\
 & \quad \left. \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] + \left( 2 d \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{2}-m, \frac{1}{2}, \frac{7}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right], \right. \right. \\
 & \quad \left. \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] + (c+d) (-1+2 m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{3}{2}-m, -\frac{1}{2}, \frac{7}{2}, \right. \\
 & \quad \left. \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right) \right) - \\
 & \left( 7 B d (c+d) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{2}-m, -\frac{1}{2}, \frac{7}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right], \right. \\
 & \quad \left. \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] \operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^{-1+2 m} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \cos \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{\frac{1}{2}(1-2m)} \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^5 \\
 & \left( 1 - \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{-\frac{1}{2}+m} \sqrt{c+d-2d \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2} \right) / \\
 & \left( 5 \left( -7(c+d) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{2}-m, -\frac{1}{2}, \frac{7}{2}, \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{2d \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \right) + \right. \\
 & \quad \left( 2d \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{1}{2}-m, \frac{1}{2}, \frac{9}{2}, \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2d \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \right) + \right. \\
 & \quad \left. (c+d)(-1+2m) \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{3}{2}-m, -\frac{1}{2}, \frac{9}{2}, \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{2d \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \right) \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \left. \right) \left( a + a \sin[e + f x] \right)^m
 \end{aligned}$$

### Problem 343: Result more than twice size of optimal antiderivative.

$$\int (a + a \sin[e + f x])^m (A + B \sin[e + f x]) \sqrt{c + d \sin[e + f x]} dx$$

Optimal (type 6, 274 leaves, 9 steps):

$$\begin{aligned}
 & \left( \sqrt{2} (A - B) \operatorname{AppellF1} \left[ \frac{1}{2} + m, \frac{1}{2}, -\frac{1}{2}, \frac{3}{2} + m, \frac{1}{2} (1 + \sin[e + f x]), -\frac{d(1 + \sin[e + f x])}{c-d} \right] \right. \\
 & \quad \left. \cos[e + f x] (a + a \sin[e + f x])^m \sqrt{c + d \sin[e + f x]} \right) / \\
 & \left( f(1+2m) \sqrt{1 - \sin[e + f x]} \sqrt{\frac{c + d \sin[e + f x]}{c - d}} \right) + \\
 & \left( \sqrt{2} B \operatorname{AppellF1} \left[ \frac{3}{2} + m, \frac{1}{2}, -\frac{1}{2}, \frac{5}{2} + m, \frac{1}{2} (1 + \sin[e + f x]), -\frac{d(1 + \sin[e + f x])}{c-d} \right] \right. \\
 & \quad \left. \cos[e + f x] (a + a \sin[e + f x])^{1+m} \sqrt{c + d \sin[e + f x]} \right) / \\
 & \left( a f (3 + 2m) \sqrt{1 - \sin[e + f x]} \sqrt{\frac{c + d \sin[e + f x]}{c - d}} \right)
 \end{aligned}$$

Result (type 6, 1364 leaves):

$$-\frac{1}{f} \cos \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{-2m}$$

$$\begin{aligned}
 & \left( \left( 6 A (c+d) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}-m, -\frac{1}{2}, \frac{3}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \right. \right. \\
 & \quad \left. \left. \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{-1+2m} \left( \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{\frac{1}{2}-m} \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right] \right. \right. \\
 & \quad \left. \left. \left( 1 - \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{-\frac{1}{2}+m} \sqrt{c+d - 2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2} \right) / \right. \\
 & \quad \left. \left( 3 (c+d) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}-m, -\frac{1}{2}, \frac{3}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \right) - \right. \\
 & \quad \left. \left( 2 d \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2}-m, \frac{1}{2}, \frac{5}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \right) + \right. \\
 & \quad \left. \left( (c+d) (-1+2m) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2}-m, -\frac{1}{2}, \frac{5}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \right) \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) + \\
 & \quad \left. \left( \left( 6 (c+d) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}-m, -\frac{3}{2}, \frac{3}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{-1+2m} \right. \right. \right. \\
 & \quad \left. \left. \left. \left( \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{\frac{1}{2}-m} \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right] \left( 1 - \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{\frac{1}{2}+m} \right. \right. \right. \\
 & \quad \left. \left. \left. \left( c+d - 2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{3/2} \right) / \left( d \left( -3 (c+d) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}-m, -\frac{3}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{3}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \right) + \left( 6 d \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{1}{2}-m, -\frac{1}{2}, \frac{5}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \right) + \right. \\
 & \quad \left. \left( (c+d) (-1+2m) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2}-m, -\frac{3}{2}, \frac{5}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \right) \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \right) \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left( 6 c (c+d) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}-m, -\frac{1}{2}, \frac{3}{2}, \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \frac{2 d \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \cos \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{-1+2m} \right. \\
 & \quad \left. \left( \cos \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{\frac{1}{2}-m} \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right] \right. \\
 & \quad \left. \left( 1 - \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{-\frac{1}{2}+m} \sqrt{c+d - 2 d \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2} \right) / \\
 & \left( d \left( 3 (c+d) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}-m, -\frac{1}{2}, \frac{3}{2}, \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \frac{2 d \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] - \left( 2 d \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2}-m, \frac{1}{2}, \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] + \right. \\
 & \quad \left. (c+d) (-1+2m) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2}-m, -\frac{1}{2}, \frac{5}{2}, \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{2 d \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \right) \left( a + a \sin [e + f x] \right)^m
 \end{aligned}$$

**Problem 344: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sin [e + f x])^m (A + B \sin [e + f x])}{\sqrt{c + d \sin [e + f x]}} dx$$

Optimal (type 6, 274 leaves, 9 steps):

$$\left( \sqrt{2} (A - B) \operatorname{AppellF1} \left[ \frac{1}{2} + m, \frac{1}{2}, \frac{1}{2}, \frac{3}{2} + m, \frac{1}{2} (1 + \sin[e + f x]), -\frac{d(1 + \sin[e + f x])}{c - d} \right] \right. \\ \left. \cos[e + f x] (a + a \sin[e + f x])^m \sqrt{\frac{c + d \sin[e + f x]}{c - d}} \right) / \\ \left( f (1 + 2m) \sqrt{1 - \sin[e + f x]} \sqrt{c + d \sin[e + f x]} \right) + \\ \left( \sqrt{2} B \operatorname{AppellF1} \left[ \frac{3}{2} + m, \frac{1}{2}, \frac{1}{2}, \frac{5}{2} + m, \frac{1}{2} (1 + \sin[e + f x]), -\frac{d(1 + \sin[e + f x])}{c - d} \right] \right. \\ \left. \cos[e + f x] (a + a \sin[e + f x])^{1+m} \sqrt{\frac{c + d \sin[e + f x]}{c - d}} \right) / \\ \left( a f (3 + 2m) \sqrt{1 - \sin[e + f x]} \sqrt{c + d \sin[e + f x]} \right)$$

Result(type 6, 1363 leaves):

$$-\frac{1}{f} \cos \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{-2m} \\ \left( - \left( \left( 6 A (c + d) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} - m, \frac{1}{2}, \frac{3}{2}, \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c + d} \right] \right)^2 \right. \right. \\ \left. \cos \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{-1+2m} \left( \cos \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{\frac{1}{2}-m} \right. \\ \left. \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right] \left( 1 - \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{-\frac{1}{2}+m} \right) / \\ \left( \sqrt{c + d - 2 d \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2} \left( -3 (c + d) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} - m, \frac{1}{2}, \frac{3}{2}, \right. \right. \right. \\ \left. \left. \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c + d} \right] \right) + \left( -2 d \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \right. \\ \left. \left. \frac{1}{2} - m, \frac{3}{2}, \frac{5}{2}, \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c + d} \right] \right) + \\ \left. \left. (c + d) (-1 + 2m) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} - m, \frac{1}{2}, \frac{5}{2}, \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\ \left. \left. \frac{2 d \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c + d} \right] \right) \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) +$$



$$\begin{aligned}
 & B \left( \left( 6 (c+d) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}-m, -\frac{1}{2}, \frac{3}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \right. \right. \\
 & \quad \left. \left. \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{-1+2m} \left( \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{\frac{1}{2}-m} \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right] \right. \right. \\
 & \quad \left. \left. \left( 1 - \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{-\frac{1}{2}+m} \sqrt{c+d - 2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2} \right) / \right. \\
 & \quad \left( d \left( 3 (c+d) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}-m, -\frac{1}{2}, \frac{3}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] - \left( 2 d \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2}-m, \frac{1}{2}, \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] + \right. \right. \\
 & \quad \left. \left. (c+d) (-1+2m) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2}-m, -\frac{1}{2}, \frac{5}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) + \right. \\
 & \quad \left( 6 c (c+d) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}-m, \frac{1}{2}, \frac{3}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{-1+2m} \left( \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{\frac{1}{2}-m} \right. \right. \\
 & \quad \left. \left. \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right] \left( 1 - \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{-\frac{1}{2}+m} \right) / \right. \\
 & \quad \left( d \sqrt{c+d - 2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2} \left( -3 (c+d) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}-m, \frac{1}{2}, \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] + \left( -2 d \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \frac{1}{2}-m, \frac{3}{2}, \frac{5}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c+d} \right] + \right. \right. \\
 & \quad \left. \left. (c+d) (-1+2m) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2}-m, \frac{1}{2}, \frac{5}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left. \frac{1}{2} - m, \frac{5}{2}, \frac{5}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] + \\
 & \left. (c+d) (-1+2m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{3}{2}-m, \frac{3}{2}, \frac{5}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \left. \left. \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)\right) + \\
 \mathbf{B} & \left( - \left( \left( 6 (c+d) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}-m, \frac{1}{2}, \frac{3}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \right. \right. \\
 & \left. \left. \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] \operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^{-1+2m} \left(\operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^{\frac{1}{2}-m} \right. \right. \\
 & \left. \left. \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right] \left(1 - \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^{-\frac{1}{2}+m} \right) \right) / \\
 & \left( d \sqrt{c+d - 2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2} \left( -3 (c+d) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}-m, \frac{1}{2}, \frac{3}{2}, \right. \right. \right. \\
 & \left. \left. \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] + \left( -2 d \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \left. \left. \frac{1}{2}-m, \frac{3}{2}, \frac{5}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] + \right. \right. \\
 & \left. \left. (c+d) (-1+2m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{3}{2}-m, \frac{1}{2}, \frac{5}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right)\right) + \\
 & \left( 6 c (c+d) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}-m, \frac{3}{2}, \frac{3}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \left. \left. \frac{2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] \operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^{-1+2m} \left(\operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^{\frac{1}{2}-m} \right. \right. \\
 & \left. \left. \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right] \left(1 - \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^{-\frac{1}{2}+m} \right) \right) / \\
 & \left( d \left( c+d - 2 d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right)^{3/2} \left( -3 (c+d) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}-m, \frac{3}{2}, \right. \right. \right. \right.
 \end{aligned}$$

$$\frac{3}{2}, \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \frac{2d \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d} \left[ -6d \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2} - m, \frac{5}{2}, \frac{5}{2}, \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \frac{2d \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] + (c+d)(-1+2m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{3}{2} - m, \frac{3}{2}, \frac{5}{2}, \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \frac{2d \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] \right] \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \right] \right] (a + a \sin[e + fx])^m$$

**Problem 346: Result more than twice size of optimal antiderivative.**

$$\int (a + a \sin[e + fx])^m (A + B \sin[e + fx]) (c + d \sin[e + fx])^n dx$$

Optimal (type 6, 270 leaves, 9 steps):

$$\left( \sqrt{2} (A - B) \operatorname{AppellF1}\left[\frac{1}{2} + m, \frac{1}{2}, -n, \frac{3}{2} + m, \frac{1}{2} (1 + \sin[e + fx]), -\frac{d(1 + \sin[e + fx])}{c - d}\right] \right. \\ \left. \cos[e + fx] (a + a \sin[e + fx])^m (c + d \sin[e + fx])^n \left(\frac{c + d \sin[e + fx]}{c - d}\right)^{-n} \right] / \left( f(1 + 2m) \sqrt{1 - \sin[e + fx]} \right) + \\ \left( \sqrt{2} B \operatorname{AppellF1}\left[\frac{3}{2} + m, \frac{1}{2}, -n, \frac{5}{2} + m, \frac{1}{2} (1 + \sin[e + fx]), -\frac{d(1 + \sin[e + fx])}{c - d}\right] \right. \\ \left. \cos[e + fx] (a + a \sin[e + fx])^{1+m} (c + d \sin[e + fx])^n \left(\frac{c + d \sin[e + fx]}{c - d}\right)^{-n} \right] / \left( a f(3 + 2m) \sqrt{1 - \sin[e + fx]} \right)$$

Result (type 6, 1375 leaves):

$$-\frac{1}{f} \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^{-2m} \\ \left( \left( 6A(c+d) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2} - m, -n, \frac{3}{2}, \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \frac{2d \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] \right. \right. \\ \left. \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^{-1+2m} \left(\cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{\frac{1}{2}-m} \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \right. \\ \left. \left(1 - \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{-\frac{1}{2}+m} \left(c + d - 2d \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^n \right) / \\ \left( 3(c+d) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2} - m, -n, \frac{3}{2}, \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \frac{2d \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] \right) -$$

$$\begin{aligned}
 & \left( 4 d n \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} - m, 1 - n, \frac{5}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c + d} \right]^2 + \right. \\
 & \quad (c + d) (-1 + 2 m) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} - m, -n, \frac{5}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \\
 & \quad \left. \left. \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c + d} \right] \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \\
 B & \left( - \left( \left( 6 (c + d) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} - m, -1 - n, \frac{3}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c + d} \right] \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{-1+2m} \right. \\
 & \quad \left. \left( \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{\frac{1}{2}-m} \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right] \left( 1 - \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{\frac{1}{2}+m} \right. \\
 & \quad \left. \left( c + d - 2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{1+n} \right) / \left( d \left( -3 (c + d) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} - m, -1 - n, \right. \right. \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c + d} \right] + \left( 4 d (1 + n) \operatorname{AppellF1} \left[ \right. \right. \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, \frac{1}{2} - m, -n, \frac{5}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c + d} \right] \right) + \right. \\
 & \quad \left. (c + d) (-1 + 2 m) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} - m, -1 - n, \frac{5}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c + d} \right] \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) - \left( 6 c (c + d) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} - m, -n, \frac{3}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c + d} \right] \right) \\
 & \quad \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^{-1+2m} \left( \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{\frac{1}{2}-m} \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right] \\
 & \quad \left. \left( 1 - \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{-\frac{1}{2}+m} \left( c + d - 2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 \right)^n \right) / \\
 & \quad \left( d \left( 3 (c + d) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} - m, -n, \frac{3}{2}, \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \frac{2 d \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{c + d} \right] - \left( 4 d n \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} - m, 1 - n, \right. \right. \right. \right.
 \end{aligned}$$

$$\frac{5}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \frac{2d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d} +$$

$$(c+d) (-1+2m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{3}{2}-m, -n, \frac{5}{2}, \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \frac{2d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \left(a + a \operatorname{Sin}[e + fx]\right)^m$$

**Problem 347: Result more than twice size of optimal antiderivative.**

$$\int (a + a \operatorname{Sin}[e + fx])^m (A + B \operatorname{Sin}[e + fx]) (c + d \operatorname{Sin}[e + fx])^{-1-m} dx$$

Optimal (type 6, 277 leaves, 7 steps):

$$-\frac{1}{(c+d)f} 2^{\frac{1}{2}+m} a (A-B) \operatorname{Cos}[e + fx] \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{2}-m, \frac{3}{2}, \frac{(c-d)(1-\operatorname{Sin}[e + fx])}{2(c+d \operatorname{Sin}[e + fx])}\right]$$

$$(a + a \operatorname{Sin}[e + fx])^{-1+m} \left(\frac{(c+d)(1+\operatorname{Sin}[e + fx])}{c+d \operatorname{Sin}[e + fx]}\right)^{\frac{1}{2}-m} (c+d \operatorname{Sin}[e + fx])^{-m} +$$

$$\left(\sqrt{2} B \operatorname{AppellF1}\left[\frac{3}{2}+m, \frac{1}{2}, 1+m, \frac{5}{2}+m, \frac{1}{2}(1+\operatorname{Sin}[e + fx]), -\frac{d(1+\operatorname{Sin}[e + fx])}{c-d}\right] \operatorname{Cos}[e + fx] (a + a \operatorname{Sin}[e + fx])^{1+m} (c+d \operatorname{Sin}[e + fx])^{-m} \left(\frac{c+d \operatorname{Sin}[e + fx]}{c-d}\right)^m\right) /$$

$$(a(c-d)f(3+2m)\sqrt{1-\operatorname{Sin}[e + fx]})$$

Result (type 6, 1020 leaves):

$$-\frac{1}{f} \operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^{-2m} \left(\frac{1}{c+d} 2 A \operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^{-1+2m} \left(\operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{\frac{1}{2}-m} \right.$$

$$\operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{2}-m, \frac{3}{2}, \frac{(c-d) \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d-2d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}\right]$$

$$\operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \left(1 - \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{-\frac{1}{2}+m}$$

$$\left(-\frac{(c+d)\left(-1 + \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)}{c+d-2d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}\right)^{\frac{1}{2}-m} \left(c+d-2d \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{-m} +$$

$$B \left(-\frac{1}{d(c+d)} 2 c \operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^{-1+2m} \left(\operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{\frac{1}{2}-m} \right.$$

$$\begin{aligned}
 & \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{2} - m, \frac{3}{2}, \frac{(c-d) \sin\left[\frac{1}{2}(-e + \frac{\pi}{2} - fx)\right]^2}{c+d-2d \sin\left[\frac{1}{2}(-e + \frac{\pi}{2} - fx)\right]^2}\right] \\
 & \sin\left[\frac{1}{2}(-e + \frac{\pi}{2} - fx)\right] \left(1 - \sin\left[\frac{1}{2}(-e + \frac{\pi}{2} - fx)\right]^2\right)^{-\frac{1}{2}+m} \\
 & \left(-\frac{(c+d) \left(-1 + \sin\left[\frac{1}{2}(-e + \frac{\pi}{2} - fx)\right]^2\right)}{c+d-2d \sin\left[\frac{1}{2}(-e + \frac{\pi}{2} - fx)\right]^2}\right)^{\frac{1}{2}-m} \left(c+d-2d \sin\left[\frac{1}{2}(-e + \frac{\pi}{2} - fx)\right]^2\right)^{-m} + \\
 & \left(6(c+d) \text{AppellF1}\left[\frac{1}{2}, \frac{1}{2} - m, m, \frac{3}{2}, \sin\left[\frac{1}{2}(-e + \frac{\pi}{2} - fx)\right]^2, \frac{2d \sin\left[\frac{1}{2}(-e + \frac{\pi}{2} - fx)\right]^2}{c+d}\right]^2\right. \\
 & \cos\left[\frac{1}{2}(-e + \frac{\pi}{2} - fx)\right]^{-1+2m} \left(\cos\left[\frac{1}{2}(-e + \frac{\pi}{2} - fx)\right]^2\right)^{\frac{1}{2}-m} \sin\left[\frac{1}{2}(-e + \frac{\pi}{2} - fx)\right] \\
 & \left. \left(1 - \sin\left[\frac{1}{2}(-e + \frac{\pi}{2} - fx)\right]^2\right)^{-\frac{1}{2}+m} \left(c+d-2d \sin\left[\frac{1}{2}(-e + \frac{\pi}{2} - fx)\right]^2\right)^{-m}\right) / \\
 & \left(d \left(3(c+d) \text{AppellF1}\left[\frac{1}{2}, \frac{1}{2} - m, m, \frac{3}{2}, \sin\left[\frac{1}{2}(-e + \frac{\pi}{2} - fx)\right]^2, \right. \right. \right. \\
 & \left. \left. \frac{2d \sin\left[\frac{1}{2}(-e + \frac{\pi}{2} - fx)\right]^2}{c+d}\right] - \left(-4dm \text{AppellF1}\left[\frac{3}{2}, \frac{1}{2} - m, 1+m, \right. \right. \right. \\
 & \left. \left. \frac{5}{2}, \sin\left[\frac{1}{2}(-e + \frac{\pi}{2} - fx)\right]^2, \frac{2d \sin\left[\frac{1}{2}(-e + \frac{\pi}{2} - fx)\right]^2}{c+d}\right] + \right. \right. \\
 & \left. \left. (c+d) (-1+2m) \text{AppellF1}\left[\frac{3}{2}, \frac{3}{2} - m, m, \frac{5}{2}, \sin\left[\frac{1}{2}(-e + \frac{\pi}{2} - fx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{2d \sin\left[\frac{1}{2}(-e + \frac{\pi}{2} - fx)\right]^2}{c+d}\right] \sin\left[\frac{1}{2}(-e + \frac{\pi}{2} - fx)\right]^2\right)\right)\right) \right) \right) (a + a \sin[e + fx])^m
 \end{aligned}$$

### Problem 348: Unable to integrate problem.

$$\int (a - a \sin[e + fx]) (a + a \sin[e + fx])^m (c + d \sin[e + fx])^n dx$$

Optimal (type 6, 132 leaves, 4 steps):

$$\frac{1}{f(1+2m)} 2\sqrt{2} \text{AppellF1}\left[\frac{1}{2} + m, -\frac{1}{2}, -n, \frac{3}{2} + m, \frac{1}{2}(1 + \sin[e + fx]), -\frac{d(1 + \sin[e + fx])}{c-d}\right] \\
 \sec[e + fx] \sqrt{1 - \sin[e + fx]} (a + a \sin[e + fx])^{1+m} (c + d \sin[e + fx])^n \left(\frac{c + d \sin[e + fx]}{c-d}\right)^{-n}$$

Result (type 8, 38 leaves):

$$\int (a - a \sin[e + f x]) (a + a \sin[e + f x])^m (c + d \sin[e + f x])^n dx$$

**Problem 349: Unable to integrate problem.**

$$\int (a - a \sin[e + f x]) (a + a \sin[e + f x])^m (c + d \sin[e + f x])^{-1-m} dx$$

Optimal (type 6, 139 leaves, 4 steps):

$$\left( 2 \sqrt{2} \operatorname{AppellF1} \left[ \frac{1}{2} + m, -\frac{1}{2}, 1 + m, \frac{3}{2} + m, \frac{1}{2} (1 + \sin[e + f x]), -\frac{d (1 + \sin[e + f x])}{c - d} \right] \right. \\ \left. \operatorname{Sec}[e + f x] \sqrt{1 - \sin[e + f x]} (a + a \sin[e + f x])^{1+m} \right. \\ \left. (c + d \sin[e + f x])^{-m} \left( \frac{c + d \sin[e + f x]}{c - d} \right)^m \right] / ((c - d) f (1 + 2 m))$$

Result (type 8, 42 leaves):

$$\int (a - a \sin[e + f x]) (a + a \sin[e + f x])^m (c + d \sin[e + f x])^{-1-m} dx$$

**Problem 353: Result more than twice size of optimal antiderivative.**

$$\int \frac{(A + B \sin[e + f x]) (c + d \sin[e + f x])^{3/2}}{(a + b \sin[e + f x])^{3/2}} dx$$

Optimal (type 4, 840 leaves, 7 steps):



$$\begin{aligned}
 & \left( (c-d) \sqrt{c+d} (2Ab^2c - 2abBc - 2aAbd + 3a^2Bd - b^2Bd) \right. \\
 & \quad \text{EllipticE} \left[ \text{ArcSin} \left[ \frac{\sqrt{a+b} \sqrt{c+d} \sin[e+fx]}{\sqrt{c+d} \sqrt{a+b \sin[e+fx]}} \right], \frac{(a-b)(c+d)}{(a+b)(c-d)} \right] \text{Sec}[e+fx] \\
 & \quad \left. \sqrt{-\frac{(bc-ad)(1-\sin[e+fx])}{(c+d)(a+b \sin[e+fx])}} \sqrt{\frac{(bc-ad)(1+\sin[e+fx])}{(c-d)(a+b \sin[e+fx])}} (a+b \sin[e+fx]) \right) / \\
 & \quad \left( (a-b) b^2 \sqrt{a+b} (bc-ad) f \right) + \frac{1}{b^3 \sqrt{a+b} f} \sqrt{c+d} (3bBc + 2Abd - 3aBd) \\
 & \quad \text{EllipticPi} \left[ \frac{b(c+d)}{(a+b)d}, \text{ArcSin} \left[ \frac{\sqrt{a+b} \sqrt{c+d} \sin[e+fx]}{\sqrt{c+d} \sqrt{a+b \sin[e+fx]}} \right], \frac{(a-b)(c+d)}{(a+b)(c-d)} \right] \text{Sec}[e+fx] \\
 & \quad \sqrt{-\frac{(bc-ad)(1-\sin[e+fx])}{(c+d)(a+b \sin[e+fx])}} \sqrt{\frac{(bc-ad)(1+\sin[e+fx])}{(c-d)(a+b \sin[e+fx])}} (a+b \sin[e+fx]) + \\
 & \quad \frac{2(Ab-aB)(bc-ad) \cos[e+fx] \sqrt{c+d} \sin[e+fx]}{b(a^2-b^2) f \sqrt{a+b \sin[e+fx]}} - \\
 & \quad \left( (2Ab(bc-ad) - B(2abc - 3a^2d + b^2d)) \cos[e+fx] \sqrt{c+d} \sin[e+fx] \right) / \\
 & \quad \left( b(a^2-b^2) f \sqrt{a+b \sin[e+fx]} \right) + \\
 & \quad \left( \sqrt{a+b} (2Ab(b(c-2d) + ad) - B(3a^2d - 6abd + b^2(2c+d))) \right) \\
 & \quad \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\sqrt{c+d} \sqrt{a+b \sin[e+fx]}}{\sqrt{a+b} \sqrt{c+d \sin[e+fx]}} \right], \frac{(a+b)(c-d)}{(a-b)(c+d)} \right] \\
 & \quad \text{Sec}[e+fx] \sqrt{\frac{(bc-ad)(1-\sin[e+fx])}{(a+b)(c+d \sin[e+fx])}} \\
 & \quad \left. \sqrt{-\frac{(bc-ad)(1+\sin[e+fx])}{(a-b)(c+d \sin[e+fx])}} (c+d \sin[e+fx]) \right) / \left( (a-b) b^3 \sqrt{c+d} f \right)
 \end{aligned}$$

Result (type 4, 2012 leaves):

$$\begin{aligned}
 & - \left( \left( 2(Ab^2c \cos[e+fx] - abBc \cos[e+fx] - aAbd \cos[e+fx] + a^2Bd \cos[e+fx]) \right. \right. \\
 & \quad \left. \left. \sqrt{c+d \sin[e+fx]} \right) / \left( b(-a^2+b^2) f \sqrt{a+b \sin[e+fx]} \right) \right) + \\
 & \quad \frac{1}{2(a-b)b(a+b)f} \left( \left( \left( 4(-bc+ad)(2aAbc^2 - 2b^2Bc^2 - 2Ab^2cd + 2abBcd + a^2Bd^2 - b^2Bd^2) \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{(c+d) \operatorname{Cot}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{-c+d}} \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \operatorname{Sin}[e+fx])}{-bc+ad}}}{\sqrt{2}}}\right], \frac{2(-bc+ad)}{(a+b)(-c+d)}\right] \\
 & \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^4 \sqrt{\frac{(c+d) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (a+b \operatorname{Sin}[e+fx])}{-bc+ad}} \\
 & \left. \sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \operatorname{Sin}[e+fx])}{-bc+ad}} \right) / \\
 & \left. \left( (a+b)(c+d) \sqrt{a+b \operatorname{Sin}[e+fx]} \sqrt{c+d \operatorname{Sin}[e+fx]} \right) - \right. \\
 & 4(-bc+ad) (2Ab^2c^2 - 2abBc^2 + 4a^2Bcd - 4b^2Bcd - 2Ab^2d^2 + 2abBd^2) \\
 & \left( \left( \sqrt{\frac{(c+d) \operatorname{Cot}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{-c+d}} \operatorname{EllipticF}\left[ \right. \right. \right. \\
 & \left. \left. \left. \operatorname{ArcSin}\left[\frac{\sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \operatorname{Sin}[e+fx])}{-bc+ad}}}{\sqrt{2}}}\right], \frac{2(-bc+ad)}{(a+b)(-c+d)}\right] \operatorname{Sec}[e+fx] \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^4 \sqrt{\frac{(c+d) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (a+b \operatorname{Sin}[e+fx])}{-bc+ad}} \right. \right. \right. \\
 & \left. \left. \left. \sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \operatorname{Sin}[e+fx])}{-bc+ad}} \right) / \right. \right. \right. \\
 & \left. \left. \left. \left( (a+b)(c+d) \sqrt{a+b \operatorname{Sin}[e+fx]} \sqrt{c+d \operatorname{Sin}[e+fx]} \right) - \right. \right. \right. \\
 & \left. \left( \sqrt{\frac{(c+d) \operatorname{Cot}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{-c+d}} \operatorname{EllipticPi}\left[\frac{-bc+ad}{(a+b)d}, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \text{ArcSin} \left[ \frac{\sqrt{-\frac{(a+b) \operatorname{Csc} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 (c+d \operatorname{Sin}[e+f x])}{-b c+a d}}}{\sqrt{2}}} \right], \frac{2(-b c+a d)}{(a+b)(-c+d)} \operatorname{Sec}[e+f x] \\
 & \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^4 \sqrt{\frac{(c+d) \operatorname{Csc} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 (a+b \operatorname{Sin}[e+f x])}{-b c+a d}} \\
 & \left. \sqrt{-\frac{(a+b) \operatorname{Csc} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 (c+d \operatorname{Sin}[e+f x])}{-b c+a d}} \right) / \\
 & \left. \left( (a+b) d \sqrt{a+b \operatorname{Sin}[e+f x]} \sqrt{c+d \operatorname{Sin}[e+f x]} \right) + \right. \\
 & 2(-2 A b^2 c d+2 a b B c d+2 a A b d^2-3 a^2 B d^2+b^2 B d^2) \\
 & \left( \frac{\operatorname{Cos}[e+f x] \sqrt{c+d \operatorname{Sin}[e+f x]}}{d \sqrt{a+b \operatorname{Sin}[e+f x]}} + \right. \\
 & \left. \left( \sqrt{\frac{a-b}{a+b}} (a+b) \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right] \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{a-b}{a+b}} \operatorname{Sin} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]}{\sqrt{\frac{a+b \operatorname{Sin}[e+f x]}{a+b}}}} \right], \right. \right. \\
 & \left. \left. \frac{2(-b c+a d)}{(a-b)(c+d)} \sqrt{c+d \operatorname{Sin}[e+f x]} \right) / \left( b d \sqrt{\frac{(a+b) \operatorname{Cos} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{a+b \operatorname{Sin}[e+f x]}} \right. \right. \\
 & \left. \left. \sqrt{a+b \operatorname{Sin}[e+f x]} \sqrt{\frac{a+b \operatorname{Sin}[e+f x]}{a+b}} \sqrt{\frac{(a+b)(c+d \operatorname{Sin}[e+f x])}{(c+d)(a+b \operatorname{Sin}[e+f x])}} \right) - \right. \\
 & \left. \frac{1}{b d} 2(-b c+a d) \left( \left( (a+b) c+a d \right) \sqrt{\frac{(c+d) \operatorname{Cot} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{-c+d}} \operatorname{EllipticF} \left[ \right. \right. \right.
 \end{aligned}$$



$$\left( 2 (A b - a B) (c - d) \sqrt{c + d} \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b} \sqrt{c + d} \sin[e + f x]}{\sqrt{c + d} \sqrt{a + b \sin[e + f x]}} \right], \frac{(a - b) (c + d)}{(a + b) (c - d)} \right] \right.$$

$$\operatorname{Sec}[e + f x] \sqrt{-\frac{(b c - a d) (1 - \sin[e + f x])}{(c + d) (a + b \sin[e + f x])}} \sqrt{\frac{(b c - a d) (1 + \sin[e + f x])}{(c - d) (a + b \sin[e + f x])}}$$

$$\left. (a + b \sin[e + f x]) \right) / \left( (a - b) b \sqrt{a + b} (b c - a d) f \right) +$$

$$\left( 2 \sqrt{a + b} (A b - a B) (c - d) \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{c + d} \sqrt{a + b \sin[e + f x]}}{\sqrt{a + b} \sqrt{c + d \sin[e + f x]}} \right], \frac{(a + b) (c - d)}{(a - b) (c + d)} \right] \right.$$

$$\operatorname{Sec}[e + f x] \sqrt{\frac{(b c - a d) (1 - \sin[e + f x])}{(a + b) (c + d \sin[e + f x])}} \sqrt{-\frac{(b c - a d) (1 + \sin[e + f x])}{(a - b) (c + d \sin[e + f x])}}$$

$$\left. (c + d \sin[e + f x]) \right) / \left( (a - b) b \sqrt{c + d} (b c - a d) f \right) + \frac{1}{b^2 \sqrt{c + d} f}$$

$$2 \sqrt{a + b} B \operatorname{EllipticPi} \left[ \frac{(a + b) d}{b (c + d)}, \operatorname{ArcSin} \left[ \frac{\sqrt{c + d} \sqrt{a + b \sin[e + f x]}}{\sqrt{a + b} \sqrt{c + d \sin[e + f x]}} \right], \frac{(a + b) (c - d)}{(a - b) (c + d)} \right]$$

$$\operatorname{Sec}[e + f x] \sqrt{\frac{(b c - a d) (1 - \sin[e + f x])}{(a + b) (c + d \sin[e + f x])}}$$

$$\sqrt{-\frac{(b c - a d) (1 + \sin[e + f x])}{(a - b) (c + d \sin[e + f x])}} (c + d \sin[e + f x])$$

Result (type 4, 1871 leaves):

$$\frac{2 (-A b \cos[e + f x] + a B \cos[e + f x]) \sqrt{c + d \sin[e + f x]}}{(a^2 - b^2) f \sqrt{a + b \sin[e + f x]}} +$$

$$\frac{1}{(a - b) (a + b) f} \left( \left( \left( 4 (a A c - b B c) (-b c + a d) \sqrt{\frac{(c + d) \operatorname{Cot} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{-c + d}} \right. \right. \right.$$

$$\left. \left. \left. \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{-\frac{(a + b) \operatorname{Csc} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 (c + d \sin[e + f x])}{-b c + a d}}}{\sqrt{2}} \right], \frac{2 (-b c + a d)}{(a + b) (-c + d)} \right] \right. \right. \right.$$

$$\left. \left. \left. \operatorname{Sec}[e + f x] \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^4 \sqrt{\frac{(c + d) \operatorname{Csc} \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 (a + b \sin[e + f x])}{-b c + a d}} \right. \right. \right.$$

$$\begin{aligned}
 & \left. \sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \operatorname{Sin}[e+fx])}{-bc+ad}}}\right) / \\
 & \left. \left( (a+b)(c+d) \sqrt{a+b \operatorname{Sin}[e+fx]} \sqrt{c+d \operatorname{Sin}[e+fx]} \right) - \right. \\
 & 4(-bc+ad)(Abc-aBc+aAd-bBd) \left( \left( \sqrt{\frac{(c+d) \operatorname{Cot}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{-c+d}} \operatorname{EllipticF}\left[ \right. \right. \right. \\
 & \left. \left. \left. \operatorname{ArcSin}\left[\frac{\sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \operatorname{Sin}[e+fx])}{-bc+ad}}}}{\sqrt{2}}}\right], \frac{2(-bc+ad)}{(a+b)(-c+d)} \right] \operatorname{Sec}[e+fx] \right. \right. \\
 & \left. \left. \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^4 \sqrt{\frac{(c+d) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (a+b \operatorname{Sin}[e+fx])}{-bc+ad}} \right. \right. \\
 & \left. \left. \left. \sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \operatorname{Sin}[e+fx])}{-bc+ad}}}\right) / \right. \right. \\
 & \left. \left. \left( (a+b)(c+d) \sqrt{a+b \operatorname{Sin}[e+fx]} \sqrt{c+d \operatorname{Sin}[e+fx]} \right) - \right. \right. \\
 & \left. \left. \left( \sqrt{\frac{(c+d) \operatorname{Cot}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{-c+d}} \operatorname{EllipticPi}\left[\frac{-bc+ad}{(a+b)d}, \right. \right. \right. \right. \\
 & \left. \left. \left. \operatorname{ArcSin}\left[\frac{\sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \operatorname{Sin}[e+fx])}{-bc+ad}}}}{\sqrt{2}}}\right], \frac{2(-bc+ad)}{(a+b)(-c+d)} \right] \operatorname{Sec}[e+fx] \right. \right. \\
 & \left. \left. \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^4 \sqrt{\frac{(c+d) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (a+b \operatorname{Sin}[e+fx])}{-bc+ad}} \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \sin[e+fx])}{-bc+ad}} \right) / \\
 & \left. \left( (a+b) d \sqrt{a+b \sin[e+fx]} \sqrt{c+d \sin[e+fx]} \right) + \right. \\
 & 2(-Abd+aBd) \left( \frac{\cos[e+fx] \sqrt{c+d \sin[e+fx]}}{d \sqrt{a+b \sin[e+fx]}} + \right. \\
 & \left. \left( \sqrt{\frac{a-b}{a+b}} (a+b) \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{a-b}{a+b}} \sin\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]}{\sqrt{\frac{a+b \sin[e+fx]}{a+b}}}\right], \right. \right. \\
 & \left. \left. \frac{2(-bc+ad)}{(a-b)(c+d)} \sqrt{c+d \sin[e+fx]} \right) / \left( b d \sqrt{\frac{(a+b) \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{a+b \sin[e+fx]}} \right. \right. \\
 & \left. \left. \sqrt{a+b \sin[e+fx]} \sqrt{\frac{a+b \sin[e+fx]}{a+b}} \sqrt{\frac{(a+b)(c+d \sin[e+fx])}{(c+d)(a+b \sin[e+fx])}} \right) - \right. \\
 & \frac{1}{bd} 2(-bc+ad) \left( \left( (a+b) c+ad \right) \sqrt{\frac{(c+d) \operatorname{Cot}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{-c+d}} \operatorname{EllipticF}\left[ \right. \right. \\
 & \left. \left. \operatorname{ArcSin}\left[\frac{\sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \sin[e+fx])}{-bc+ad}}}{\sqrt{2}}}\right], \frac{2(-bc+ad)}{(a+b)(-c+d)} \right] \operatorname{Sec}[e+fx] \right. \\
 & \left. \left. \sin\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^4 \sqrt{\frac{(c+d) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (a+b \sin[e+fx])}{-bc+ad}} \right) \right.
 \end{aligned}$$

$$\left( \sqrt{\left( -\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \operatorname{Sin}[e+fx])}{-bc+ad} \right)} \right) /$$

$$\left( (a+b) (c+d) \sqrt{a+b \operatorname{Sin}[e+fx]} \sqrt{c+d \operatorname{Sin}[e+fx]} \right) -$$

$$\left( (bc+ad) \sqrt{\frac{(c+d) \operatorname{Cot}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{-c+d}} \operatorname{EllipticPi}\left[\frac{-bc+ad}{(a+b)d}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \operatorname{Sin}[e+fx])}{-bc+ad}}}{\sqrt{2}}}\right], \frac{2(-bc+ad)}{(a+b)(-c+d)} \right] \operatorname{Sec}[e+fx]$$

$$\operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^4 \sqrt{\frac{(c+d) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (a+b \operatorname{Sin}[e+fx])}{-bc+ad}}$$

$$\sqrt{\left( -\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \operatorname{Sin}[e+fx])}{-bc+ad} \right)} /$$

$$\left( (a+b) d \sqrt{a+b \operatorname{Sin}[e+fx]} \sqrt{c+d \operatorname{Sin}[e+fx]} \right) \right)$$

**Problem 355: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Sin}[e + fx]}{(a + b \operatorname{Sin}[e + fx])^{3/2} \sqrt{c + d \operatorname{Sin}[e + fx]}} dx$$

Optimal (type 4, 417 leaves, 3 steps):



$$\left( 2 (A b - a B) (c - d) \sqrt{c + d} \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b} \sqrt{c + d} \sin[e + f x]}{\sqrt{c + d} \sqrt{a + b \sin[e + f x]}} \right], \frac{(a - b) (c + d)}{(a + b) (c - d)} \right] \right.$$

$$\operatorname{Sec}[e + f x] \sqrt{-\frac{(b c - a d) (1 - \sin[e + f x])}{(c + d) (a + b \sin[e + f x])}} \sqrt{\frac{(b c - a d) (1 + \sin[e + f x])}{(c - d) (a + b \sin[e + f x])}}$$

$$\left. (a + b \sin[e + f x]) \right) / \left( (a - b) \sqrt{a + b} (b c - a d)^2 f \right) +$$

$$\left( 2 \sqrt{a + b} (A - B) \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{c + d} \sqrt{a + b \sin[e + f x]}}{\sqrt{a + b} \sqrt{c + d \sin[e + f x]}} \right], \frac{(a + b) (c - d)}{(a - b) (c + d)} \right] \right.$$

$$\operatorname{Sec}[e + f x] \sqrt{\frac{(b c - a d) (1 - \sin[e + f x])}{(a + b) (c + d \sin[e + f x])}} \sqrt{-\frac{(b c - a d) (1 + \sin[e + f x])}{(a - b) (c + d \sin[e + f x])}}$$

$$\left. (c + d \sin[e + f x]) \right) / \left( (a - b) \sqrt{c + d} (b c - a d) f \right)$$

Result (type 4, 1919 leaves):

$$-\frac{2 (A b^2 \cos[e + f x] - a b B \cos[e + f x]) \sqrt{c + d \sin[e + f x]}}{(a^2 - b^2) (-b c + a d) f \sqrt{a + b \sin[e + f x]}} + \frac{1}{(a - b) (a + b) (-b c + a d) f}$$

$$\left( \left( \left( 4 (-b c + a d) (-a A b c + b^2 B c + a^2 A d - A b^2 d) \sqrt{\frac{(c + d) \cot \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2}{-c + d}} \right. \right. \right.$$

$$\operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{-\frac{(a + b) \csc \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 (c + d \sin[e + f x])}{-b c + a d}}}{\sqrt{2}} \right], \frac{2 (-b c + a d)}{(a + b) (-c + d)} \right]$$

$$\operatorname{Sec}[e + f x] \sin \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^4 \sqrt{\frac{(c + d) \csc \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 (a + b \sin[e + f x])}{-b c + a d}}$$

$$\left. \sqrt{-\frac{(a + b) \csc \left[ \frac{1}{2} \left( -e + \frac{\pi}{2} - f x \right) \right]^2 (c + d \sin[e + f x])}{-b c + a d}} \right) /$$

$$\left( (a+b)(c+d) \sqrt{a+b \sin[e+fx]} \sqrt{c+d \sin[e+fx]} \right) -$$

$$4(-bc+ad)(-Ab^2c+abBc-aAbd+a^2Bd) \left( \sqrt{\frac{(c+d) \cot\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{-c+d}} \right)$$

$$\text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{-\frac{(a+b) \csc\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \sin[e+fx])}{-bc+ad}}}{\sqrt{2}}}\right], \frac{2(-bc+ad)}{(a+b)(-c+d)}\right] \text{Sec}[$$

$$e+fx] \sin\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^4 \sqrt{\frac{(c+d) \csc\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (a+b \sin[e+fx])}{-bc+ad}}$$

$$\left. \sqrt{-\frac{(a+b) \csc\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \sin[e+fx])}{-bc+ad}} \right) /$$

$$\left( (a+b)(c+d) \sqrt{a+b \sin[e+fx]} \sqrt{c+d \sin[e+fx]} \right) -$$

$$\left( \sqrt{\frac{(c+d) \cot\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{-c+d}} \text{EllipticPi}\left[\frac{-bc+ad}{(a+b)d}, \right. \right.$$

$$\left. \left. \text{ArcSin}\left[\frac{\sqrt{-\frac{(a+b) \csc\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \sin[e+fx])}{-bc+ad}}}{\sqrt{2}}}\right], \frac{2(-bc+ad)}{(a+b)(-c+d)}\right] \text{Sec}[e+fx] \right.$$

$$\left. \sin\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^4 \sqrt{\frac{(c+d) \csc\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (a+b \sin[e+fx])}{-bc+ad}} \right.$$

$$\left. \left. \sqrt{-\frac{(a+b) \csc\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \sin[e+fx])}{-bc+ad}} \right) / \right.$$

$$\begin{aligned}
 & \left. \left( (a+b) d \sqrt{a+b \sin[e+fx]} \sqrt{c+d \sin[e+fx]} \right) \right) + \\
 & 2 (A b^2 d - a b B d) \left( \frac{\cos[e+fx] \sqrt{c+d \sin[e+fx]}}{d \sqrt{a+b \sin[e+fx]}} + \right. \\
 & \left. \left( \sqrt{\frac{a-b}{a+b}} (a+b) \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{\frac{a-b}{a+b}} \sin\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]}{\sqrt{\frac{a+b \sin[e+fx]}{a+b}}}\right]} \right), \right. \\
 & \left. \frac{2(-bc+ad)}{(a-b)(c+d)} \sqrt{c+d \sin[e+fx]} \right) / \left( b d \sqrt{\frac{(a+b) \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{a+b \sin[e+fx]}} \right. \\
 & \left. \sqrt{a+b \sin[e+fx]} \sqrt{\frac{a+b \sin[e+fx]}{a+b}} \sqrt{\frac{(a+b)(c+d \sin[e+fx])}{(c+d)(a+b \sin[e+fx])}} \right) - \\
 & \frac{1}{bd} 2(-bc+ad) \left( \left( (a+b)c+ad \right) \sqrt{\frac{(c+d) \cot\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{-c+d}} \text{EllipticF}\left[ \right. \right. \\
 & \left. \left. \text{ArcSin}\left[\frac{\sqrt{-\frac{(a+b) \csc\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \sin[e+fx])}{-bc+ad}}}{\sqrt{2}}}\right], \frac{2(-bc+ad)}{(a+b)(-c+d)} \right] \text{Sec}[e+fx] \right. \\
 & \left. \sin\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^4 \sqrt{\frac{(c+d) \csc\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (a+b \sin[e+fx])}{-bc+ad}} \right. \\
 & \left. \left. \sqrt{\left( -\frac{(a+b) \csc\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \sin[e+fx])}{-bc+ad} \right)} \right) / \right. \\
 & \left. \left( (a+b)(c+d) \sqrt{a+b \sin[e+fx]} \sqrt{c+d \sin[e+fx]} \right) - \right.
 \end{aligned}$$

$$\left( (bc + ad) \sqrt{\frac{(c+d) \operatorname{Cot}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{-c+d}} \operatorname{EllipticPi}\left[\frac{-bc+ad}{(a+b)d}, \operatorname{ArcSin}\left[\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 (c+d \operatorname{Sin}[e+fx])}{-bc+ad}}{\sqrt{2}}\right], \frac{2(-bc+ad)}{(a+b)(-c+d)}\right] \operatorname{Sec}[e+fx] \right.$$

$$\left. \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^4 \sqrt{\frac{(c+d) \operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 (a+b \operatorname{Sin}[e+fx])}{-bc+ad}} \sqrt{\left(-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 (c+d \operatorname{Sin}[e+fx])}{-bc+ad}\right)} \right)$$

$$\left. \left( (a+b) d \sqrt{a+b \operatorname{Sin}[e+fx]} \sqrt{c+d \operatorname{Sin}[e+fx]} \right) \right)$$

**Problem 356: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Sin}[e + fx]}{(a + b \operatorname{Sin}[e + fx])^{3/2} (c + d \operatorname{Sin}[e + fx])^{3/2}} dx$$

Optimal (type 4, 544 leaves, 4 steps):

$$\frac{2 b (A b - a B) \operatorname{Cos}[e + f x]}{(a^2 - b^2) (b c - a d) f \sqrt{a + b \operatorname{Sin}[e + f x]} \sqrt{c + d \operatorname{Sin}[e + f x]}} -$$

$$\left( 2 (A (a^2 d^2 + b^2 (c^2 - 2 d^2)) - B (a^2 c d - b^2 c d + a b (c^2 - d^2))) \right.$$

$$\operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{c+d} \sqrt{a+b \operatorname{Sin}[e+f x]}}{\sqrt{a+b} \sqrt{c+d \operatorname{Sin}[e+f x]}}\right], \frac{(a+b)(c-d)}{(a-b)(c+d)}\right] \operatorname{Sec}[e+f x]$$

$$\left. \sqrt{\frac{(b c - a d) (1 - \operatorname{Sin}[e + f x])}{(a + b) (c + d \operatorname{Sin}[e + f x])}} \sqrt{-\frac{(b c - a d) (1 + \operatorname{Sin}[e + f x])}{(a - b) (c + d \operatorname{Sin}[e + f x])}} (c + d \operatorname{Sin}[e + f x])} \right) /$$

$$(\sqrt{a+b} (c-d) \sqrt{c+d} (b c - a d)^3 f) + \left( 2 (A b c + b B c - a A d - 2 A b d + a B d) \right.$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{c+d} \sqrt{a+b \operatorname{Sin}[e+f x]}}{\sqrt{a+b} \sqrt{c+d \operatorname{Sin}[e+f x]}}\right], \frac{(a+b)(c-d)}{(a-b)(c+d)}\right] \operatorname{Sec}[e+f x]$$

$$\left. \sqrt{\frac{(b c - a d) (1 - \operatorname{Sin}[e + f x])}{(a + b) (c + d \operatorname{Sin}[e + f x])}} \sqrt{-\frac{(b c - a d) (1 + \operatorname{Sin}[e + f x])}{(a - b) (c + d \operatorname{Sin}[e + f x])}} (c + d \operatorname{Sin}[e + f x])} \right) /$$

$$(\sqrt{a+b} (c-d) \sqrt{c+d} (b c - a d)^2 f)$$

Result (type 4, 2236 leaves):

$$\frac{1}{f} \sqrt{a + b \operatorname{Sin}[e + f x]} \sqrt{c + d \operatorname{Sin}[e + f x]}$$

$$\left( \frac{2 (A b^3 \operatorname{Cos}[e + f x] - a b^2 B \operatorname{Cos}[e + f x])}{(a^2 - b^2) (-b c + a d)^2 (a + b \operatorname{Sin}[e + f x])} - \frac{2 (B c d^2 \operatorname{Cos}[e + f x] - A d^3 \operatorname{Cos}[e + f x])}{(b c - a d)^2 (c^2 - d^2) (c + d \operatorname{Sin}[e + f x])} \right) +$$

$$\frac{1}{(a - b) (a + b) (c - d) (c + d) (-b c + a d)^2 f}$$

$$\left( -\frac{1}{(a + b) (c + d) \sqrt{a + b \operatorname{Sin}[e + f x]} \sqrt{c + d \operatorname{Sin}[e + f x]}} \right.$$

$$4 (-b c + a d) (a A b^2 c^3 - b^3 B c^3 - 2 a^2 A b c^2 d + 2 A b^3 c^2 d + a^3 A c d^2 - 2 a A b^2 c d^2 +$$

$$b^3 B c d^2 + 2 a^2 A b d^3 - 2 A b^3 d^3 - a^3 B d^3 + a b^2 B d^3) \sqrt{\frac{(c + d) \operatorname{Cot}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2}{-c + d}}$$

$$\left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 (c+d \operatorname{Sin}[e+f x])}{-b c + a d}}}{\sqrt{2}}}\right], \frac{2 (-b c + a d)}{(a + b) (-c + d)}\right] \right)$$

$$\begin{aligned}
 & \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^4 \sqrt{\frac{(c + d) \text{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 (a + b \text{Sin}[e + f x])}{-b c + a d}} \\
 & \sqrt{-\frac{(a + b) \text{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 (c + d \text{Sin}[e + f x])}{-b c + a d}} - \\
 & 4 (-b c + a d) (A b^3 c^3 - a b^2 B c^3 + a A b^2 c^2 d - 2 a^2 b B c^2 d + b^3 B c^2 d + a^2 A b c d^2 - 2 A b^3 c d^2 - \\
 & a^3 B c d^2 + 2 a b^2 B c d^2 + a^3 A d^3 - 2 a A b^2 d^3 + a^2 b B d^3) \left( \left( \sqrt{\frac{(c + d) \text{Cot}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{-c + d}} \right. \right. \\
 & \left. \left. \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{-\frac{(a + b) \text{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 (c + d \text{Sin}[e + f x])}{-b c + a d}}}{\sqrt{2}}}\right], \frac{2 (-b c + a d)}{(a + b) (-c + d)}\right] \text{Sec}[ \right. \right. \\
 & \left. \left. e + f x] \text{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^4 \sqrt{\frac{(c + d) \text{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 (a + b \text{Sin}[e + f x])}{-b c + a d}} \right. \right. \\
 & \left. \left. \sqrt{-\frac{(a + b) \text{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 (c + d \text{Sin}[e + f x])}{-b c + a d}} \right) \right. \right. \\
 & \left. \left. ((a + b) (c + d) \sqrt{a + b \text{Sin}[e + f x]} \sqrt{c + d \text{Sin}[e + f x]}) - \right. \right. \\
 & \left. \left. \left( \sqrt{\frac{(c + d) \text{Cot}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{-c + d}} \text{EllipticPi}\left[\frac{-b c + a d}{(a + b) d}, \right. \right. \right. \\
 & \left. \left. \left. \text{ArcSin}\left[\frac{\sqrt{-\frac{(a + b) \text{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 (c + d \text{Sin}[e + f x])}{-b c + a d}}}{\sqrt{2}}}\right], \frac{2 (-b c + a d)}{(a + b) (-c + d)}\right] \text{Sec}[e + f x] \right. \right. \\
 & \left. \left. \text{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^4 \sqrt{\frac{(c + d) \text{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 (a + b \text{Sin}[e + f x])}{-b c + a d}} \right. \right. \\
 & \left. \left. \sqrt{-\frac{(a + b) \text{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 (c + d \text{Sin}[e + f x])}{-b c + a d}} \right) \right. \right.
 \end{aligned}$$

$$\left( (a+b) d \sqrt{a+b \sin[e+fx]} \sqrt{c+d \sin[e+fx]} \right) +$$

$$2(-A b^3 c^2 d + a b^2 B c^2 d + a^2 b B c d^2 - b^3 B c d^2 - a^2 A b d^3 + 2 A b^3 d^3 - a b^2 B d^3)$$

$$\left( \frac{\cos[e+fx] \sqrt{c+d \sin[e+fx]}}{d \sqrt{a+b \sin[e+fx]}} + \right.$$

$$\left. \left( \sqrt{\frac{a-b}{a+b}} (a+b) \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{a-b}{a+b}} \sin\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]}{\sqrt{\frac{a+b \sin[e+fx]}{a+b}}}\right]\right], \right.$$

$$\left. \frac{2(-bc+ad)}{(a-b)(c+d)} \sqrt{c+d \sin[e+fx]} \right) / \left( b d \sqrt{\frac{(a+b) \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{a+b \sin[e+fx]}} \right)$$

$$\left( \sqrt{a+b \sin[e+fx]} \sqrt{\frac{a+b \sin[e+fx]}{a+b}} \sqrt{\frac{(a+b)(c+d \sin[e+fx])}{(c+d)(a+b \sin[e+fx])}} \right) -$$

$$\frac{1}{bd} 2(-bc+ad) \left( \left( (a+b)c+ad \right) \sqrt{\frac{(c+d) \cot\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{-c+d}} \operatorname{EllipticF}\left[ \right.$$

$$\left. \operatorname{ArcSin}\left[\frac{\sqrt{-\frac{(a+b) \csc\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \sin[e+fx])}{-bc+ad}}}{\sqrt{2}}\right], \frac{2(-bc+ad)}{(a+b)(-c+d)} \right] \operatorname{Sec}[e+fx]$$

$$\sin\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^4 \sqrt{\frac{(c+d) \csc\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (a+b \sin[e+fx])}{-bc+ad}}$$

$$\left( \sqrt{\left( -\frac{(a+b) \csc\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \sin[e+fx])}{-bc+ad} \right)} \right) /$$

$$\left( (a+b)(c+d) \sqrt{a+b \sin[e+fx]} \sqrt{c+d \sin[e+fx]} \right) -$$

$$\left( (bc + ad) \sqrt{\frac{(c + d) \operatorname{Cot}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{-c + d}} \operatorname{EllipticPi}\left[\frac{-bc + ad}{(a + b)d}, \operatorname{ArcSin}\left[\frac{(a + b) \operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 (c + d \operatorname{Sin}[e + fx])}{-bc + ad}\right]}{\sqrt{2}}\right], \frac{2(-bc + ad)}{(a + b)(-c + d)} \operatorname{Sec}[e + fx] \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^4 \sqrt{\frac{(c + d) \operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 (a + b \operatorname{Sin}[e + fx])}{-bc + ad}} \sqrt{\left(-\frac{(a + b) \operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 (c + d \operatorname{Sin}[e + fx])}{-bc + ad}\right)} \right) \left. \right) \left. \right) \left. \right)$$

**Problem 357: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Sin}[e + fx]}{(a + b \operatorname{Sin}[e + fx])^{3/2} (c + d \operatorname{Sin}[e + fx])^{5/2}} dx$$

Optimal (type 4, 858 leaves, 5 steps):



$$\begin{aligned}
 & \frac{2 b (A b - a B) \operatorname{Cos}[e + f x]}{(a^2 - b^2) (b c - a d) f \sqrt{a + b \operatorname{Sin}[e + f x]} (c + d \operatorname{Sin}[e + f x])^{3/2}} + \\
 & \frac{\left( 2 d (A (a^2 d^2 + b^2 (3 c^2 - 4 d^2)) - B (a^2 c d - b^2 c d + 3 a b (c^2 - d^2))) \operatorname{Cos}[e + f x] \right.}{\left. \sqrt{a + b \operatorname{Sin}[e + f x]} \right) / \left( 3 (a^2 - b^2) (b c - a d)^2 (c^2 - d^2) f (c + d \operatorname{Sin}[e + f x])^{3/2} \right) + \\
 & \frac{1}{3 \sqrt{a + b} (c - d)^2 (c + d)^{3/2} (b c - a d)^4 f} \\
 & \frac{2 (B (2 a^2 b c d (3 c^2 - d^2) - 2 b^3 c d (3 c^2 - d^2) - a^3 d^2 (c^2 + 3 d^2) + a b^2 (3 c^4 - 5 c^2 d^2 + 6 d^4)) +}{A (4 a^3 c d^3 - 4 a b^2 c d^3 - a^2 b d^2 (9 c^2 - 5 d^2) - b^3 (3 c^4 - 15 c^2 d^2 + 8 d^4))} \\
 & \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{c + d} \sqrt{a + b \operatorname{Sin}[e + f x]}}{\sqrt{a + b} \sqrt{c + d \operatorname{Sin}[e + f x]}}\right], \frac{(a + b) (c - d)}{(a - b) (c + d)}\right] \operatorname{Sec}[e + f x] \\
 & \sqrt{\frac{(b c - a d) (1 - \operatorname{Sin}[e + f x])}{(a + b) (c + d \operatorname{Sin}[e + f x])}} \sqrt{-\frac{(b c - a d) (1 + \operatorname{Sin}[e + f x])}{(a - b) (c + d \operatorname{Sin}[e + f x])}} (c + d \operatorname{Sin}[e + f x]) - \\
 & \left( 2 (B (a^2 d^2 (c + 3 d) - b^2 c (3 c^2 + 3 c d - 2 d^2) - 6 a b d (c^2 - d^2)) - \right. \\
 & \left. A (a^2 d^2 (3 c + d) - 6 a b d (c^2 - d^2) + b^2 (3 c^3 - 9 c^2 d - 6 c d^2 + 8 d^3))) \right) \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{c + d} \sqrt{a + b \operatorname{Sin}[e + f x]}}{\sqrt{a + b} \sqrt{c + d \operatorname{Sin}[e + f x]}}\right], \frac{(a + b) (c - d)}{(a - b) (c + d)}\right] \operatorname{Sec}[e + f x] \\
 & \sqrt{\frac{(b c - a d) (1 - \operatorname{Sin}[e + f x])}{(a + b) (c + d \operatorname{Sin}[e + f x])}} \sqrt{-\frac{(b c - a d) (1 + \operatorname{Sin}[e + f x])}{(a - b) (c + d \operatorname{Sin}[e + f x])}} (c + d \operatorname{Sin}[e + f x]) \Bigg) / \\
 & \left( 3 \sqrt{a + b} (c - d)^2 (c + d)^{3/2} (b c - a d)^3 f \right)
 \end{aligned}$$

Result (type 4, 2807 leaves):

$$\begin{aligned}
 & \frac{1}{f} \sqrt{a + b \operatorname{Sin}[e + f x]} \sqrt{c + d \operatorname{Sin}[e + f x]} \\
 & \left( -\frac{2 (A b^4 \operatorname{Cos}[e + f x] - a b^3 B \operatorname{Cos}[e + f x])}{(a^2 - b^2) (-b c + a d)^3 (a + b \operatorname{Sin}[e + f x])} + \frac{2 (-B c d^2 \operatorname{Cos}[e + f x] + A d^3 \operatorname{Cos}[e + f x])}{3 (b c - a d)^2 (c^2 - d^2) (c + d \operatorname{Sin}[e + f x])^2} - \right. \\
 & \left. (2 (6 b B c^3 d^2 \operatorname{Cos}[e + f x] - 9 A b c^2 d^3 \operatorname{Cos}[e + f x] - A b c^2 d^3 \operatorname{Cos}[e + f x] + 4 a A c d^4 \operatorname{Cos}[e + f x] - \right. \\
 & \left. 2 b B c d^4 \operatorname{Cos}[e + f x] + 5 A b d^5 \operatorname{Cos}[e + f x] - 3 a B d^5 \operatorname{Cos}[e + f x]) \Bigg) / \right. \\
 & \left. \left( 3 (b c - a d)^3 (c^2 - d^2)^2 (c + d \operatorname{Sin}[e + f x]) \right) \right) + \\
 & \frac{1}{3 (a - b) (a + b) (c - d)^2 (c + d)^2 (-b c + a d)^3 f} \\
 & \left( -\frac{1}{(a + b) (c + d) \sqrt{a + b \operatorname{Sin}[e + f x]} \sqrt{c + d \operatorname{Sin}[e + f x]}} \right)
 \end{aligned}$$

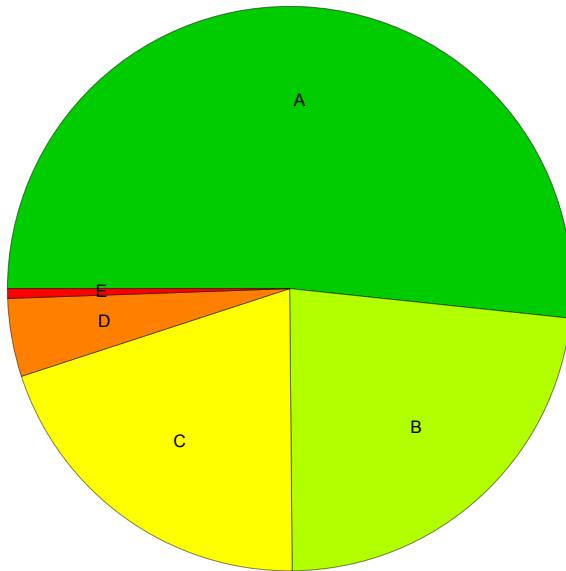
$$\begin{aligned}
 & 4 (-bc + ad) (-3aAb^3c^5 + 3b^4Bc^5 + 9a^2Ab^2c^4d - 9Ab^4c^4d - 9a^3Abc^3d^2 + 15aAb^3c^3d^2 - \\
 & \quad a^2b^2Bc^3d^2 - 5b^4Bc^3d^2 + 3a^4Ac^2d^3 - 20a^2Ab^2c^2d^3 + 17Ab^4c^2d^3 + 10a^3bBc^2d^3 - \\
 & \quad 10ab^3Bc^2d^3 + 5a^3Abcd^4 - 8aAb^3cd^4 - 4a^4Bcd^4 + 5a^2b^2Bcd^4 + 2b^4Bcd^4 + a^4Ad^5 + \\
 & \quad 7a^2Ab^2d^5 - 8Ab^4d^5 - 6a^3bBd^5 + 6ab^3Bd^5) \sqrt{\frac{(c+d) \operatorname{Cot}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{-c+d}} \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 (c+d \operatorname{Sin}[e+fx])}{-bc+ad}}}{\sqrt{2}}}\right], \frac{2(-bc+ad)}{(a+b)(-c+d)}\right] \\
 & \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^4 \sqrt{\frac{(c+d) \operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 (a+b \operatorname{Sin}[e+fx])}{-bc+ad}} \\
 & \sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 (c+d \operatorname{Sin}[e+fx])}{-bc+ad}} - \\
 & 4 (-bc + ad) (-3Ab^4c^5 + 3ab^3Bc^5 - 3aAb^3c^4d + 9a^2b^2Bc^4d - 6b^4Bc^4d - 9a^2Ab^2c^3d^2 + \\
 & \quad 15Ab^4c^3d^2 + 5a^3bBc^3d^2 - 11ab^3Bc^3d^2 - 5a^3Abc^2d^3 + 11aAb^3c^2d^3 - a^4Bc^2d^3 - \\
 & \quad 7a^2b^2Bc^2d^3 + 2b^4Bc^2d^3 + 4a^4Ac^2d^4 + a^2Ab^2cd^4 - 8Ab^4cd^4 - 5a^3bBcd^4 + 8ab^3Bcd^4 + \\
 & \quad 5a^3Abd^5 - 8aAb^3d^5 - 3a^4Bd^5 + 6a^2b^2Bd^5) \left( \sqrt{\frac{(c+d) \operatorname{Cot}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{-c+d}} \right) \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 (c+d \operatorname{Sin}[e+fx])}{-bc+ad}}}{\sqrt{2}}}\right], \frac{2(-bc+ad)}{(a+b)(-c+d)}\right] \operatorname{Sec}[ \\
 & \quad e+fx] \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^4 \sqrt{\frac{(c+d) \operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 (a+b \operatorname{Sin}[e+fx])}{-bc+ad}} \\
 & \left. \sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 (c+d \operatorname{Sin}[e+fx])}{-bc+ad}} \right) / \\
 & \left( (a+b)(c+d) \sqrt{a+b \operatorname{Sin}[e+fx]} \sqrt{c+d \operatorname{Sin}[e+fx]} \right) - \\
 & \left( \sqrt{\frac{(c+d) \operatorname{Cot}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{-c+d}} \operatorname{EllipticPi}\left[\frac{-bc+ad}{(a+b)d}, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \text{ArcSin}\left[\frac{\sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \operatorname{Sin}[e+fx])}{-bc+ad}}}{\sqrt{2}}}\right], \frac{2(-bc+ad)}{(a+b)(-c+d)}\right] \operatorname{Sec}[e+fx] \\
 & \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^4 \sqrt{\frac{(c+d) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (a+b \operatorname{Sin}[e+fx])}{-bc+ad}} \\
 & \left. \sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \operatorname{Sin}[e+fx])}{-bc+ad}}}\right) / \\
 & \left. \left( (a+b) d \sqrt{a+b \operatorname{Sin}[e+fx]} \sqrt{c+d \operatorname{Sin}[e+fx]} \right) + \right. \\
 & 2 \left( 3 A b^4 c^4 d - 3 a b^3 B c^4 d - 6 a^2 b^2 B c^3 d^2 + 6 b^4 B c^3 d^2 + 9 a^2 A b^2 c^2 d^3 - 15 A b^4 c^2 d^3 + \right. \\
 & \left. a^3 b B c^2 d^3 + 5 a b^3 B c^2 d^3 - 4 a^3 A b c d^4 + 4 a A b^3 c d^4 + 2 a^2 b^2 B c d^4 - 2 b^4 B c d^4 - \right. \\
 & \left. 5 a^2 A b^2 d^5 + 8 A b^4 d^5 + 3 a^3 b B d^5 - 6 a b^3 B d^5 \right) \left( \frac{\operatorname{Cos}[e+fx] \sqrt{c+d \operatorname{Sin}[e+fx]}}{d \sqrt{a+b \operatorname{Sin}[e+fx]}} + \right. \\
 & \left. \left( \sqrt{\frac{a-b}{a+b}} (a+b) \operatorname{Cos}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{a-b}{a+b}} \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]}}{\sqrt{\frac{a+b \operatorname{Sin}[e+fx]}{a+b}}}\right], \right. \right. \\
 & \left. \left. \frac{2(-bc+ad)}{(a-b)(c+d)} \sqrt{c+d \operatorname{Sin}[e+fx]} \right) / \left( b d \sqrt{\frac{(a+b) \operatorname{Cos}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{a+b \operatorname{Sin}[e+fx]}} \right. \right. \\
 & \left. \left. \sqrt{a+b \operatorname{Sin}[e+fx]} \sqrt{\frac{a+b \operatorname{Sin}[e+fx]}{a+b}} \sqrt{\frac{(a+b)(c+d \operatorname{Sin}[e+fx])}{(c+d)(a+b \operatorname{Sin}[e+fx])}} \right) - \right. \\
 & \left. \frac{1}{bd} 2(-bc+ad) \left( \left( (a+b) c + a d \right) \sqrt{\frac{(c+d) \operatorname{Cot}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{-c+d}} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{-\frac{(a+b) \text{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \text{Sin}[e+fx])}{-bc+ad}}}{\sqrt{2}}}\right], \frac{2(-bc+ad)}{(a+b)(-c+d)}\right] \\
 & \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^4 \sqrt{\left(\frac{1}{-bc+ad}(c+d) \text{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right.} \\
 & \quad \left.(a+b \text{Sin}[e+fx])\right) \sqrt{\left(-\frac{1}{-bc+ad}(a+b) \text{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \text{Sin}[e+fx])\right)} \\
 & \quad \left. e+fx\right) \Bigg] / \left((a+b)(c+d) \sqrt{a+b \text{Sin}[e+fx]} \sqrt{c+d \text{Sin}[e+fx]}\right) - \\
 & \left( (bc+ad) \sqrt{\frac{(c+d) \text{Cot}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{-c+d}} \text{EllipticPi}\left[\frac{-bc+ad}{(a+b)d}, \text{ArcSin}\left[\frac{\sqrt{-\frac{(a+b) \text{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \text{Sin}[e+fx])}{-bc+ad}}}{\sqrt{2}}}\right], \frac{2(-bc+ad)}{(a+b)(-c+d)}\right] \text{Sec}[e+fx] \right. \\
 & \quad \left. \text{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^4 \sqrt{\left(\frac{1}{-bc+ad}(c+d) \text{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right.} \right. \\
 & \quad \left. \left.(a+b \text{Sin}[e+fx])\right) \sqrt{\left(-\frac{1}{-bc+ad}(a+b) \text{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (c+d \text{Sin}[e+fx])\right)} \right. \\
 & \quad \left. (c+d \text{Sin}[e+fx])\right) \Bigg] / \left((a+b)d \sqrt{a+b \text{Sin}[e+fx]} \sqrt{c+d \text{Sin}[e+fx]}\right) \Bigg) \Bigg)
 \end{aligned}$$

## Summary of Integration Test Results

358 integration problems



- A - 185 optimal antiderivatives
- B - 83 more than twice size of optimal antiderivatives
- C - 72 unnecessarily complex antiderivatives
- D - 16 unable to integrate problems
- E - 2 integration timeouts